

Solvability for time-fractional semilinear parabolic equations with singular initial data

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Abstract

We discuss the existence and nonexistence of a local and global-in-time solution to the fractional problem $\begin{cases} \partial_t^\alpha u = \Delta u + f(u) & x \in \Omega, t > 0 \\ u = \varphi & x \in \Omega, t = 0 \end{cases}$ one has $|f(x) - f(\eta)| \leq C(1 + |x| + |\eta|)^{p-1} |x - \eta|$ for all $x, \eta \in \mathbb{R}$. Particular attention is paid to the doubly critical case $(p, r) = (1 + 2/N, 1)$.

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