

# Asymptotical mean-square stability of linear $\vartheta$ -methods for stochastic pantograph differential equations: variable stepsize and transformation approach

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## Abstract

The paper deals with the asymptotical mean-square stability of the linear  $\vartheta$ -methods under variable stepsize and transformation approach for stochastic pantograph differential equations. A limiting equation for the analysis of numerical stability is introduced by Kronecker products. Under the condition which guarantee the stability of exact solutions, the optimal stability region of the linear  $\vartheta$ -methods under variable stepsize is given by using the limiting equation, i.e.,  $\vartheta \in (1/2, 1]$ , which is the same to the deterministic problems. Moreover the linear  $\vartheta$ -methods under the transformation approach are also considered and the result of the stability is improved for  $\vartheta = 1/2$ . Finally, numerical examples are given to illustrate the asymptotical meansquare stability under variable stepsize and transformation approach.

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