Comparison of methods to derive the height-area relationship of shallow lakes in West Africa using remote sensing

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Abstract

In West Africa, lakes and reservoirs play a vital role as they are critical resources for drinking water, livestock, irrigation and fisheries. Given the scarcity of in situ data, satellite remote sensing is an important tool for monitoring lake volume changes in this region. Several methods have been developed to do this using water height and area relationships, but few publications have compared their performance over small and medium-sized lakes. In this work we compare four methods based on recent data from the Pleiades, Sentinel-2 and -3, ICESat-2 and GEDI missions over 16 lakes in the Central Sahel, ranging in area from 0.22 km² to 21 km². All methods show consistent results and are generally in good agreement with in situ data (height RMSE and volume NRMSE mostly below 0.30m and 11% respectively). The obtained height-area relationships show very little noise (fit RMSD mostly below 0.10m), except for the Sentinel-3-based method which tends to produce higher dispersion. The precision of the estimated water height is about 0.20m for Pleiades Digital Surface Models (DSMs) and less than 0.13m for the other methods. In addition, fine shape patterns are consistently observed over small height amplitudes, highlighting the ability to monitor shallow lakes with non-linear bathymetric behavior. Inherent limitations such as DSM quality, temporal coverage of lidar data, and spatial coverage of radar altimetry data are identified. Finally, we show that the combination of lidar and radar altimetry-based methods has great potential for estimating water volume changes in this region.
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Key Points:
• Four different remote sensing methods to derive volume changes of small and medium-sized shallow lakes have been intercompared.
• All methods, based on radar and lidar altimetry, Sentinel-2 water areas, and Pleiades Digital Surface Models, show good performances.
• Pros and cons of each method are identified and discussed.

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Abstract

In West Africa, lakes and reservoirs play a vital role as they are critical resources for drinking water, livestock, irrigation and fisheries. Given the scarcity of in-situ data, satellite remote sensing is an important tool for monitoring lake volume changes in this region. Several methods have been developed to do this using water height and area relationships, but few publications have compared their performance over small and medium-sized lakes. In this work we compare four methods based on recent data from the Pleiades, Sentinel-2 and -3, ICESat-2 and GEDI missions over 16 lakes in the Central Sahel, ranging in area from 0.22 km$^2$ to 21 km$^2$. All methods show consistent results and are generally in good agreement with in-situ data (height RMSE and volume NRMSE mostly below 0.30m and 11% respectively). The obtained height-area relationships show very little noise (fit RMSD mostly below 0.10m), except for the Sentinel-3-based method which tends to produce higher dispersion. The precision of the estimated water height is about 0.20m for Pleiades Digital Surface Models (DSMs) and less than 0.13m for the other methods. In addition, fine shape patterns are consistently observed over small height amplitudes, highlighting the ability to monitor shallow lakes with non-linear bathymetric behavior. Inherent limitations such as DSM quality, temporal coverage of DSM and lidar data, and spatial coverage of radar altimetry data are identified. Finally, we show that the combination of lidar and radar altimetry-based methods has great potential for estimating water volume changes in this region.

1 Introduction

Lakes store 87% of surface liquid freshwater on Earth (Gleick, 1993). Even though the main freshwater stocks are located in glaciers and underground (Oki & Kanae, 2006), lakes are a crucial component of the water cycle as they provide a readily accessible water resource. Their number is dominated by abundant small water bodies and ponds (Biggs et al., 2017) whereas medium-sized and large lakes (size $> 1$km$^2$) represent 85% of the global lake area (Pi et al., 2022). Lakes and reservoirs provide crucial services for humans (Reynaud & Lanzanova, 2017) and ecosystems (Schallenberg et al., 2013) such as freshwater and food supply, electricity, nutrients processing, natural habitats and recreational services. The capability of lakes to ensure these services inherently depends on their water storage.

Monitoring lake volume change is essential as several recent studies highlighted significant variations over the past decades. For instance, Wurtsbaugh et al. (2017) demonstrated that many of the world’s saline lakes are shrinking at an important rate. Yao et al. (2023) identified a decline of lake water volume over 53% of the 1972 largest global lakes, with the majority of the loss attributable to direct human activities and climate change. Even though lake desiccation trends are widespread, the Yao et al. study, consistently with Luo et al. (2022) and (Wang et al., 2018), also revealed regional patterns with net water volume gains in areas such as the Inner Tibetan Plateau and the Northern Great Plains of North America.

The hydrological functioning of water bodies in West Africa is poorly known at the large scale (Papa et al., 2023). Yet areas such as Central Sahel host a multitude of water bodies, ranging from reservoirs (Cecchi et al., 2009), small lakes and ponds (Gardelle et al., 2010; Grippa et al., 2019) and temporary water bodies (Haas et al., 2009), which are widespread but still relatively unknown in number. Being used for drinking water, livestock watering, irrigation and fishing, these water bodies play a vital role in such an area subject to a long dry season (Cecchi et al., 2009; Frenken, 2005). Despite the severe drought that impacted Central Sahel in the 1970s and 1980s, several studies have highlighted a paradoxical increase in the surface area of lakes and ponds (Baba et al., 2019; Gal et al., 2016; Gardelle et al., 2010), as well as an increase in runoff and river discharges (Descroix et al., 2018; Favreau et al., 2009; Mahe et al., 2010). Attempts to study the evolution of water volumes in West Africa have been carried out either at the scale of a few lakes (Fowe et al., 2015; Gal et al.,
2016; Pham-Duc et al., 2020), or at a larger scale but punctually in time (Annor et al., 2009; Cecchi et al., 2009; Liebe et al., 2005). In addition, West African lakes and reservoirs have been included in global studies, but these are brief in time (Cooley et al., 2021) or cover only a few large lakes (Luo et al., 2022; Yao et al., 2023). In this regard, efforts remain to be done for both long-term and large-scale monitoring of the lake volume changes in this region.

Historically, in-situ sensors are used to measure the evolution of lake water level and volume. However, the limited spatial coverage and the global decline of in-situ operations and installations (Papa et al., 2023; Riggs et al., 2023; Schwatke et al., 2015) challenge the capability to have long and large-scale time series. With periodic observations and a considerably increased spatial coverage, satellites are a relevant tool for assessing lake water volume trends globally.

Remote sensing allows measuring physical parameters of water bodies such as water surface height and area. Water surface height is derived from the return time estimation of electromagnetic waves emitted by nadir-looking radar or laser altimeters. Synthetic Aperture Radar (SAR) altimeters such as those on board Sentinel-3 and Sentinel-6 are able to measure the elevation of water bodies of a few hectares with a sub-monthly revisit time (Normandin et al., 2018; Taburet et al., 2020). However, these measurements still suffer from coarse across-track resolutions which may lead to contamination by bright surfaces located in the radar footprint (Boy et al., 2022). In addition, the nadir-viewing and the inter-track distance of several tens of kilometers of the conventional radar altimeters restrict their spatial coverage. The Ice, Cloud and land Elevation Satellite-2 (ICESat-2) and the Global Dynamics Ecosystem Investigation (GEDI) missions carry on board multi-beams laser altimeters enabling along-track surface elevation posting rate from tens of centimeters to tens of meters (Neuenschwander et al., 2023), (Dubayah et al., 2020). Nonetheless, these measurements remain discrete and their temporal coverage is limited by the multi-month revisit time of the satellites and some degraded acquisition periods for GEDI (Urbazaev et al., 2022).

The estimation of the water extent from optical or radar imagery observations is based on the separation of the spectral or backscattering signature of water from that of the soil (Pekel et al., 2016; Yao et al., 2019). With a revisit time of 5 days and a spatial resolution of up to 10m, the Sentinel-2 optical sensors can be used to monitor water surface area variations of a large number of lakes and reservoirs (Reis et al., 2021; Schwatke et al., 2019; Yang et al., 2017). Cloud cover, which is usually one of the main obstacles to optical observation of water bodies, is not a major problem in West Africa since the dry season lasts between 6 and 9 months (Nicholson, 2018).

Water surface height and area can be combined to calculate volume changes between consecutive observations. This is usually done by assuming that the observed portion of the lake behaves like a cone or pyramid frustum (Crétaux et al., 2016; Luo et al., 2022; Terekhov et al., 2020), or by multiplying the water level change by the average surface area between the two dates (Gao et al., 2012; Li et al., 2020; Song et al., 2013). These two solutions require simultaneous observations of water surface height and area and are based on geometric approximations whose accuracy decreases as the water level change increases. A third way consists of using the height-area relationship (Abileah et al., 2011), which synthesizes the lake’s bathymetry information into a relationship that describes changes in surface area as a function of water level. Once the height-area relationship has been constructed, volume change can be calculated by integration (Carabajal & Boy, 2021; Duan & Bastiaanssen, 2013; Magome et al., 2003) and using only one of the two variables.

The construction of the height-area relationship requires computing the height and extent of the lake banks contour lines (isobaths). With remote sensing data, isobaths are typically calculated by combining near-simultaneous (within a few days) observations of water surface height and area from radar or lidar altimetry data and imagery respectively.
Bank topography data such as global Digital Elevation Models (DEM) generated before impoundment or at low water levels have been combined with satellite images to retrieve the water surface elevation of lakes that cannot be observed by altimeters (Avisse et al., 2017; Bhagwat et al., 2019; Terekhov et al., 2020; Tseng et al., 2016). In addition, height-area relationships can also be generated through the analysis of a DEM alone. This method enabled studying the volume changes of many medium-sized and large lakes worldwide (Fang et al., 2019; Pan et al., 2013; Yao et al., 2018; S. Zhang & Gao, 2020). Publications such as Arsen et al. (2013); Bacalhau et al. (2022); Ma et al. (2019); N. Xu et al. (2020) have taken advantage of the high spatial resolution and vertical accuracy of lidar altimetry data to determine not the elevation of the water surface but that of the banks. Unlike DEMs, this bank topography data is discrete but, once intersected with water contours derived by satellite imagery, has shown great potential for bathymetry retrieval above the lowest observed water level.

In terms of intercomparison of methods, Magome et al. (2003) estimated volume change of Lake Volta in Ghana by comparing different methods using altimetry (TOPEX/Poseidon) and optical imagery (Moderate-Resolution Imaging Spectroradiometer, MODIS) or their combination with a DEM. They obtained better results when combining altimetry and DEM and highlighted the greater spatial coverage of the method using the combination of imagery and DEM. Zolà and Bengtsson (2007) also compared several methods over lake Poopó in Bolivia using echo-sounding measurements, combination of Landsat-5 with in situ water heights, and water balance calculations. They found consistent results and good complementarity between the different methods. Apart from these publications, both focusing on large lakes (> 100km²), few studies have attempted to intercompare different methods to provide height-area relationships, on smaller lakes and with recent data. The aim of this work is to intercompare four different methods based on recent data (Pleiades, Sentinel-2, Sentinel-3, ICESat-2, GEDI) over 16 small (<1km²) and medium-sized (1-100km²) lakes located in Central Sahel. The results of each method are evaluated using criteria of accuracy, precision, sensitivity to surface characteristics and spatio-temporal coverage. The study area, data and methods are described in Section 2 and the comparison results are presented in Section 3 and further discussed in Section 4.

2 Material and methods

2.1 Study area and in-situ data

The study area is mainly located in Central Sahel, between the 10.5°N and 15.5°N latitudes and extends over Mali, Niger and Burkina Faso (BF). From North to South, the climate is semi-arid and dry sub-humid. Rainfall is driven by a tropical monsoon system and follows a latitudinal gradient with mean annual precipitation ranging, from the North to the South, from 200mm yr⁻¹ to 1000mm yr⁻¹. Rainfall is concentrated during the wet season stretching from June to October. The rest of the year gives way to a long dry season with a very little cloud cover, which is suited for observing water bodies using optical imagery.

Sixteen lakes have been selected according to the in-situ and remote sensing data availability or to existing knowledge and documentation (Figure 1 and Table S1). They are spread along the climatic gradient and include three lakes in Mali, two in Niger and eleven in Burkina Faso.

Ten of these water bodies are reservoirs and others are natural lakes. Their mean altitude varies between 200 and 500m above mean sea level, their mean water surface area ranges from 0.22km² (Bangou Kirey) to 21km² (Kokorou), and most of them are relatively shallow (a few meters deep). These lakes show different optical water types with varied levels of turbidity, from moderately turbid (Robert et al 2016) to very turbid (e.g. lake Bangou Kirey, (Touré et al., 2016), and some of them harbor temporary or permanent aquatic vegetation (Gardelle et al., 2010; Baba et al., 2019).
Figure 1. Study area and lakes analyzed in this study.

in-situ data are of different nature and come from different sources. Water surface height data are measured continuously, every 30 minutes, through pressure transducers on the Bangou Kirey lake and the Arzuma reservoir, respectively since July 2022 and March 2023. Additional water surface height measurements have been collected on the Agoufou lake by AMMA-CATCH observatory (Galle et al., 2018) between 2015 and 2019 with a weekly or monthly frequency. Height-volume (H-V) relationships of the Burkinabe reservoirs of Bam, Seguenega and Seytenga have been provided by the Direction Générale des Ressources en Eau (DGRE) in Burkina Faso and come from topographic survey performed before the dams impoundment. Finally, the height-area (H-A) and height-volume-area (H-V-A) relationships of the Kokorou lake and the Toussiana reservoir are extracted respectively from the digitization of Baba et al. (2019) and from Sanogo and Dezetter (1997).

2.2 Satellite data, water surface area and height extraction

2.2.1 Water surface areas and contours from Sentinel-2 optical images

Sentinel-2A and -2B acquire high-resolution multispectral images with a revisit time of approximately 5 days (Table 1). The MultiSpectral Instrument (MSI) onboard Sentinel-2 has 13 spectral bands from blue to Short-Wave InfraRed (SWIR), with spatial resolution from 10m to 60m on the ground. For this study, we use the green and SWIR bands which have resolutions of 10m and 20m. Images are L2A Surface Reflectance (SR) products corrected from atmospheric effects with Sen2Corr processing. Images are downloaded through Google Earth Engine (GEE, (Gorelick et al., 2017)) as the "COPERNICUS/S2_SR" collection, over December 2018 to December 2022. All bands are downscaled to a pixel size of 20m x 20m and images with a percentage of cloudy pixels greater than 5% are discarded. The residual cloudy pixels are masked using the QA cloud and cirrus bitmasks, and an empirical threshold of 0.2 on the blue reflectance. After these steps, a few remaining images (usually
less than 5 per lake) contaminated by clouds or aerosols have been discarded after visual inspection.

To compute water surface area, we mask water pixels by applying a threshold on the MNDWI (H. Xu, 2006), which is a spectral index commonly used to detect water on optical images, based on the normalized difference between the green (B3) and the short-wave infrared (B12) bands.

\[
MNDWI = \frac{\text{green} - \text{SWIR}}{\text{green} + \text{SWIR}}
\]

First, we clip the images to the close surroundings of the water body to exclude close but unconnected water bodies. Then, the MNDWI is computed and the threshold, constant in time, is determined ad hoc for each lake following De Fleury et al. (2023) and Reis et al. (2021). Reis et al. (2021) have shown that water detection is usually accurate for a full range of MNDWI thresholds rather than a well-defined value. The water surface area is finally calculated by counting the number of pixels above the threshold and multiplying by the pixel area. The water contour is delineated using the marching squares algorithm, a 2D adaptation of the marching cubes algorithm (Lorensen & Cline, 1987) which is implemented in the “find contours” function from the Scikit-image Python package. This function takes as input the MNDWI pixels raster and the threshold value and generates iso-value contours at a sub-pixel scale by linearly interpolating the MNDWI pixel values. If the lake separates into several parts as it dries up, we keep only the largest part. For each lake, a time series of water surface areas and water contours is eventually generated.

### 2.2.2 Pleiades Digital Surface Model

Pleiades-1A and -1B Pleiades are two satellites equipped with a very high-resolution optical sensor acquiring panchromatic images (480-830nm) with a pixel size of 0.50m (Table 1 and Figure 3). We ordered the acquisition of pairs of cloud-free Pleiades panchromatic stereo-images (Pleiades ©CNES 2021, 2022, 2023, Distribution Airbus DS) over each lake, with a B/H ratio between 0.35 and 0.8. Pleiades images allow the creation of Digital Surface Models (DSM) by photogrammetric processing through the computation of matching pixels displacement between two stereo-images. DSMs were processed using the Digital Surface Model from OPTical stereoscopic very-high resolution imagery (DSM-OPT) online service, based on the MicMac tool (Rupnik et al., 2017) and operated by the Solid Earth ForM@Ter pole of the research infrastructure DATA TERRA. DSM-OPT also provides an ortho-image which is a panchromatic image georeferenced identically to the DSM.

Since DSM estimation by photogrammetry is challenging over the water surface due to low pixel correlation, we ordered Pleiades images at the end of the dry season, when water surface level is minimum, which allows exploring the maximum bank extent. We generated DSMs at 1m x 1m horizontal resolution, in line with Bagnardi et al. (2016). As the semi-arid landscapes of the study area often show small surface roughness (compared to mountainous or forest landscapes for instance), we adapted the correlation window size to 9 x 9 pixels and we used 0.2 as the minimum correlation coefficient for matching (Bagnardi et al., 2016). Due to the large extent of the Bam reservoir, two stereo-pairs acquisitions are needed to observe the northern and southern part of the reservoir. To end up with a single DSM, we generated a DSM for each part and we merged them after applying the Nuth and Kääb method (Nuth & Kääb, 2011) to ensure co-registration. However, a residual elevation bias between the two parts has been observed after co-registration. We corrected it by comparing the DSM of each part with terrain ICESat-2 data and subtracting the respective mean difference.

Some Pleiades DSMs showed along-track undulations which were highlighted when computing the difference with the GLO-30 Copernicus DEM (European Space Agency, 2021). For instance, we observed along-track undulations of several meters in Pleiades-1B-derived DSM of the Bangou Kirey and Kokorou lakes. These undulations have been noticed on many DEMs from several space-borne missions (Hugonnier et al., 2022) and are caused
by errors in the image geometry estimation due to sensor motion (jitter). Our method to correct for these undulations is partly based on Girod et al. (2017). We compute the average per line of the DEM difference with GLO-30 (Figure 2) and subtract it to the Pleiades DSM.

2.2.3 Bank elevation profile from ICESat-2 lidar altimeter data

The Ice, Cloud and land Elevation Satellite-2 (ICESat-2) was launched in September 2018 (Table 1 and Figure 3) by NASA (Markus et al., 2017). The Advanced Topographic Laser Altimeter System (ATLAS) onboard ICESat-2 is a photon-counting lidar with 3 pairs of laser beams emitting pulses at 10 kHz and separated by 3.3 km in the cross-track direction. The footprint size of each beam has a 14 m diameter. Each pair is composed of a strong beam and a weak beam (energy ratio of 4:1) with a wavelength of 532 nm and located 90 m from each other.

The ATL08 version 6 product is dedicated to land and vegetation and contains along-track heights above the WGS84 ellipsoid for the ground and canopy surfaces (Neuenschwander et al., 2023). We downloaded all ATL08 data over the October 2018 (first data available) - June 2023 period. The nominal posting rate is theoretically 100 m but data gaps can occur due to low signal-to-noise ratio or acquisition errors. For the mid-point of each 100 m segment, ATL08 provides three height metrics, respectively the mean, the median and the best-fit terrain height. The latter is the height resulting from the polynomial which best fits the 100 m terrain profile, among 1st, 3rd and 4th order polynomials. Since the topography of the banks is likely to vary inhomogeneously over 100 m, and as suggested by Tian and Shan (2021), we use the best-fit height in this study. Liu et al. (2021) assessed ICESat-2 ATL08 terrain height data accuracy against airborne lidar products over 40 sites located in the U.S. mainland, Alaska, and Hawaii. They showed that quite similar performances were obtained independently of beam energy, whereas strong beams should theoretically be more accurate because of their better signal-to-noise ratio. They also found nighttime terrain accuracy slightly better than daytime. However, daytime data represent a non-negligible proportion
of the ATL08 data quantity and consequently condition the spatial coverage. Hence, we
decided not to filter ATL08 data on the beam energy and acquisition time criteria.

Moreover, the number of terrain photons detected within a segment is important to fit
the 100 m height profile and derive a robust estimation of the segment height. Hence, we set
a threshold of 10 on the minimum detected number of terrain photons, in line with the results
of Urbazaev et al. (2022). To remove large outliers, we keep data with a photon heights STD
inferior to 1 m and discard data whose best fit height is inferior to the minimum detected
photon height, this being probably due to a fitting error. Finally, given that ICESat-2 beams
were purposely mispointing during the first height cycles of the mission, that is during the
two first years (nominal cycle of 91 days), certain lakes have irregular or limited temporal
coverage.

2.2.4 Bank elevation profile from GEDI lidar altimeter data

The Global Ecosystem Dynamics Investigation mission on board the International Space
Station started in December 2018 (Dubayah et al., 2020). It consists of a full-waveform lidar
with 3 lasers producing a total of 8 beam ground transects spaced 600 m apart in the cross-
track direction. Each ground transect has a footprint size of 30 m and samples the Earth’s
surface approximately every 60 m along-track (Table 1 and Figure 3). GEDI L2A version
2 data product, distributed by NASA’s Land Processes Distributed Active Archive Center
(LP DAAC), provides ground elevation, canopy top height and relative height metrics. The
ground elevation is represented by the lowest mode elevation which gives the height of the
last significant energy return detected in the waveform.

We removed large outliers by rejecting data whose elevation absolute difference with
the digital elevation model srtm value, a parameter in the product representing the Shuttle
Radar Topography Mission (SRTM) elevation at GEDI footprint location, was greater than
100 m. We also discarded data with a non-zero degrade_flg value, meaning that the lidar
shot occurred during a non-degraded period. As for ICESat-2 ATL08 data and following
the suggestions of Liu et al. (2021) who assessed GEDI L2A terrain height data accuracy
as well, we considered unnecessary to discard GEDI data on the basis of beam energy and
acquisition time.

2.2.5 Water surface heights from Sentinel-3 radar altimetry data

The Sentinel-3 (S3) mission includes the Sentinel-3A and 3B satellites carrying on
board the Synthetic Aperture Radar Altimeter (SRAL), a delay/Doppler altimeter (Table
1 and Figure 3). The altimeter operates in global mode with an along-track posting rate
of approximately 300 m and an across-track resolution of several kilometers. Water surface
height measurements of the same target are provided every 27 days. Water surface height
data have been retrieved from the radar waveforms recorded by Sentinel-3 with the Offset
Centre of Gravity (OCOG) retracking algorithm and have been provided by the Centre de
Topographie des Océans et de l’Hydrosphère (CTOH). They have been processed using the
Altimetric Time Series Software (AlTiS version 2.0, (Frappart et al., 2021)). The data were
first selected within a polygon fitted to the lake maximum water extent derived from the
corresponding water contour time series. Then, they were filtered with a threshold of 40 dB
on the backscattering coefficient for data acquired before January 2020, and a threshold of
20 dB for data acquired after January 2020 (De Fleury et al., 2023). These thresholds are
in line with what is suggested by Taburet et al. (2020) and Kittel et al. (2021). Besides,
multi-peak waveforms or dry-lake data were rejected with an empirical threshold of 20 on the
waveform peakiness. The resulting water surface height is computed as the median of the
remaining height values. Water surface heights with a Median Absolute Deviation (MAD)
along the transect greater than 1 m are rejected. For each lake, a water surface height time
series was eventually generated.
Figure 3. Data available over the Arzuma reservoir. Gray level background is the Pleiades DSM with the corresponding water mask in blue. Pressure transducer is represented by a black triangle. ICESat-2, unused and used GEDI data are respectively represented by green diamonds, yellow and red stars. Sentinel-3 theoretical ground track is represented by magenta crosses. Full, dashed and dotted black lines represent 3 selected water contours computed from Sentinel-2 images.
Table 1. Remote sensing data and corresponding mission used in this study.

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<th>GEDI</th>
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2.3 Methods to derive height-area relationships

2.3.1 DEM filling

This method uses an incremental approach to count DEM pixels whose elevation is between two given altitudes, and repeats the operation over a set of elevation increments until filling the entirety of the banks of the water body. Taking advantage of the DSM Pleiades vertical resolution, the incremental step between two successive elevations of the processing is empirically set to 0.1m. For each elevation increment, the corresponding pixel number is converted to an area by multiplying by the pixel area, and forms an elevation-area pair. All the elevation-area pairs form the H-A curve. Moreover, since the processing stops at an altitude defined manually, it is possible that, at a certain point, the computed water areas exceed the physical reality of the lake dynamics over the study period. The upper limit of the H-A relationship is therefore set to the maximum Sentinel-2-observed water area. For the following, this method will be referred to as the “DSM Pleiades” and is graphically represented in Figure 4a.

A Pleiades DSM footprint is at least 100km². We first limit the processed area to the region of interest by clipping the DSM to a polygon representing the close surroundings of the water body. Water surfaces generate “No Data” values or extreme outliers on the DSM due to low pixel correlations during the stereo-matching processing, and have to be filtered out. Hence, we mask water pixels on the orthoimage. Since orthoimage reflectance values generally follow a bi-modal distribution, we separate water from soil by defining a global threshold on the reflectance pixels. Finally, we mitigate the remaining minimal classification errors by filling the holes with a morphological closure using a square structuring element of size 9x9.

Once water has been masked, we determine the altitude of the water surface as the median elevation of the water pixels located along the contour. This contour is computed as the external morphological gradient using a cross structuring element of size 1. In addition, contamination by outliers is mitigated using the MADe method (Kannan et al., 2015).
2.3.2 Intersecting a DEM with water contours

This method is similar to what Mason et al. (1995-12-01) mentions as the “waterline method”, and multiple studies such as Ragettli et al. (2021) already employed it to retrieve lake bathymetry. Assuming the water surface is flat, isobaths can be computed as the intersection of water contours with a DEM. The water contours elevation is computed as the median value of the intersected DEM pixels elevations, consecutively to an outliers removal process based on the MADe method. Furthermore, we consider that the water contour must intersect a minimum number of DEM pixels, empirically set as 20. Finally, the lower limit of the H-A relationship is set to the minimum Pleiades-observed water area. For the application of this method on Pleiades DSMs, we will use the term ”DSM Pleiades/contours” (Figure 4b).

Since the Pleiades DSM are surface models, they provide elevation of the highest observed point on the ground. Thus, they are impacted by relief like buildings and, particularly for the studied lakes, trees and riparian vegetation. To mitigate this impact, we mask out the obvious wooded parts of the Pleiades DSMs. This is the case for the right banks of the Bangou Kirey lake. The Inbanta lake is densely covered in trees and if all of them were masked the remaining area would be too small to compute the H-A curve. Therefore, for this lake we do not mask out any area. The resulting impact of vegetation will be discussed later.

2.3.3 Intersecting bank elevation profile with water contours

Instead of using a whole DEM providing continuous information of the ground elevation, this method requires one or multiple discrete elevation profiles of the banks of the water body. Here, we use elevation profiles either from ICESat-2 or GEDI lidar topography measurements. This method will be referred to as the “Profile ICESat-2/contours” or “Profile GEDI/contours” method (Figure 4c). As with the DSM-based methods, the water level at the dates the elevation profiles were recorded determines the extent of the bank bathymetry that can be characterized. Isobaths are retrieved by calculating the intersections between the water contours and the banks elevation profile. For this purpose, the profiles are converted to geometric lines and we compute the crossover points with the water contour polygons. The crossover points elevation is linearly interpolated between the two measurement points. It is important to check that the pair of measurement points was acquired over the ground and not over water, and that they are located on the same bank, otherwise the resulting interpolated elevation will be erroneous. To do this, we mask out the measurement points acquired over water using the closest Sentinel-2 image in time.

We empirically set a maximal threshold of 2% on the bank slope to reject crossover points located at places too steep with respect to lidar data posting rate. Then, because it is more robust than the mean, the median value of the crossover points elevations is retained for the water contour elevation, following Arsen et al. (2013). Finally, we filter out water contours whose elevation is computed from only one crossover point, as it may reflect erroneous intersections due to small water contour detection errors. Given the multiplicity of the laser beams or the shape of some contours, we frequently have more than two crossover points per contour.

We observe large biases (tens of centimeters to tens of meters) between GEDI data from different dates of acquisition. For simplicity, we only select for each lake the acquisition date giving the most complete H-A curve. Most of the time, it results in selecting the latest acquisition date of the dry season.

2.3.4 Matching water surface height with water surface area measurements

This method uses water surface height data and combines them with synchronous water surface area observations. To construct the height-area relationship, we search for the
Figure 4. Schematic representation of the 4 methods used in this study to derive the height-area relationships.

Sentinel-2 images co-dated with the Sentinel-3 data and match the height and area measurements with a temporal tolerance of 3 days. A tolerance of 3 days is appropriate given the temporal variability of the lakes studied (De Fleury et al., 2023), and provides a good trade-off with respect to data availability. If the time difference between Sentinel-2 and Sentinel-3 acquisitions is not zero, we linearly interpolate successive water area data to the water surface height date. This method will be referred to as the "Height S3/area" method (Figure 4d).

2.4 Processing the height-area relationships

2.4.1 Processing the height-area relationships of in-situ data

For three reservoirs (Bam, Seytenga and Seguenega), in-situ data provided as H-V relationships have been converted to H-A relationships, computing the areas as the derivative of the volume with respect to the height \( A = \frac{dV}{dH} \) (Gao et al., 2012). For three lakes (Agoufou, Arzuma and Bangou Kirey), water surface height in-situ measurements are combined with Sentinel-2 water surface areas acquired on the same day. For Agoufou, since height data are acquired at a weekly frequency, Sentinel-2 areas are interpolated between two consecutive dates to match the in-situ data.

2.4.2 Resolving the bias between elevation data

As we do not have absolute elevation data for all methods, the comparison of the height-area relationships requires prior elevation bias removal. Indeed, the in-situ data and part of the Pleiades DSMs are not absolutely leveled, GEDI data showed acquisition time-dependent biases and the other remote sensing data have different references. The elevation biases are removed directly on the height-area curves. The DSM Pleiades/contours height-area method is taken as reference because it provides long and regular datasets, and the bias with the other methods is computed as the mean of the height differences:

\[
\text{bias} = \text{mean}(h_{\text{method}} - h_{\text{Pleiades}})
\]
2.4.3 Combining the height-area relationships based on open source data

The capabilities of the height-area relationships derived from methods based on open
source data only have been also assessed. This concerns Profile ICESat-2/contours, Profile
GEDI/contours and Height S3/area methods based on Sentinel-2 ICESat-2, GEDI and
Sentinel-3 data.

For each lake, we fit the H-A relationship of the three methods combined with the best
polynomial function of degree lower or equal to 2. Then, we discard the data outside the fit
95% confidence interval in order to remove the outliers. For the following, this method will
be referred to as the “Combined open source” method.

2.5 Processing the volume-area relationships

For each height-area dataset associated with a specific lake and method, water volume
changes are computed as the integral of the corresponding height-area function between
two consecutive heights (Yao et al., 2023; Abileah et al., 2011). To do this, the H-A
relationship is fitted and then integrated over H. A polynomial function (maximum degree
of 5) is used for the fit and the Akaike Information Criterion (citeAkaike1973 is used to
select the best fit and avoid overfitting. The volume-area relationship is finally given by
cumulating volume changes. Since the height of the lake bottom is not always known, the
reference is set to the “in-situ” data and all other methods are truncated to the minimum
in-situ volume. Volumes from the different methods are then computed as relative volumes
given by \( V_{method} - V_{0,\text{insitu}} \). Moreover, since the different datasets do not start at the same
water area, a dataset-specific volume offset called \( V_{0,\text{method}} \) has to be resolved. The offset
is computed as the mean difference with the in-situ dataset.

2.6 Methodology for the performance assessment of the different methods

Different metrics are used to assess the precision and accuracy of the different methods:

- Median Absolute Deviation
  \[
  MAD = \text{median}(|y_i - \text{median}(y)|)
  \]

- Coefficient of determination
  \[
  R^2 = 1 - \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y}_i)^2}
  \]

- Root Mean Squared Difference
  \[
  \text{RMSD} = \sqrt{\frac{1}{n} \sum_{i=0}^{n-1} (y_i - \hat{y}_i)^2}
  \]

- Normalized Root Mean Squared Difference
  \[
  \text{NRMSD} = \frac{\text{RMSD}}{y_{\text{max}} - y_{\text{min}}}
  \]

- Root Mean Squared Error
  \[
  \text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=0}^{n-1} (y_i - y_{\text{insitu}})^2}
  \]

- Normalized Root Mean Squared Error
  \[
  \text{NRMSE} = \frac{\text{RMSE}}{y_{\text{insitu,max}} - y_{\text{insitu,min}}}
  \]
where \( n \) is the number of observations, \( y_i \) the value observed by remote sensing, \( y_{\text{insitu}} \) the value observed in-situ, \( \hat{y}_i \) the predicted value and \( \bar{y}_i \) the mean value.

To assess the precision of the water heights retrieved by the different sources of elevation data, i.e. how flat these elevation data sources observe the water surface, we use the MAD because it is more robust to outliers than the standard deviation. The MAD is computed along the water transect for Sentinel-3 data and along the water contours estimated by Sentinel-2 for methods using Pleiades, ICESat-2 and GEDI data. For the last three methods, the dispersion estimate also includes water contour detection uncertainty and therefore does not allow a strict assessment of the precision of the water level data alone.

We provide information on the H-A curves dispersion using the \( R^2 \), height RMSD and height NRMSD of the A-H polynomial fits. The Normalized RMSD (NRMSD) is the RMSD divided by the amplitude of the height observations \((y_{\text{max}} - y_{\text{min}})\).

For the accuracy assessment of the heights and volumes, \( R^2 \), RMSE and NRMSE are used. Since lakes can have very different volumes, NRMSE provides a more comprehensive information compared to RMSE. in-situ H-A and A-V curves are interpolated to obtain height and volume matchups with data from the other methods.

### 3 Results

#### 3.1 Height-area relationships

The height amplitude observed by the remote sensing-based methods is ranging from 1.5 m (Agoufou, Bangui Mallam, Inbanta, Manga) to 4 m (Arzuma, Toussiana), with most amplitudes below 3 m (Figure 5). Fine shape patterns such as slope changes are well retrieved using the different methods and are in good agreement with in-situ data (e.g. Arzuma, Djigo, Kokorou, Tibin).

The methods relying on bank elevation data (Pleiades, ICESat-2 and GEDI) are dependent on the acquisition dates which limit the observable extent of the H-A curves. In the case of ICESat-2 data, the low number of data over the small lakes (Bangou Kirey, Manga, North Tanvi, South Tanvi) is also due to the fact that the laser beams only overpassed the lakes during the planned first two years of lidar mispointing. For Bangou Kirey, Pleiades, ICESat-2 and GEDI sensors overpassed the lake at a relatively high water level, not allowing exploring the full H-A curve. Conversely, simultaneous observations of in-situ water level and Sentinel-2-derived area are not available for the highest water levels, which occur for only a few days during the rainy season when cloud cover is a problem for optical imagery. Therefore, it remains difficult to compare in-situ and satellite estimates for this lake.

Complete drying of some lakes during the dry season increases the H-A curves extent but also introduces errors in the Pleiades DSM. Indeed the H-A relationships derived by the DSM Pleiades method show hockey cross patterns for Inbanta and North Tanvi. For these lakes which dried up, the water contour could not be used to estimate the starting altitude as described in Section 2.3.1, which has been set to 310 m for Inbanta and 296 m for North Tanvi. The presence of high noise in the DSM challenged other solutions to derive the starting altitude, such as for example using the minimum DSM elevation within the lake polygon. The location of the noisy DSM pixels is confirmed by areas of low pixel correlations corresponding to smooth surfaces such as, for instance, the lake bottom for North Tanvi (Figure 6). The noise leads to troughs several meters deep which force the starting altitude (lake bottom) to be underestimated. These pixels are filled progressively with small changes in lake area, which explains the observed hockey cross pattern. As soon as the lake is not completely dry, the average elevation computed over the smallest water area smooths the noise and gives a correct minimum water elevation. For Inbanta, we also note a difference between the DSM Pleiades and the DSM Pleiades/contours curves reflected by overestimated water areas within the two first thirds of the DSM Pleiades curve. This
Figure 5. Height-area relationships derived from all the methods a) over the lakes with in-situ data and b) over the other lakes.
Figure 6. Data available over North Tanvi reservoir. We show a zoom on Pleiades DSM pixels over the bottom of the reservoir. The amplitude of the DSM noise exceeds 1.5m in some places.

difference is also attributed to the DSM noise, the resulting troughs causing a substantial quantity of pixels to be prematurely filled.

3.2 Volume-area relationships

The V-A curves also denote a generally good agreement between the different methods (Figure 7). Some small slope differences observed on the H-A curves comparison are more evident on the volume-area curves (e.g. DSM Pleiades over Kokorou lake), which is partly due to error propagation in the calculations. The largest differences with respect to in-situ data are observed over Bam and Seytenga reservoirs, where all remote sensing methods agree well with each other and differ from in-situ data. Part of these discrepancies may be due to bank erosion and sedimentation (Cecchi et al., 2020), with sediment transfer from the lake edge mainly due to land use (Tully et al., 2015) and wave-induced bank erosion (Hilton, 1985). For example, Boena and Dapola (2001) documented the Bam reservoir silting and showed that the sediment deposits in the lake could be of substantial thickness.

3.3 Quantitative results

3.3.1 Dispersion of the area-height relationship

All methods provided good fit results with almost all $R^2$ above 0.80 and most values above 0.90 (Table 2). The DSM Pleiades method outperforms all the other methods with all RMSD values below 0.03m, except for two lakes (Inbanta and North Tanvi) where RMSD equals 0.21m and 0.15m, respectively. The DSM Pleiades/contours, Profile ICESat-2/ and Profile GEDI/contours methods show good and consistent results with all RMSD values below 0.14m, most being below 0.10m. The Height S3/area method tends to produce curves
Figure 7. Volume-area relationships derived from the different methods over the lakes with in-situ data.
with dispersion values almost systematically greater than those from other methods. RMSD is between 0.09m and 0.34m, with 4 lakes having RMSD above 0.20m. A small part of this dispersion is inherently related to the time interpolation required to match water surface height and area measurements.

### 3.3.2 Precision of water elevation

The median MAD obtained using the different sources of elevation data (Figure 8) are respectively between 0.11m and 0.70m with most values below 0.20m for Pleiades, between 0.04m and 0.19m with most values below 0.13m for ICESat-2, between 0.04m and 0.23m with most values below 0.13m for GEDI, and between 0.01m and 0.12m with most values below 0.06m for Sentinel-3. Therefore, all sources of elevation data provide good results.

The number of points per contour/transect used to compute the precision varies with the methods and highly depends on lake size and, especially for Sentinel-3, and on the satellite’s track attack angle with respect to the lake banks. The median number of points per contour ranges from 675 (Babou) to 4260 (Tibin) for Pleiades DSMs, from 2 (North Tanvi) to 50 (Bam) for ICESat-2, from 2 (Bangou Kirey) to 20 (Tibin) for GEDI (mainly because we selected only one acquisition date) and from 1 (Toussiana) to 12 (Bam) per transect for Sentinel-3.

The relatively low precision of Pleiades DSMs (> 0.40m) over certain lakes can be explained either by high amplitudes of noise due to very smooth areas or by flooded vegetation and trees. It is not surprising that the precision of Pleiades is poorer than other data sources, as we have chosen to generate the DSMs at a spatial resolution of 1m x 1m, which introduces more pixel-to-pixel noise than a coarser resolution. The average precision of 0.04m for Sentinel-3 must be taken carefully because for half of the lakes, the transects are made of a median number of 3 points or less. Except for these cases, all sources of data show a good precision stability with Inter-Quartile Ranges (IQR) < 0.20m.

### 3.3.3 Height-area and volume-area relationships accuracy

For all methods, the height RMSE is between 0.03m and 0.42m with most values below 0.30m and the height NRMSE is between 1.3% and 13.7% with most values below 8%. Some methods are missing for some lakes. They all perform well on the common lakes but not similarly from one lake to another. However, we do not observe systematic differences between one method and another. Heights derived from Sentinel-3 give higher RMSE and NRMSE on certain lakes. One of the reasons might be that radar altimeter waveforms are affected by crops or other water bodies surrounding the reservoir that generate relatively high backscattering (Arzuma). The other reason is the limitation of the radar altimeter along-track resolution. This can occur with small water bodies (noise observed for Babou and Manga lakes) or larger water bodies whose orientation with respect to the altimeter ground track generates narrow transects (Toussiana). Since these transects are made of very few measurements, they are more likely to provide larger errors.

For all methods, the volume RMSE is between 0.03Mm$^3$ and 8.72Mm$^3$ with most values below 5Mm$^3$ and the volume NRMSE is between 2.3% and 15.8% with most values below 11% (Table 3 and Figure 9). Similarly to the height statistics, we do not observe systematic differences between one method and another, or between one lake and another. Nevertheless, Profile GEDI/contours and Height S3/area methods are particularly impacted by some higher RMSEs due to the dispersion in the volume-area curve. In addition, some poor performances have been improved when going from height to volume accuracy, whereas some good performances have been reduced. This observation reflects that volume accuracy is not only a matter of height-area relationship accuracy and dispersion, but also a matter of height-area shape. This statement is supported by the results over Toussiana reservoir, where the difference between the Height S3/area method and the others methods are much
Table 2. Polynomial fit statistics of the area-height relationships.

<table>
<thead>
<tr>
<th>Location</th>
<th>DSM Pleiades</th>
<th>DSM Pleiades/contours</th>
<th>Profile ICESat-2/contours</th>
<th>Profile GEDI/contours</th>
<th>Height S3/area</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Polynomial degree / $R^2$ / RMSD (m) / NRMSD (%)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Agoufou</td>
<td>5 / &gt; 0.99 / &lt; 0.01 / 0.04</td>
<td>5 / 0.99 / 0.02 / 1.32</td>
<td>4 / 0.99 / 0.04 / 2.1</td>
<td>5 / 0.98 / 0.02 / 0.92</td>
<td></td>
</tr>
<tr>
<td>Arzuma</td>
<td>5 / &gt; 0.99 / 0.01 / 0.23</td>
<td>3 / 0.99 / 0.08 / 2.04</td>
<td>5 / 0.8 / 0.09 / 2.26</td>
<td>4 / 0.96 / 0.12 / 3.17</td>
<td>1 / 0.81 / 0.34 / 8.59</td>
</tr>
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<td>Babou</td>
<td>5 / &gt; 0.99 / 0.01 / 0.62</td>
<td>5 / &gt; 0.99 / 0.03 / 1.36</td>
<td>5 / 0.98 / 0.05 / 2.23</td>
<td>5 / 0.98 / 0.05 / 2.21</td>
<td>4 / 0.96 / 0.12 / 5.58</td>
</tr>
<tr>
<td>Bam</td>
<td>5 / &gt; 0.99 / 0.03 / 0.82</td>
<td>5 / 0.95 / 0.12 / 3.82</td>
<td>5 / 0.97 / 0.09 / 2.93</td>
<td>4 / 0.93 / 0.1 / 3.14</td>
<td>2 / 0.98 / 0.1 / 3.23</td>
</tr>
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<td>Bangou Kirey</td>
<td>5 / &gt; 0.99 / &lt; 0.01 / 0.09</td>
<td>2 / 0.9 / 0.09 / 5.25</td>
<td>1 / 0.31 / 0.08 / 4.61</td>
<td>4 / 0.87 / 0.03 / 1.52</td>
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<tr>
<td>Bangui Mallam</td>
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<tr>
<td>Djigo</td>
<td>5 / &gt; 0.99 / 0.03 / 1.06</td>
<td>5 / 0.99 / 0.07 / 2.31</td>
<td>5 / 0.99 / 0.07 / 2.3</td>
<td>5 / 0.97 / 0.07 / 2.58</td>
<td>5 / 0.96 / 0.13 / 4.48</td>
</tr>
<tr>
<td>Inbanta</td>
<td>5 / 0.98 / 0.21 / 3.36</td>
<td>3 / 0.8 / 0.14 / 2.36</td>
<td>5 / 0.96 / 0.07 / 1.18</td>
<td>5 / 0.94 / 0.07 / 1.13</td>
<td>1 / 0.68 / 0.24 / 3.88</td>
</tr>
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<tr>
<td>Manga</td>
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<td>3 / 0.97 / 0.09 / 5.64</td>
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<td>North Tanvi</td>
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<td>Seguenega</td>
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<td>Seytenga</td>
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<td>4 / 0.99 / 0.04 / 1.92</td>
<td>5 / 0.99 / 0.03 / 1.58</td>
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<td>3 / 0.94 / 0.1 / 4.9</td>
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<td>5 / 0.99 / 0.04 / 1.57</td>
<td>2 / 0.97 / 0.1 / 4.02</td>
</tr>
<tr>
<td>Toussiana</td>
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<td>2 / 0.99 / 0.07 / 1.8</td>
<td>1 / 0.94 / 0.3 / 7.3</td>
</tr>
</tbody>
</table>
Figure 8. Box plot of the water elevation precision achieved by the different data sources. For each lake in x-axis, we plot the distribution of the water elevation precision in y-axis. The precisions computed for each transect/contour are stacked into a box reflecting the 25th, 50th and 75th percentiles of the distribution. Water elevations resulting from only one measurement are rejected.
Figure 9. Comparison between relative volumes from in-situ (x-axis) and from other methods (y-axis). The 1:1 curve is plotted as grey dashed line.
lower when looking at the volume accuracy than the height accuracy metrics. We think that this is mainly due to the shape of the Height S3/area-derived height-area relationship that allows the volume-area relationship to fit the in-situ data more closely (Figure 5).

Table 3. Accuracy statistics of height and volume.

<table>
<thead>
<tr>
<th></th>
<th>DSM Pleiades</th>
<th>DSM Pleiades/contours</th>
<th>Profile ICESat-2/contours</th>
<th>Profile GEDI/contours</th>
<th>Height S3/area</th>
<th>Combined open source</th>
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<td></td>
<td>– Height –</td>
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<tr>
<td></td>
<td>$R^2$</td>
<td>RMSE (m)</td>
<td>NRMSE (%)</td>
<td>$R^2$</td>
<td>RMSE (m)</td>
<td>NRMSE (%)</td>
</tr>
<tr>
<td>Agoufou</td>
<td>&gt; 0.99 / 0.03 / 2.31</td>
<td>0.98 / 0.04 / 2.62</td>
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<tr>
<td>Arzuma</td>
<td>0.99 / 0.09 / 3.11</td>
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<td>0.32 / 0.15 / 5.13</td>
<td>0.92 / 0.17 / 5.45</td>
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<td>0.94 / 0.15 / 5.11</td>
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3.4 Combining all height-area curves from open source data

When combining the methods based on open source data (Figure 10), the results give height RMSE between 0.05m and 0.25m and height NRMSE between 1.7% and 8.9% with most values below 6%. The volume RMSE is between 0.04Mm$^3$ and 8.72Mm$^3$ with most values below 1.44Mm$^3$, and the volume NRMSE is between 4.2% and 15.8% with most values below 10.3% (Table 3). Except for a few lakes, these results are comparable to that obtained with the Profile ICESat-2/contours method alone.

4 Discussion

4.1 Comparison with the literature

4.1.1 Precision and accuracy of the area-height relationships

Many publications (Schwatke et al., 2020; Busker et al., 2019; Li et al., 2020; Chen et al., 2022) show similar results to those shown in 3.3.1 about the dispersion in the area-height relationships, and reported high values of $R^2$ (>$0.90$). This is expected as water surface height and area are correlated. Our results with the Height S3/area method (RMSD values between 0.09m and 0.34m, with average being 0.16m) are slightly better that those of...
Figure 10. Combination of height-area curves from ICESat-2-, GEDI- and Sentinel-3-based methods for a) lakes with in-situ data and b) other lakes.
Schwatke et al. (2020) who reported RMSD values between 0.15m and 0.53m, and average of 0.27m, over 6 Texan lakes having a number of points comparable to that of our curves (e.g. 32 points or less). Schwatke et al. (2020) used altimetry data from multiple missions with different accuracy, allowed a time lag of up to 10 days between water surface height and area data acquisitions, and did not perform time interpolation to generate the matchups, which may cause slightly larger RMSD.

Regarding the height-area relationship accuracy, most RMSE values are below 0.30m. Li et al. (2020) obtained RMSE values of 0.06m, 0.47m, 0.76m and 1.20m over four medium-sized lakes (1-100km$^2$) when validating their height-area curves derived from the combination of either ICESat, Hydroweb (https://hydroweb.theia-land.fr) (Crétaux et al., 2011) or G-REALM (https://ipad.fas.usda.gov/cropexplorer/global_reservoir/) (Birkett et al., 2011) altimetry data with water areas from the Joint Research Center (JRC) Global Surface Water (GSW) dataset (Pekel et al., 2016). Part of the difference with our results may be explained by elevation biases between remote sensing and in-situ data reported in the study of Li et al. (2020).

### 4.1.2 Precision of the height estimations

The water elevation precision along lake contours has been assessed in Section 3.3.2, with values ranging between 0.04m and 0.19m, and most values below 0.13m. Five lakes show a precision better or equal to 0.08m. These values are in line with Arsen et al. (2013) who reported water contour elevation standard deviations ranging from 0.02m to 0.11m when intersecting ICESat 170m posting rate banks elevation profiles with water contours over lake Poopo in Bolivia.

For GEDI, we did not find assessment of the water elevation precision along contour lines in the literature. If we compare the water contour elevation precision with values obtained along transects over water from other publications, our results (precision between 0.04m and 0.23m, with most values below 0.13m) are in line with Z. Zhang et al. (2023) who studied the water level dynamics of Qinghai Lake with GEDI data. The large biases noted on GEDI profiles from different acquisition dates were also pointed out by Fayad et al. (2020), and require further investigations.

For Sentinel-3, Taburet et al. (2020) reported a median standard deviation of water elevation of 0.17m. This is consistent but slightly higher than our results, which is expected as Taburet et al. (2020) studied thousands of water bodies, including rivers. Also, the use of the median absolute deviation in our study provides better results compared to using the standard deviation. More generally, standard deviations of a few centimeters have already been achieved over larger lakes with radar altimeters previous to Sentinel-3 (Crétaux & Birkett, 2006). This study shows that such a performance can be achieved on small and medium-sized lakes as well.

### 4.1.3 Water area estimations

The MNDWI threshold for water classification has been determined ad hoc for each lake. Using the same spectral index, we also tested automatic methods based on histogram analysis such as Otsu (Otsu, 1979) and Minimum Error Thresholding (Kittler & Illingworth, 1986). Both methods assume that the MNDWI distribution is bi-modal with two classes respectively associated with land and water. The Otsu’s method determines the optimal threshold as the value which maximizes the inter-class variance and the MET method assumes that the histogram is a mixture of two gaussian-like distributions associated with the respective classes. Both methods were found to perform poorly in particular for lakes covered by aquatic vegetation (tri-modal histograms) or for lakes almost dried out (monomodal histograms for some dates). Consequently, we decided to follow De Fleury et al. (2023) and use ad hoc MNDWI thresholding. For some lakes, fairly negative threshold values have been
selected to account for aquatic vegetation (Table S1). We acknowledge that spatio-temporal variations in spectral signature of the lake or atmospheric conditions may lead to underestimation or overestimation of the water surface area, but ad hoc thresholding allows for a more consistent time series. The accuracy of the water surface areas has not been directly assessed but the results of Section 3.3.2 indicate that the precision of the water contours elevation is of the order of 0.10m to 0.20m. This, combined with the satisfactory height-area relationships dispersion and accuracy, reflects a good water contours detection accuracy and proves ad hoc MNDWI thresholding to be efficient for our study.

4.1.4 Accuracy of the volume-area relationships

We reported volume NRMSE between 2.3% and 15.8%, with most values below 11%. This is in line with Busker et al. (2019) who validated volume variations derived from the combination of radar altimetry and GSW monthly areas over 18 global lakes and reservoirs and obtained NRMSE between 1.784% and 18.872% with most values below 11% (extrapolated volumes excluded). Schwatke et al. (2020) also obtained similar results with NRMSE (defined as the RMSE divided by the difference of the 95% percentile and the 5% percentile of the height variations) varying between 2.8% and 14.9%, with an average of 8.3%, when validating against in-situ volume variations. The in-situ data used in our study come from various sources (with errors difficult to estimate) and may induce different uncertainties during the comparisons.

4.2 Pros and cons of each method

4.2.1 Pleiades-based methods

Pleiades-based height-area relationships show generally good performance in terms of accuracy, water elevation precision and dispersion. In particular, those derived from the DSM Pleiades method have the advantage of relying on a single data source. However, our study shows that despite their very high spatial resolution, Pleiades DSMs should be subjected to preliminary quality checks for issues related to jitter and high noise due to low pixel correlation, which can introduce errors of several meters. Dried out lake Pleiades DSMs allow characterizing the topography of the whole lake bathymetry but also represent a challenge for the estimation of the lake bottom altitude. Indeed in the absence of water, determining the starting altitude of the height-area relationship is not straightforward as the lake bottom may show high noise. In this study we manually selected a starting altitude from which water areas increase significantly. Alternative options might be to use the elevation from an external water contour intersected with the DSM, or to correct for the amplitude of the noise estimated over a flat area. If the noise is more widely spread over the banks (not only on the lake bottom but also on higher parts of the banks), reducing the starting altitude is mandatory in order not to underestimate the water areas subsequently computed.

The DSM Pleiades/contours method, which combines Pleiades DSMs with water contours, requires an additional data source compared to the DSM Pleiades method but is not affected by the effect of dry lake noise on the starting elevation of the curves, as these are truncated to the minimum water contour extent. More generally, Pleiades DSMs represent the surface elevation, and thus remain affected by all kinds of relief such as vegetation whose footprint on the DSMs is often wider due to smoothing in the DSM generation processing.

4.2.2 Lidar-based methods

Profile ICESat-2/ and Profile GEDI/contours methods are able to generate accurate height-area relationships over small to medium-sized lakes with sometimes a single but more often a few numbers of bank elevation profiles. Furthermore, these relationships are consistent with very high resolution DSM-based curves and highlight the potential of existing lidar altimetry missions for lake volume changes monitoring. We also note that the satis-
factory water elevation precision obtained with ICESat-2 and GEDI data suggests that the algorithm implemented in the respective operational products used in this study properly separate echos from tree canopy and ground. Nonetheless, the methods face some limitations. Among them, the height-area relationship quality depends on the lake’s shape and the attack angle of the lidar altimeter ground tracks with respect to the water contours. The more parallel to the lake the trajectory is, the bigger the impact of water detection errors on the resulting contour elevation will be. The location of the lidar profiles is important as well since it also conditions the sensitivity of the methods to water detection errors (as it could be the case for dendritic lakes or profiles located close to the shore). The lidar data posting rates of respectively 60m and 100m represent a limitation with respect to the range of bank slope that can be observed. A threshold on the bank slope must be applied to prevent errors induced by linear interpolation of the topography or water detection which is more challenging as the banks get steeper. Another limitation of ICESat-2 (nominal revisit time of 91 days, drifting orbit during the first two years of the mission) and GEDI (variable revisit time) data is the temporal coverage which conditions the observable volume dynamics. In addition, GEDI suffers from some degraded acquisition periods (Urbazaev et al., 2022). Finally, being optical sensors, lidars are not suited to areas with important cloud cover. In this study we were not significantly impacted by this effect as the dry season, with very low or absent cloud cover, represents the major part of the year in the study area.

4.2.3 Height S3/area method

As well as lidar data, Sentinel-3 data are less impacted by relief than the Pleiades DSMs and better separate water from flooded vegetation, as suggested by the comparison between Height S3/area and Pleiades-based height-area relationships over the Inbanta lake. One of the advantages of Sentinel-3 data, in addition to having no trouble with cloud cover, is also the temporal coverage (revisit time of 27 days) which excludes the acquisition dates dependency associated with the other methods and may allow observing a greater water volume dynamics. Even more frequent revisit time is possible with Sentinel-6 data (10 days) but the spatial coverage decreases substantially (e.g. only one of the lakes studied is covered by Sentinel-6). Nonetheless, despite good water surface height precision (below 0.10m for most lakes), the Height S3/area method tends to generate height-area relationships with more dispersion (Section 3.3.1). In addition to the impact of time interpolation for matching S2 and S3 data, part of these errors might be attributed to contamination of the radar waveform by surrounding bright surfaces such as crops, humid soils or neighboring water bodies which challenge the retracking (Boy et al., 2022).

4.3 Learnings from this study

4.3.1 Characterization of small and shallow water bodies

Overall, the methods were able to derive consistent height-area relationships of small and medium-sized lakes with areas ranging from tens of hectares to tens of square kilometers and small height amplitudes about 1.5m. This result represents a step forward for volume change monitoring of shallow lakes. Indeed, multiple publications in the literature focus on lakes with higher water level amplitude or use 1m-vertical resolution DEM such as SRTM data to estimate height-area relationships or volume changes (Fang et al., 2019; S. Zhang & Gao, 2020; Pan et al., 2013; Yao et al., 2018).

The slope breaks and curvatures consistently observed on the height-area relationships of some lakes such as Djigo, Kokorou and Tibin (Figure 5) are of particular interest as they reveal fine shape behaviors. Since multiple existing studies (Gao et al., 2012; Crétaux et al., 2015; Busker et al., 2019; Smith & Pavelsky, 2009; S. Zhang & Gao, 2020; Bhagwat et al., 2019; Fang et al., 2019; Li et al., 2020; Chen et al., 2022), consider linear, quadratic or power-law regressions to fit the height-area relationship, our observations show that such
assumptions might be unsuited to capture complex shape patterns in the case of small and medium-sized lakes.

### 4.3.2 Spatial coverage and data accessibility

Pleiades images are commercial data, so they are not open-access. We tested the potential of open-access global DEMs such as SRTM data to produce height-area relationships. For this, the DEM filling method has been used on the SRTM DEM of each of the sixteen lakes studied. With the exception of the Tibin reservoir, which is among the largest studied lakes (mean area of 15.39km²) and was not impounded yet during the SRTM acquisition, the resulting height-area relationships showed a general disagreement with all other methods as they were almost systematically steeper. Moreover, the 1-m vertical resolution of SRTM, as well as that of other global DEMs such as the ALOS Global Digital Surface Model (AW3D30) or the ASTER Global Digital Elevation Map (GDEM), is insufficient to capture water surface height variations of a few meters that we commonly observe. GLO-30 Copernicus DEM has a better vertical resolution but represents a 2011-2015 averaged topography from multiple DEMs derived from the TanDEM-X mission and acquired with different water levels. Hence, bank topography must be regarded carefully as it may contain contributions from water.

Due to the spatial coverage limitation of the conventional altimetry missions, none of the studied lakes are included in the global databases such as Hydroweb, G-REALM or the Database for Hydrological Time Series of Inland Waters (DAHITI, https://dahiti.dgfi.tum.de/en) (Schwatke et al., 2015). De Fleury et al. (2023) intersected Sentinel-3A and Sentinel-3B altimeter ground tracks with the lakes maximum water extent from GSW dataset over Central Sahel and estimated a total number of only 150 lakes below the tracks, which is far below the several thousands of water bodies found in the region by Pi et al. (2022). Moreover, the inter-track distance of other altimetry missions such as Sentinel-6 is larger than that of Sentinel-3. This emphasizes the limited spatial coverage of the radar altimeters.

Multi-beams lidar altimetry data from ICESat-2 and GEDI missions allows bypassing the limitations mentioned above by providing open-access surface elevation data with enhanced spatial coverage compared to that of radar altimetry missions. Indeed, Chen et al. (2022) showed for example that the ICESat-2 ATL13 product allowed observing 2 to 7 times more global water bodies than what the traditional altimetry missions can do. The ATL13 product being spatially limited by a shape mask derived from existing inland water bodies databases (Jasinski et al., 2023), it is likely that the ATL08 product used in our study allows for an even better spatial coverage.

### 4.3.3 Combination of methods based on open-access data

We showed that combining the methods based on non-commercial data gave results comparable to that obtained with the Profile ICESat-2/contours method alone, so the benefit in terms of accuracy is not substantial. However, combining different methods mitigates some of the limitations of each method and provides more robust curves. The temporal coverage (sub-monthly revisit time) of radar altimetry data and the spatial coverage of lidar data improve the height-area curves extent and the number of water bodies observed, respectively. Thus, the combination of radar and lidar altimetry data provides an open source solution for upsampling volume dynamics analysis to a wider range of lakes, as the methods are easily transferable to other lakes. This could be of particular interest for the monitoring of ungauged lakes or lakes with outdated in-situ data.
5 Conclusion

The height-area relationships of sixteen lakes and reservoirs in West Africa have been derived from four different methods. These methods used different data sources such as Pleiades DSMs, Sentinel-2 optical imagery, ICESat-2 and GEDI lidar altimetry and Sentinel-3 radar altimetry. We found a generally good agreement with in-situ data (most height RMSE values below 0.30m and volume NRMSE values below 11%) and among the methods. With the exception of the Sentinel-3-based method which tends to produce higher dispersions, all methods provide curves with very low noise (fit RMSD values below 0.10m for most lakes). Fine shape patterns were consistently observed over small height amplitudes, highlighting the ability of the different methods to monitor shallow lakes with non-linear bathymetric behaviors. We found satisfactory water elevation precisions, with values close to 0.20m using Pleiades DSMs and slightly better values of the order of 0.13m or less using the other methods. We identified inherent limitations in terms of data quality, surface features, spatio-temporal coverage and data accessibility. This analysis suggests that lidar-based methods combined with radar altimetry data show similar performance to high-resolution DSMs-based methods and therefore have great potential for estimating water volume changes over lakes and reservoirs in this region. Furthermore, benefiting from its wide-swath Ka-band radar interferometer (KaRIN), the Surface Water and Ocean Topography (SWOT) mission, launched on December 16, 2022, will be able to observe 90% of the inland areas and all lakes larger than 250 x 250m² (requirements) located between 78°N and 78°S (Biancamaria et al., 2016). With a minimum revisit time of 21 days, SWOT will thus provide volume change estimates for the majority of the lakes and reservoirs in the study area, further expanding the number of water bodies that could be addressed by remote sensing. The H-A-V relationships derived in this study will provide a valuable database to assess SWOT performances in this area.

Open Research Section

Data Availability

The in-situ water surface elevation data on Bangou Kirey and Agoufou lakes are available in the AMMA-CATCH observatory database (www.amma-catch.org, DOI: https://doi.org/10.2136/vzj2018.03.0062). For the height-volume relationships of Bam, Seguenega and Sceytenga reservoir, please contact the Institut International d’Ingénierie de l’Eau et de l’Environnement (2IE, ousmane.yonaba@2ie-edu.org, tazen.fowe@2ie-edu.org). The height-area relationships of the Kokorou lake and Toussiana reservoir have been extracted respectively from Baba et al. (2019) and Sanogo and Dezetter (1997).

The Sentinel-2 L2A Surface Reflectance (SR) images are available on Google Earth Engine (GEE, (Gorelick et al., 2017)) as the “Sentinel-2 MSI: MultiSpectral Instrument, Level-2A” collection (https://developers.google.com/earth-engine/datasets/catalog/COPERNICUS_S2_SR). The Sentinel-3 Sar Radar Altimeter (SRAL) data and the Altimetric Time Series Software (AlTiS, (Frappart et al., 2021)) are provided by the Centre de Topographie des Océans et de l’Hydrosphère (CTOH, https://www.legos.omp.eu/ctoh/catalogue/). The Ice, Cloud and land Elevation Satellite-2 (ICESat-2) L3A Land and Vegetation height data product (ATL08) is accessible on the National Snow and Ice Data Center (NSIDC) website (https://nsidc.org/data/atl08/versions/6). The Global Dynamics Ecosystem Investigation (GEDI) L2A Geolocated Elevation and Height Metrics (GEDI02_A) are downloaded from the NASA Land Processes Distributed Active Archive Center (LP DAAC, https://lpdaac.usgs.gov/products/gedi02_av002/).

The dataset containing the height-area-volume relationships of the remote sensing-based methods is provided as a CSV file accessible through https://dataverse.ird.fr/privateurl.xhtml?token=ac61adc6-254a-4ccc-9061-7a6d1bd21612. The dataset also includes the in-situ data-based height-area-volume relationship of the Arzuma reservoir. In
order to allow a direct comparison, the provided relationships are all unbiased with respect to the DSM Pleiades method.

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Comparison of methods to derive the height-area relationship of shallow lakes in West Africa using remote sensing

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**Key Points:**

- Four different remote sensing methods to derive volume changes of small and medium-sized shallow lakes have been intercompared.
- All methods, based on radar and lidar altimetry, Sentinel-2 water areas, and Pleiades Digital Surface Models, show good performances.
- Pros and cons of each method are identified and discussed.

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Abstract

In West Africa, lakes and reservoirs play a vital role as they are critical resources for drinking water, livestock, irrigation and fisheries. Given the scarcity of in-situ data, satellite remote sensing is an important tool for monitoring lake volume changes in this region. Several methods have been developed to do this using water height and area relationships, but few publications have compared their performance over small and medium-sized lakes. In this work we compare four methods based on recent data from the Pleiades, Sentinel-2 and -3, ICESat-2 and GEDI missions over 16 lakes in the Central Sahel, ranging in area from 0.22 km$^2$ to 21 km$^2$. All methods show consistent results and are generally in good agreement with in-situ data (height RMSE and volume NRMSE mostly below 0.30m and 11% respectively). The obtained height-area relationships show very little noise (fit RMSD mostly below 0.10m), except for the Sentinel-3-based method which tends to produce higher dispersion. The precision of the estimated water height is about 0.20m for Pleiades Digital Surface Models (DSMs) and less than 0.13m for the other methods. In addition, fine shape patterns are consistently observed over small height amplitudes, highlighting the ability to monitor shallow lakes with non-linear bathymetric behavior. Inherent limitations such as DSM quality, temporal coverage of DSM and lidar data, and spatial coverage of radar altimetry data are identified. Finally, we show that the combination of lidar and radar altimetry-based methods has great potential for estimating water volume changes in this region.

1 Introduction

Lakes store 87% of surface liquid freshwater on Earth (Gleick, 1993). Even though the main freshwater stocks are located in glaciers and underground (Oki & Kanae, 2006), lakes are a crucial component of the water cycle as they provide a readily accessible water resource. Their number is dominated by abundant small water bodies and ponds (Biggs et al., 2017) whereas medium-sized and large lakes (size > 1km$^2$) represent 85% of the global lake area (Pi et al., 2022). Lakes and reservoirs provide crucial services for humans (Reynaud & Lanzanova, 2017) and ecosystems (Schallenberg et al., 2013) such as freshwater and food supply, electricity, nutrients processing, natural habitats and recreational services. The capability of lakes to ensure these services inherently depends on their water storage.

Monitoring lake volume change is essential as several recent studies highlighted significant variations over the past decades. For instance, Wurtsbaugh et al. (2017) demonstrated that many of the world’s saline lakes are shrinking at an important rate. Yao et al. (2023) identified a decline of lake water volume over 53% of the 1972 largest global lakes, with the majority of the loss attributable to direct human activities and climate change. Even though lake desiccation trends are widespread, the Yao et al. study, consistently with Luo et al. (2022) and (Wang et al., 2018), also revealed regional patterns with net water volume gains in areas such as the Inner Tibetan Plateau and the Northern Great Plains of North America.

The hydrological functioning of water bodies in West Africa is poorly known at the large scale (Papa et al., 2023). Yet areas such as Central Sahel host a multitude of water bodies, ranging from reservoirs (Cecchi et al., 2009), small lakes and ponds (Gardelle et al., 2010; Grippa et al., 2019) and temporary water bodies (Haas et al., 2009), which are widespread but still relatively unknown in number. Being used for drinking water, livestock watering, irrigation and fishing, these water bodies play a vital role in such an area subject to a long dry season (Cecchi et al., 2009; Frenken, 2005). Despite the severe drought that impacted Central Sahel in the 1970s and 1980s, several studies have highlighted a paradoxical increase in the surface area of lakes and ponds (Baba et al., 2019; Gal et al., 2016; Gardelle et al., 2010), as well as an increase in runoff and river discharges (Descroix et al., 2018; Favreau et al., 2009; Mahe et al., 2010). Attempts to study the evolution of water volumes in West Africa have been carried out either at the scale of a few lakes (Fowe et al., 2015; Gal et al.,
2016; Pham-Duc et al., 2020), or at a larger scale but punctually in time (Annor et al., 2009; Cecchi et al., 2009; Liebe et al., 2005). In addition, West African lakes and reservoirs have been included in global studies, but these are brief in time (Cooley et al., 2021) or cover only a few large lakes (Luo et al., 2022; Yao et al., 2023). In this regard, efforts remain to be done for both long-term and large-scale monitoring of the lake volume changes in this region.

Historically, in-situ sensors are used to measure the evolution of lake water level and volume. However, the limited spatial coverage and the global decline of in-situ operations and installations (Papa et al., 2023; Riggs et al., 2023; Schwatke et al., 2015) challenge the capability to have long and large-scale time series. With periodic observations and a considerably increased spatial coverage, satellites are a relevant tool for assessing lake water volume trends globally.

Remote sensing allows measuring physical parameters of water bodies such as water surface height and area. Water surface height is derived from the return time estimation of electromagnetic waves emitted by nadir-looking radar or laser altimeters. Synthetic Aperture Radar (SAR) altimeters such as those on board Sentinel-3 and Sentinel-6 are able to measure the elevation of water bodies of a few hectares with a sub-monthly revisit time (Normandin et al., 2018; Taburet et al., 2020). However, these measurements still suffer from coarse across-track resolutions which may lead to contamination by bright surfaces located in the radar footprint (Boy et al., 2022). In addition, the nadir-viewing and the inter-track distance of several tens of kilometers of the conventional radar altimeters restrict their spatial coverage. The Ice, Cloud and land Elevation Satellite-2 (ICESat-2) and the Global Dynamics Ecosystem Investigation (GEDI) missions carry on board multi-beams laser altimeters enabling along-track surface elevation posting rate from tens of centimeters to tens of meters (Neuenschwander et al., 2023), (Dubayah et al., 2020). Nonetheless, these measurements remain discrete and their temporal coverage is limited by the multi-month revisit time of the satellites and some degraded acquisition periods for GEDI (Urbazaev et al., 2022).

The estimation of the water extent from optical or radar imagery observations is based on the separation of the spectral or backscattering signature of water from that of the soil (Pekel et al., 2016; Yao et al., 2019). With a revisit time of 5 days and a spatial resolution of up to 10m, the Sentinel-2 optical sensors can be used to monitor water surface area variations of a large number of lakes and reservoirs (Reis et al., 2021; Schwatke et al., 2019; Yang et al., 2017). Cloud cover, which is usually one of the main obstacles to optical observation of water bodies, is not a major problem in West Africa since the dry season lasts between 6 and 9 months (Nicholson, 2018).

Water surface height and area can be combined to calculate volume changes between consecutive observations. This is usually done by assuming that the observed portion of the lake behaves like a cone or pyramid frustum (Crétaux et al., 2016; Luo et al., 2022; Terekhov et al., 2020), or by multiplying the water level change by the average surface area between the two dates (Gao et al., 2012; Li et al., 2020; Song et al., 2013). These two solutions require simultaneous observations of water surface height and area and are based on geometric approximations whose accuracy decreases as the water level change increases. A third way consists of using the height-area relationship (Abileah et al., 2011), which synthesizes the lake’s bathymetry information into a relationship that describes changes in surface area as a function of water level. Once the height-area relationship has been constructed, volume change can be calculated by integration (Carabajal & Boy, 2021; Duan & Bastiaanssen, 2013; Magome et al., 2003) and using only one of the two variables.

The construction of the height-area relationship requires computing the height and extent of the lake banks contour lines (isobaths). With remote sensing data, isobaths are typically calculated by combining near-simultaneous (within a few days) observations of water surface height and area from radar or lidar altimetry data and imagery respectively.
(Abileah et al., 2011; Busker et al., 2019; Gao et al., 2012; Schwatke et al., 2020). Bank
topography data such as global Digital Elevation Models (DEM) generated before impound-
ment or at low water levels have been combined with satellite images to retrieve the water
surface elevation of lakes that cannot be observed by altimeters (Avissé et al., 2017; Bhagwat
et al., 2019; Terekhov et al., 2020; Tseng et al., 2016). In addition, height-area relationships
can also be generated through the analysis of a DEM alone. This method enabled studying
the volume changes of many medium-sized and large lakes worldwide (Fang et al., 2019;
Pan et al., 2013; Yao et al., 2018; S. Zhang & Gao, 2020). Publications such as Arsen et al.
(2013); Bacalhau et al. (2022); Ma et al. (2019); N. Xu et al. (2020) have taken advantage of
the high spatial resolution and vertical accuracy of lidar altimetry data to determine not the
elevation of the water surface but that of the banks. Unlike DEMs, this bank topography
data is discrete but, once intersected with water contours derived by satellite imagery, has
shown great potential for bathymetry retrieval above the lowest observed water level.

In terms of intercomparison of methods, Magome et al. (2003) estimated volume change
of Lake Volta in Ghana by comparing different methods using altimetry (TOPEX/ Poseidon)
and optical imagery (Moderate-Resolution Imaging Spectroradiometer, MODIS) or their
combination with a DEM. They obtained better results when combining altimetry and
DEM and highlighted the greater spatial coverage of the method using the combination of
imagery and DEM. Zolá and Bengtsson (2007) also compared several methods over lake
Poopó in Bolivia using echo-sounding measurements, combination of Landsat-5 with in situ
water heights, and water balance calculations. They found consistent results and good com-
plementarity between the different methods. Apart from these publications, both focusing
on large lakes (> 100 km$^2$), few studies have attempted to intercompare different methods
to provide height-area relationships, on smaller lakes and with recent data. The aim of this
work is to intercompare four different methods based on recent data (Pleiades, Sentinel-2,
Sentinel-3, ICESat-2, GEDI) over 16 small (< 1 km$^2$) and medium-sized (1-100 km$^2$) lakes
located in Central Sahel. The results of each method are evaluated using criteria of ac-
curacy, precision, sensitivity to surface characteristics and spatio-temporal coverage. The
study area, data and methods are described in Section 2 and the comparison results are
presented in Section 3 and further discussed in Section 4.

2 Material and methods

2.1 Study area and in-situ data

The study area is mainly located in Central Sahel, between the 10.8°N and 15.5°N
latitudes and extends over Mali, Niger and Burkina Faso (BF). From North to South, the
climate is semi-arid and dry sub-humid. Rainfall is driven by a tropical monsoon system and
follows a latitudinal gradient with mean annual precipitation ranging, from the North to the
South, from 200 mm yr$^{-1}$ to 1000 mm yr$^{-1}$. Rainfall is concentrated during the wet season
stretching from June to October. The rest of the year gives way to a long dry season with
a very little cloud cover, which is suited for observing water bodies using optical imagery.

Sixteen lakes have been selected according to the in-situ and remote sensing data avail-
ability or to existing knowledge and documentation (Figure 1 and Table S1). They are
spread along the climatic gradient and include three lakes in Mali, two in Niger and eleven
in Burkina Faso.

Ten of these water bodies are reservoirs and others are natural lakes. Their mean
altitude varies between 200 and 500 m above mean sea level, their mean water surface area
ranges from 0.22 km$^2$ (Bangou Kirey) to 21 km$^2$ (Kokorou), and most of them are relatively
shallow (a few meters deep). These lakes show different optical water types with varied
levels of turbidity, from moderately turbid (Robert et al. 2016) to very turbid (e.g. lake
Bangou Kirey, (Touré et al., 2016), and some of them harbor temporary or permanent
aquatic vegetation (Gardelle et al., 2010; Baba et al., 2019).
in-situ data are of different nature and come from different sources. Water surface height data are measured continuously, every 30 minutes, through pressure transducers on the Bangou Kirey lake and the Arzuma reservoir, respectively since July 2022 and March 2023. Additional water surface height measurements have been collected on the Agoufou lake by AMMA-CATCH observatory (Galle et al., 2018) between 2015 and 2019 with a weekly or monthly frequency. Height-volume (H-V) relationships of the Burkinabe reservoirs of Bam, Seguenega and Seytenga have been provided by the Direction Générale des Ressources en Eau (DGRE) in Burkina Faso and come from topographic survey performed before the dams impoundment. Finally, the height-area (H-A) and height-volume-area (H-V-A) relationships of the Kokorou lake and the Toussiana reservoir are extracted respectively from the digitization of Baba et al. (2019) and from Sanogo and Dezetter (1997).

2.2 Satellite data, water surface area and height extraction

2.2.1 Water surface areas and contours from Sentinel-2 optical images

Sentinel-2A and -2B acquire high-resolution multispectral images with a revisit time of approximately 5 days (Table 1). The MultiSpectral Instrument (MSI) onboard Sentinel-2 has 13 spectral bands from blue to Short-Wave InfraRed (SWIR), with spatial resolution from 10m to 60m on the ground. For this study, we use the green and SWIR bands which have resolutions of 10m and 20m. Images are L2A Surface Reflectance (SR) products corrected from atmospheric effects with Sen2Corr processing. Images are downloaded through Google Earth Engine (GEE, (Gorelick et al., 2017)) as the "COPERNICUS/S2_SR" collection, over December 2018 to December 2022. All bands are downscaled to a pixel size of 20m x 20m and images with a percentage of cloudy pixels greater than 5% are discarded. The residual cloudy pixels are masked using the QA cloud and cirrus bitmasks, and an empirical threshold of 0.2 on the blue reflectance. After these steps, a few remaining images (usually
To compute water surface area, we mask water pixels by applying a threshold on the MNDWI (H. Xu, 2006), which is a spectral index commonly used to detect water on optical images, based on the normalized difference between the green (B3) and the short-wave infrared (B12) bands.

\[
MNDWI = \frac{\text{green} - \text{SWIR}}{\text{green} + \text{SWIR}}
\]

First, we clip the images to the close surroundings of the water body to exclude close but unconnected water bodies. Then, the MNDWI is computed and the threshold, constant in time, is determined ad hoc for each lake following De Fleury et al. (2023) and Reis et al. (2021). Reis et al. (2021) have shown that water detection is usually accurate for a full range of MNDWI thresholds rather than a well-defined value. The water surface area is finally calculated by counting the number of pixels above the threshold and multiplying by the pixel area. The water contour is delineated using the marching squares algorithm, a 2D adaptation of the marching cubes algorithm (Lorensen & Cline, 1987) which is implemented in the “find contours” function from the Scikit-image Python package. This function takes as input the MNDWI pixels raster and the threshold value and generates iso-value contours at a sub-pixel scale by linearly interpolating the MNDWI pixel values. If the lake separates into several parts as it dries up, we keep only the largest part. For each lake, a time series of water surface areas and water contours is eventually generated.

### 2.2.2 Pleiades Digital Surface Model

Pleiades-1A and -1B Pleiades are two satellites equipped with a very high-resolution optical sensor acquiring panchromatic images (480-830nm) with a pixel size of 0.50m (Table 1 and Figure 3). We ordered the acquisition of pairs of cloud-free Pleiades panchromatic stereo-images (Pleiades ©CNES 2021, 2022, 2023, Distribution Airbus DS) over each lake, with a B/H ratio between 0.35 and 0.8. Pleiades images allow the creation of Digital Surface Models (DSM) by photogrammetric processing through the computation of matching pixels displacement between two stereo-images. DSMs were processed using the Digital Surface Model from OPTical stereoscopic very-high resolution imagery (DSM-OPT) online service, based on the MicMac tool (Rupnik et al., 2017) and operated by the Solid Earth ForM@Ter pole of the research infrastructure DATA TERRA. DSM-OPT also provides an ortho-image which is a panchromatic image georeferenced identically to the DSM.

Since DSM estimation by photogrammetry is challenging over the water surface due to low pixel correlation, we ordered Pleiades images at the end of the dry season, when water surface level is minimum, which allows exploring the maximum bank extent. We generated DSMs at 1m x 1m horizontal resolution, in line with Bagnardi et al. (2016). As the semi-arid landscapes of the study area often show small surface roughness (compared to mountainous or forest landscapes for instance), we adapted the correlation window size to 9 x 9 pixels and we used 0.2 as the minimum correlation coefficient for matching (Bagnardi et al., 2016). Due to the large extent of the Bam reservoir, two stereo-pairs acquisitions are needed to observe the northern and southern part of the reservoir. To end up with a single DSM, we generated a DSM for each part and we merged them after applying the Nuth and Kääb method (Nuth & Kääb, 2011) to ensure co-registration. However, a residual elevation bias between the two parts has been observed after co-registration. We corrected it by comparing the DSM of each part with terrain ICESat-2 data and subtracting the respective mean difference.

Some Pleiades DSMs showed along-track undulations which were highlighted when computing the difference with the GLO-30 Copernicus DEM (European Space Agency, 2021). For instance, we observed along-track undulations of several meters in Pleiades-1B-derived DSM of the Bangou Kirey and Kokorou lakes. These undulations have been noticed on many DEMs from several space-borne missions (Hugonnet et al., 2022) and are caused
by errors in the image geometry estimation due to sensor motion (jitter). Our method to correct for these undulations is partly based on Girod et al. (2017). We compute the average per line of the DEM difference with GLO-30 (Figure 2) and subtract it to the Pleiades DSM.

2.2.3 Bank elevation profile from ICESat-2 lidar altimeter data

The Ice, Cloud and land Elevation Satellite-2 (ICESat-2) was launched in September 2018 (Table 1 and Figure 3) by NASA (Markus et al., 2017). The Advanced Topographic Laser Altimeter System (ATLAS) onboard ICESat-2 is a photon-counting lidar with 3 pairs of laser beams emitting pulses at 10 kHz and separated by 3.3 km in the cross-track direction. The footprint size of each beam has a 14 m diameter. Each pair is composed of a strong beam and a weak beam (energy ratio of 4:1) with a wavelength of 532 nm and located 90 m from each other.

The ATL08 version 6 product is dedicated to land and vegetation and contains along-track heights above the WGS84 ellipsoid for the ground and canopy surfaces (Neuenschwander et al., 2023). We downloaded all ATL08 data over the October 2018 (first data available) - June 2023 period. The nominal posting rate is theoretically 100 m but data gaps can occur due to low signal-to-noise ratio or acquisition errors. For the mid-point of each 100 m segment, ATL08 provides three height metrics, respectively the mean, the median and the best-fit terrain height. The latter is the height resulting from the polynomial which best fits the 100 m terrain profile, among 1st, 3rd and 4th order polynomials. Since the topography of the banks is likely to vary inhomogeneously over 100 m, and as suggested by Tian and Shan (2021), we use the best-fit height in this study. Liu et al. (2021) assessed ICESat-2 ATL08 terrain height data accuracy against airborne lidar products over 40 sites located in the U.S. mainland, Alaska, and Hawaii. They showed that quite similar performances were obtained independently of beam energy, whereas strong beams should theoretically be more accurate because of their better signal-to-noise ratio. They also found nighttime terrain accuracy slightly better than daytime. However, daytime data represent a non-negligible proportion

![Figure 2. Difference between Pleiades DSM and GLO-30 DEM over Kokorou lake.](image)
of the ATL08 data quantity and consequently condition the spatial coverage. Hence, we
decided not to filter ATL08 data on the beam energy and acquisition time criteria.

Moreover, the number of terrain photons detected within a segment is important to fit
the 100 m height profile and derive a robust estimation of the segment height. Hence, we set
a threshold of 10 on the minimum detected number of terrain photons, in line with the results
of Urbazaev et al. (2022). To remove large outliers, we keep data with a photon heights STD
inferior to 1 m and discard data whose best fit height is inferior to the minimum detected
photon height, this being probably due to a fitting error. Finally, given that ICESat-2 beams
were purposely mispointing during the first height cycles of the mission, that is during the
two first years (nominal cycle of 91 days), certain lakes have irregular or limited temporal
coverage.

2.2.4 Bank elevation profile from GEDI lidar altimeter data

The Global Ecosystem Dynamics Investigation mission on board the International Space
Station started in December 2018 (Dubayah et al., 2020). It consists of a full-waveform lidar
with 3 lasers producing a total of 8 beam ground transects spaced 600 m apart in the cross-
track direction. Each ground transect has a footprint size of 30 m and samples the Earth’s
surface approximately every 60 m along-track (Table 1 and Figure 3). GEDI L2A version
2 data product, distributed by NASA’s Land Processes Distributed Active Archive Center
(LP DAAC), provides ground elevation, canopy top height and relative height metrics. The
ground elevation is represented by the lowest mode elevation which gives the height of the
last significant energy return detected in the waveform.

We removed large outliers by rejecting data whose elevation absolute difference with
the digital_elevation_model_srtm value, a parameter in the product representing the Shuttle
Radar Topography Mission (SRTM) elevation at GEDI footprint location, was greater than
100 m. We also discarded data with a non-zero degrade_flag value, meaning that the lidar
shot occurred during a non-degraded period. As for ICESat-2 ATL08 data and following
the suggestions of Liu et al. (2021) who assessed GEDI L2A terrain height data accuracy
as well, we considered unnecessary to discard GEDI data on the basis of beam energy and
acquisition time.

2.2.5 Water surface heights from Sentinel-3 radar altimetry data

The Sentinel-3 (S3) mission includes the Sentinel-3A and 3B satellites carrying on
board the Synthetic Aperture Radar Altimeter (SRAL), a delay/Doppler altimeter (Table
1 and Figure 3). The altimeter operates in global mode with an along-track posting rate
of approximately 300m and an across-track resolution of several kilometers. Water surface
height measurements of the same target are provided every 27 days. Water surface height
data have been retrieved from the radar waveforms recorded by Sentinel-3 with the Offset
Centre of Gravity (OCOG) retracking algorithm and have been provided by the Centre de
Topographie des Océans et de l’Hydrosphère (CTOH). They have been processed using the
Altimetric Time Series Software (AlTiS version 2.0, (Frappart et al., 2021)). The data were
first selected within a polygon fitted to the lake maximum water extent derived from the
corresponding water contour time series. Then, they were filtered with a threshold of 40dB
on the backscattering coefficient for data acquired before January 2020, and a threshold of
20dB for data acquired after January 2020 (De Fleury et al., 2023). These thresholds are
in line with what is suggested by Taburet et al. (2020) and Kittel et al. (2021). Besides,
multi-peak waveforms or dry-lake data were rejected with an empirical threshold of 20 on the
waveform peakiness. The resulting water surface height is computed as the median of the
remaining height values. Water surface heights with a Median Absolute Deviation (MAD)
along the transect greater than 1m are rejected. For each lake, a water surface height time
series was eventually generated.
Figure 3. Data available over the Arzuma reservoir. Gray level background is the Pleiades DSM with the corresponding water mask in blue. Pressure transducer is represented by a black triangle. ICESat-2, unused and used GEDI data are respectively represented by green diamonds, yellow and red stars. Sentinel-3 theoretical ground track is represented by magenta crosses. Full, dashed and dotted black lines represent 3 selected water contours computed from Sentinel-2 images.
Table 1. Remote sensing data and corresponding mission used in this study.

<table>
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<tr>
<th>Mission</th>
<th>S2</th>
<th>S3</th>
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<th>GEDI</th>
<th>Pleiades</th>
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<td>Sentinel-3</td>
<td>Ice, Cloud and Land Elevation Satellite-2</td>
<td>Global Ecosystem Dynamics Investigation</td>
<td>Pleiades</td>
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<td>Dec 2018</td>
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<td>L2 OCOG</td>
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2.3 Methods to derive height-area relationships

2.3.1 DEM filling

This method uses an incremental approach to count DEM pixels whose elevation is between two given altitudes, and repeats the operation over a set of elevation increments until filling the entirety of the banks of the water body. Taking advantage of the DSM Pleiades vertical resolution, the incremental step between two successive elevations of the processing is empirically set to 0.1m. For each elevation increment, the corresponding pixel number is converted to an area by multiplying by the pixel area, and forms an elevation-area pair. All the elevation-area pairs form the H-A curve. Moreover, since the processing stops at an altitude defined manually, it is possible that, at a certain point, the computed water areas exceed the physical reality of the lake dynamics over the study period. The upper limit of the H-A relationship is therefore set to the maximum Sentinel-2-observed water area. For the following, this method will be referred to as the ”DSM Pleiades“ and is graphically represented in Figure 4a.

A Pleiades DSM footprint is at least 100km². We first limit the processed area to the region of interest by clipping the DSM to a polygon representing the close surroundings of the water body. Water surfaces generate “No Data” values or extreme outliers on the DSM due to low pixel correlations during the stereo-matching processing, and have to be filtered out. Hence, we mask water pixels on the orthoimage. Since orthoimage reflectance values generally follow a bi-modal distribution, we separate water from soil by defining a global threshold on the reflectance pixels. Finally, we mitigate the remaining minimal classification errors by filling the holes with a morphological closure using a square structuring element of size 9x9.

Once water has been masked, we determine the altitude of the water surface as the median elevation of the water pixels located along the contour. This contour is computed as the external morphological gradient using a cross structuring element of size 1. In addition, contamination by outliers is mitigated using the MADe method (Kannan et al., 2015).
2.3.2 Intersecting a DEM with water contours

This method is similar to what Mason et al. (1995-12-01) mentions as the “waterline method”, and multiple studies such as Ragettli et al. (2021) already employed it to retrieve lake bathymetry. Assuming the water surface is flat, isobaths can be computed as the intersection of water contours with a DEM. The water contours elevation is computed as the median value of the intersected DEM pixels elevations, consecutively to an outliers removal process based on the MADe method. Furthermore, we consider that the water contour must intersect a minimum number of DEM pixels, empirically set as 20. Finally, the lower limit of the H-A relationship is set to the minimum Pleiades-observed water area. For the application of this method on Pleiades DSMs, we will use the term ”DSM Pleiades/contours” (Figure 4b).

Since the Pleiades DSM are surface models, they provide elevation of the highest observed point on the ground. Thus, they are impacted by relief like buildings and, particularly for the studied lakes, trees and riparian vegetation. To mitigate this impact, we mask out the obvious wooded parts of the Pleiades DSMs. This is the case for the right banks of the Bangou Kirey lake. The Inbanta lake is densely covered in trees and if all of them were masked the remaining area would be too small to compute the H-A curve. Therefore, for this lake we do not mask out any area. The resulting impact of vegetation will be discussed later.

2.3.3 Intersecting bank elevation profile with water contours

Instead of using a whole DEM providing continuous information of the ground elevation, this method requires one or multiple discrete elevation profiles of the banks of the water body. Here, we use elevation profiles either from ICESat-2 or GEDI lidar topography measurements. This method will be referred to as the “Profile ICESat-2/contours” or “Profile GEDI/contours” method (Figure 4c). As with the DSM-based methods, the water level at the dates the elevation profiles were recorded determines the extent of the bank bathymetry that can be characterized. Isobaths are retrieved by calculating the intersections between the water contours and the banks elevation profile. For this purpose, the profiles are converted to geometric lines and we compute the crossover points with the water contour polygons. The crossover points elevation is linearly interpolated between the two measurement points. It is important to check that the pair of measurement points was acquired over the ground and not over water, and that they are located on the same bank, otherwise the resulting interpolated elevation will be erroneous. To do this, we mask out the measurement points acquired over water using the closest Sentinel-2 image in time.

We empirically set a maximal threshold of 2% on the bank slope to reject crossover points located at places too steep with respect to lidar data posting rate. Then, because it is more robust than the mean, the median value of the crossover points elevations is retained for the water contour elevation, following Arsen et al. (2013). Finally, we filter out water contours whose elevation is computed from only one crossover point, as it may reflect erroneous intersections due to small water contour detection errors. Given the multiplicity of the laser beams or the shape of some contours, we frequently have more than two crossover points per contour.

We observe large biases (tens of centimeters to tens of meters) between GEDI data from different dates of acquisition. For simplicity, we only select for each lake the acquisition date giving the most complete H-A curve. Most of the time, it results in selecting the latest acquisition date of the dry season.

2.3.4 Matching water surface height with water surface area measurements

This method uses water surface height data and combines them with synchronous water surface area observations. To construct the height-area relationship, we search for the
Sentinel-2 images co-dated with the Sentinel-3 data and match the height and area measurements with a temporal tolerance of 3 days. A tolerance of 3 days is appropriate given the temporal variability of the lakes studied (De Fleury et al., 2023), and provides a good trade-off with respect to data availability. If the time difference between Sentinel-2 and Sentinel-3 acquisitions is not zero, we linearly interpolate successive water area data to the water surface height date. This method will be referred to as the "Height S3/area" method (Figure 4d).

2.4 Processing the height-area relationships

2.4.1 Processing the height-area relationships of in-situ data

For three reservoirs (Bam, Seytenga and Seguenega), in-situ data provided as H-V relationships have been converted to H-A relationships, computing the areas as the derivative of the volume with respect to the height $A = dV/dH$ (Gao et al., 2012). For three lakes (Agoufou, Arzuma and Bangou Kirey), water surface height in-situ measurements are combined with Sentinel-2 water surface areas acquired on the same day. For Agoufou, since height data are acquired at a weekly frequency, Sentinel-2 areas are interpolated between two consecutive dates to match the in-situ data.

2.4.2 Resolving the bias between elevation data

As we do not have absolute elevation data for all methods, the comparison of the height-area relationships requires prior elevation bias removal. Indeed, the in-situ data and part of the Pleiades DSMs are not absolutely leveled, GEDI data showed acquisition time-dependent biases and the other remote sensing data have different references. The elevation biases are removed directly on the height-area curves. The DSM Pleiades/contours height-area method is taken as reference because it provides long and regular datasets, and the bias with the other methods is computed as the mean of the height differences:

$$bias = mean(h_{method} - h_{Pleiades})$$
2.4.3 Combining the height-area relationships based on open source data

The capabilities of the height-area relationships derived from methods based on open source data only have been also assessed. This concerns Profile ICESat-2/contours, Profile GEDI/contours and Height S3/area methods based on Sentinel-2 ICESat-2, GEDI and Sentinel-3 data.

For each lake, we fit the H-A relationship of the three methods combined with the best polynomial function of degree lower or equal to 2. Then, we discard the data outside the fit 95% confidence interval in order to remove the outliers. For the following, this method will be referred to as the “Combined open source” method.

2.5 Processing the volume-area relationships

For each height-area dataset associated with a specific lake and method, water volume changes are computed as the integral of the corresponding height-area function between two consecutive heights (Yao et al., 2023; Abileah et al., 2011). To do this, the H-A relationship is fitted and then integrated over H. A polynomial function (maximum degree of 5) is used for the fit and the Akaike Information Criterion (citeAkaike1973 is used to select the best fit and avoid overfitting. The volume-area relationship is finally given by cumulating volume changes. Since the height of the lake bottom is not always known, the reference is set to the “in-situ” data and all other methods are truncated to the minimum in-situ volume. Volumes from the different methods are then computed as relative volumes given by \( V_{\text{method}} - V_{\text{insitu}} \). Moreover, since the different datasets do not start at the same water area, a dataset-specific volume offset called \( V_{0, \text{method}} \) has to be resolved. The offset is computed as the mean difference with the in-situ dataset.

2.6 Methodology for the performance assessment of the different methods

Different metrics are used to assess the precision and accuracy of the different methods:

- Median Absolute Deviation
  \[
  \text{MAD} = \text{median}(|y_i - \text{median}(y)|)
  \]

- Coefficient of determination
  \[
  R^2 = 1 - \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y})^2}
  \]

- Root Mean Squared Difference
  \[
  
  \]

- Normalized Root Mean Squared Difference
  \[
  NRMSD = \frac{\text{RMSD}}{y_{\text{max}} - y_{\text{min}}}
  \]

- Root Mean Squared Error
  \[
  \text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=0}^{n-1} (y_i - y_{\text{insitu}})^2}
  \]

- Normalized Root Mean Squared Error
  \[
  NRMSE = \frac{\text{RMSE}}{y_{\text{insitu}, \max} - y_{\text{insitu}, \min}}
  \]
where \( n \) is the number of observations, \( y_i \) the value observed by remote sensing, \( y_{\text{insitu}} \) the value observed in-situ, \( \hat{y}_i \) the predicted value and \( \bar{y}_i \) the mean value.

To assess the precision of the water heights retrieved by the different sources of elevation data, i.e. how flat these elevation data sources observe the water surface, we use the MAD because it is more robust to outliers than the standard deviation. The MAD is computed along the water transect for Sentinel-3 data and along the water contours estimated by Sentinel-2 for methods using Pleiades, ICESat-2 and GEDI data. For the last three methods, the dispersion estimate also includes water contour detection uncertainty and therefore does not allow a strict assessment of the precision of the water level data alone.

We provide information on the H-A curves dispersion using the \( R^2 \), height RMSD and height NRMSD of the A-H polynomial fits. The Normalized RMSD (NRMSD) is the RMSD divided by the amplitude of the height observations (\( y_{\text{max}} - y_{\text{min}} \)).

For the accuracy assessment of the heights and volumes, \( R^2 \), RMSE and NRMSE are used. Since lakes can have very different volumes, NRMSE provides a more comprehensive information compared to RMSE. In-situ H-A and A-V curves are interpolated to obtain height and volume matchups with data from the other methods.

3 Results

3.1 Height-area relationships

The height amplitude observed by the remote sensing-based methods is ranging from 1.5m (Agoufou, Bangui Mallam, Inbanta, Manga) to 4m (Arzuma, Toussiana), with most amplitudes below 3m (Figure 5). Fine shape patterns such as slope changes are well retrieved using the different methods and are in good agreement with in-situ data (e.g. Arzuma, Djigo, Kokorou, Tibin).

The methods relying on bank elevation data (Pleiades, ICESat-2 and GEDI) are dependent on the acquisition dates which limit the observable extent of the H-A curves. In the case of ICESat-2 data, the low number of data over the small lakes (Bangou Kirey, Manga, North Tanvi, South Tanvi) is also due to the fact that the laser beams only overpassed the lakes during the planned first two years of lidar mispointing. For Bangou Kirey, Pleiades, ICESat-2 and GEDI sensors overpassed the lake at a relatively high water level, not allowing exploring the full H-A curve. Conversely, simultaneous observations of in-situ water level and Sentinel-2-derived area are not available for the highest water levels, which occur for only a few days during the rainy season when cloud cover is a problem for optical imagery. Therefore, it remains difficult to compare in-situ and satellite estimates for this lake.

Complete drying of some lakes during the dry season increases the H-A curves extent but also introduces errors in the Pleiades DSM. Indeed the H-A relationships derived by the DSM Pleiades method show hockey cross patterns for Inbanta and North Tanvi. For these lakes which dried up, the water contour could not be used to estimate the starting altitude as described in Section 2.3.1, which has been set to 310m for Inbanta and 296m for North Tanvi. The presence of high noise in the DSM challenged other solutions to derive the starting altitude, such as for example using the minimum DSM elevation within the lake polygon. The location of the noisy DSM pixels is confirmed by areas of low pixel correlations corresponding to smooth surfaces such as, for instance, the lake bottom for North Tanvi (Figure 6). The noise leads to troughs several meters deep which force the starting altitude (lake bottom) to be underestimated. These pixels are filled progressively with small changes in lake area, which explains the observed hockey cross pattern. As soon as the lake is not completely dry, the average elevation computed over the smallest water area smoothes the noise and gives a correct minimum water elevation. For Inbanta, we also note a difference between the DSM Pleiades and the DSM Pleiades/contours curves reflected by overestimated water areas within the two first thirds of the DSM Pleiades curve. This
Figure 5. Height-area relationships derived from all the methods a) over the lakes with in-situ data and b) over the other lakes.
difference is also attributed to the DSM noise, the resulting troughs causing a substantial quantity of pixels to be prematurely filled.

3.2 Volume-area relationships

The V-A curves also denote a generally good agreement between the different methods (Figure 7). Some small slope differences observed on the H-A curves comparison are more evident on the volume-area curves (e.g. DSM Pleiades over Kokorou lake), which is partly due to error propagation in the calculations. The largest differences with respect to in-situ data are observed over Bam and Seytenga reservoirs, where all remote sensing methods agree well with each other and differ from in-situ data. Part of these discrepancies may be due to bank erosion and sedimentation (Cecchi et al., 2020), with sediment transfer from the lake edge mainly due to land use (Tully et al., 2015) and wave-induced bank erosion (Hilton, 1985). For example, Boena and Dapola (2001) documented the Bam reservoir silting and showed that the sediment deposits in the lake could be of substantial thickness.

3.3 Quantitative results

3.3.1 Dispersion of the area-height relationship

All methods provided good fit results with almost all $R^2$ above 0.80 and most values above 0.90 (Table 2). The DSM Pleiades method outperforms all the other methods with all RMSD values below 0.03m, except for two lakes (Inbanta and North Tanvi) where RMSD equals 0.21m and 0.15m, respectively. The DSM Pleiades/contours, Profile ICESat-2/ and Profile GEDI/contours methods show good and consistent results with all RMSD values below 0.14m, most being below 0.10m. The Height S3/area method tends to produce curves
Figure 7. Volume-area relationships derived from the different methods over the lakes with in-situ data.
with dispersion values almost systematically greater than those from other methods. RMSD is between 0.09m and 0.34m, with 4 lakes having RMSD above 0.20m. A small part of this dispersion is inherently related to the time interpolation required to match water surface height and area measurements.

### 3.3.2 Precision of water elevation

The median MAD obtained using the different sources of elevation data (Figure 8) are respectively between 0.11m and 0.70m with most values below 0.20m for Pleiades, between 0.04m and 0.19m with most values below 0.13m for ICESat-2, between 0.04m and 0.23m with most values below 0.13m for GEDI, and between 0.01m and 0.12m with most values below 0.06m for Sentinel-3. Therefore, all sources of elevation data provide good results.

The number of points per contour/transect used to compute the precision varies with the methods and highly depends on lake size and, especially for Sentinel-3, and on the satellite’s track attack angle with respect to the lake banks. The median number of points per contour ranges from 675 (Babou) to 4260 (Tibin) for Pleiades DSMs, from 2 (North Tanvi) to 50 (Bam) for ICESat-2, from 2 (Bangou Kirey) to 20 (Tibin) for GEDI (mainly because we selected only one acquisition date) and from 1 (Toussiana) to 12 (Bam) per transect for Sentinel-3.

The relatively low precision of Pleiades DSMs (> 0.40m) over certain lakes can be explained either by high amplitudes of noise due to very smooth areas or by flooded vegetation and trees. It is not surprising that the precision of Pleiades is poorer than other data sources, as we have chosen to generate the DSMs at a spatial resolution of 1m x 1m, which introduces more pixel-to-pixel noise than a coarser resolution. The average precision of 0.04m for Sentinel-3 must be taken carefully because for half of the lakes, the transects are made of a median number of 3 points or less. Except for these cases, all sources of data show a good precision stability with Inter-Quartile Ranges (IQR) < 0.20m.

### 3.3.3 Height-area and volume-area relationships accuracy

For all methods, the height RMSE is between 0.03m and 0.42m with most values below 0.30m and the height NRMSE is between 1.3% and 13.7% with most values below 8%. Some methods are missing for some lakes. They all perform well on the common lakes but not similarly from one lake to another. However, we do not observe systematic differences between one method and another. Heights derived from Sentinel-3 give higher RMSE and NRMSE on certain lakes. One of the reasons might be that radar altimeter waveforms are affected by crops or other water bodies surrounding the reservoir that generate relatively high backscattering (Arzuma). The other reason is the limitation of the radar altimeter along-track resolution. This can occur with small water bodies (noise observed for Babou and Manga lakes) or larger water bodies whose orientation with respect to the altimeter ground track generates narrow transects (Toussiana). Since these transects are made of very few measurements, they are more likely to provide larger errors.

For all methods, the volume RMSE is between 0.03Mm$^3$ and 8.72Mm$^3$ with most values below 5Mm$^3$ and the volume NRMSE is between 2.3% and 15.8% with most values below 11% (Table 3 and Figure 9). Similarly to the height statistics, we do not observe systematic differences between one method and another, or between one lake and another. Nevertheless, Profile GEDI/contours and Height S3/area methods are particularly impacted by some higher RMSEs due to the dispersion in the volume-area curve. In addition, some poor performances have been improved when going from height to volume accuracy, whereas some good performances have been reduced. This observation reflects that volume accuracy is not only a matter of height-area relationship accuracy and dispersion, but also a matter of height-area shape. This statement is supported by the results over Toussiana reservoir, where the difference between the Height S3/area method and the others methods are much more pronounced.
Table 2. Polynomial fit statistics of the area-height relationships.

<table>
<thead>
<tr>
<th>Location</th>
<th>DSM Pleiades</th>
<th>DSM Pleiades/contours</th>
<th>Profile ICESat-2/contours</th>
<th>Profile GEDI/contours</th>
<th>Height S3/area</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Polynomial degree / R² / RMSD (m) / NRMSD (%)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Agoufou</td>
<td>5 / &gt; 0.99 / &lt; 0.01 / 0.04</td>
<td>5 / 0.99 / 0.02 / 1.32</td>
<td>4 / 0.99 / 0.04 / 2.1</td>
<td>5 / 0.98 / 0.02 / 0.92</td>
<td></td>
</tr>
<tr>
<td>Arzuma</td>
<td>5 / &gt; 0.99 / 0.01 / 0.23</td>
<td>3 / 0.99 / 0.08 / 2.04</td>
<td>5 / 0.8 / 0.09 / 2.26</td>
<td>4 / 0.96 / 0.12 / 3.17</td>
<td>1 / 0.81 / 0.34 / 8.59</td>
</tr>
<tr>
<td>Babou</td>
<td>5 / &gt; 0.99 / 0.01 / 0.62</td>
<td>5 / &gt; 0.99 / 0.03 / 1.36</td>
<td>5 / 0.98 / 0.05 / 2.23</td>
<td>5 / 0.98 / 0.05 / 2.21</td>
<td>4 / 0.96 / 0.12 / 5.58</td>
</tr>
<tr>
<td>Bam</td>
<td>5 / &gt; 0.99 / 0.03 / 0.82</td>
<td>5 / 0.95 / 0.12 / 3.82</td>
<td>5 / 0.97 / 0.09 / 2.93</td>
<td>4 / 0.93 / 0.1 / 3.14</td>
<td>2 / 0.98 / 0.1 / 3.23</td>
</tr>
<tr>
<td>Bangou Kirey</td>
<td>5 / &gt; 0.99 / &lt; 0.01 / 0.09</td>
<td>2 / 0.9 / 0.09 / 5.25</td>
<td>1 / 0.31 / 0.08 / 4.61</td>
<td>4 / 0.87 / 0.03 / 1.52</td>
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<tr>
<td>Bangui Mallam</td>
<td>5 / &gt; 0.99 / 0.01 / 0.4</td>
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<td>5 / 0.97 / 0.08 / 2.78</td>
<td>5 / 0.99 / 0.05 / 1.91</td>
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</tr>
<tr>
<td>Djigo</td>
<td>5 / &gt; 0.99 / 0.03 / 1.06</td>
<td>5 / 0.99 / 0.07 / 2.31</td>
<td>5 / 0.99 / 0.07 / 2.3</td>
<td>5 / 0.97 / 0.07 / 2.58</td>
<td>5 / 0.96 / 0.13 / 4.48</td>
</tr>
<tr>
<td>Inbanta</td>
<td>5 / 0.98 / 0.21 / 3.36</td>
<td>3 / 0.8 / 0.14 / 2.36</td>
<td>5 / 0.96 / 0.07 / 1.18</td>
<td>5 / 0.94 / 0.07 / 1.13</td>
<td>1 / 0.68 / 0.24 / 3.88</td>
</tr>
<tr>
<td>Kokorou</td>
<td>5 / &gt; 0.99 / &lt; 0.01 / 0.03</td>
<td>1 / 0.98 / 0.04 / 1.46</td>
<td>5 / 0.98 / 0.08 / 2.48</td>
<td>5 / 0.94 / 0.1 / 3.33</td>
<td></td>
</tr>
<tr>
<td>Manga</td>
<td>5 / &gt; 0.99 / &lt; 0.01 / &lt; 0.01</td>
<td>4 / &gt; 0.99 / &lt; 0.01 / &lt; 0.01</td>
<td>2 / 0.91 / 0.08 / 4.91</td>
<td>5 / 0.99 / 0.03 / 1.61</td>
<td>3 / 0.97 / 0.09 / 5.64</td>
</tr>
<tr>
<td>North Tanvi</td>
<td>5 / 0.99 / 0.15 / 2.63</td>
<td>4 / 0.99 / 0.06 / 1.17</td>
<td>5 / &gt; 0.99 / &lt; 0.01 / &lt; 0.01</td>
<td>3 / 0.92 / 0.09 / 1.61</td>
<td>5 / &gt; 0.99 / &lt; 0.01 / &lt; 0.01</td>
</tr>
<tr>
<td>Seguenega</td>
<td>5 / &gt; 0.99 / 0.01 / 0.34</td>
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<td>1 / 0.84 / 0.09 / 3.6</td>
<td>5 / 0.95 / 0.11 / 4.36</td>
<td>4 / 0.95 / 0.13 / 4.97</td>
</tr>
<tr>
<td>Seytenga</td>
<td>3 / &gt; 0.99 / 0.01 / 0.25</td>
<td>4 / 0.99 / 0.04 / 1.92</td>
<td>5 / 0.99 / 0.03 / 1.58</td>
<td>5 / 0.94 / 0.09 / 4.23</td>
<td>3 / 0.94 / 0.1 / 4.9</td>
</tr>
<tr>
<td>South Tanvi</td>
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<td>5 / 0.99 / 0.05 / 1.91</td>
<td>3 / 0.82 / 0.12 / 4.43</td>
<td>3 / 0.85 / 0.11 / 4.1</td>
<td>1 / 0.93 / 0.2 / 7.53</td>
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<tr>
<td>Tibin</td>
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<td>5 / &gt; 0.99 / 0.02 / 0.63</td>
<td>5 / 0.99 / 0.06 / 2.32</td>
<td>5 / 0.99 / 0.04 / 1.57</td>
<td>2 / 0.97 / 0.1 / 4.02</td>
</tr>
<tr>
<td>Toussiana</td>
<td>5 / &gt; 0.99 / 0.01 / 0.12</td>
<td>4 / &gt; 0.99 / 0.03 / 0.79</td>
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<td>2 / 0.99 / 0.07 / 1.8</td>
<td>1 / 0.94 / 0.3 / 7.3</td>
</tr>
</tbody>
</table>
Figure 8. Box plot of the water elevation precision achieved by the different data sources. For each lake in x-axis, we plot the distribution of the water elevation precision in y-axis. The precisions computed for each transect/contour are stacked into a box reflecting the 25th, 50th and 75th percentiles of the distribution. Water elevations resulting from only one measurement are rejected.
Figure 9. Comparison between relative volumes from in-situ (x-axis) and from other methods (y-axis). The 1:1 curve is plotted as grey dashed line.
lower when looking at the volume accuracy than the height accuracy metrics. We think that this is mainly due to the shape of the Height S3/area-derived height-area relationship that allows the volume-area relationship to fit the in-situ data more closely (Figure 5).

Table 3. Accuracy statistics of height and volume.

<table>
<thead>
<tr>
<th></th>
<th>DSM Pleiades</th>
<th>DSM Pleiades/contours</th>
<th>Profile ICESat-2/contours</th>
<th>Profile GEDI/contours</th>
<th>Height S3/area</th>
<th>Combined opensource</th>
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<tr>
<td><strong>– Height –</strong></td>
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<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>R² / RMSE (m) / NRMSE (%)</td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>Agoufou</td>
<td>&gt; 0.99 / 0.03 / 2.31</td>
<td>0.98 / 0.04 / 2.62</td>
<td>0.97 / 0.05 / 3.64</td>
<td>0.97 / 0.05 / 3.64</td>
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<tr>
<td>Arzuma</td>
<td>0.99 / 0.09 / 3.11</td>
<td>0.98 / 0.13 / 4.58</td>
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<td>0.68 / 0.4 / 13.73</td>
<td>0.94 / 0.15 / 5.11</td>
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<td>Bam</td>
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<td>0.91 / 0.35 / 4.86</td>
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<td>0.87 / 0.3 / 5.87</td>
<td>0.98 / 0.28 / 5.49</td>
<td>0.96 / 0.25 / 4.93</td>
</tr>
<tr>
<td>Bangou Kirey</td>
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<td>0.66 / 0.11 / 4.2</td>
<td>0.48 / 0.23 / 8.93</td>
<td>0.48 / 0.23 / 8.93</td>
<td></td>
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</tr>
<tr>
<td>Kokorou</td>
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<td>0.73 / 0.07 / 2.56</td>
<td>0.96 / 0.11 / 3.97</td>
<td>0.87 / 0.09 / 3.27</td>
<td></td>
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</tr>
<tr>
<td>Seguenega</td>
<td>&gt; 0.99 / 0.03 / 1.43</td>
<td>0.94 / 0.07 / 3.84</td>
<td>0.97 / 0.11 / 5.64</td>
<td>0.92 / 0.14 / 7.27</td>
<td>0.88 / 0.14 / 7.43</td>
<td>0.91 / 0.11 / 5.95</td>
</tr>
<tr>
<td>Seytenga</td>
<td>0.95 / 0.27 / 6.23</td>
<td>0.9 / 0.28 / 6.57</td>
<td>0.94 / 0.22 / 5.24</td>
<td>0.91 / 0.27 / 6.28</td>
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<td>Toussiana</td>
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<td>&gt; 0.99 / 0.12 / 1.43</td>
<td>0.95 / 0.16 / 1.91</td>
<td>0.99 / 0.11 / 1.27</td>
<td>0.94 / 0.32 / 3.76</td>
<td>0.98 / 0.14 / 1.7</td>
</tr>
</tbody>
</table>

|                  |              |                       |                           |                       |               |                     |
| **– Volume –**    |              |                       |                           |                       |               |                     |
| R² / RMSE (Mm³) / NRMSE (%) |              |                       |                           |                       |               |                     |
| Agoufou           | > 0.99 / 0.05 / 2.37 | 0.98 / 0.08 / 3.51 | 0.98 / 0.08 / 3.77 | 0.98 / 0.16 / 7.23 |               |                     |
| Arzuma            | 0.99 / 0.14 / 2.99 | 0.98 / 0.2 / 4.27    | 0.32 / 0.3 / 6.37 | 0.93 / 0.28 / 5.86 | 0.62 / 0.71 / 14.97 | 0.94 / 0.27 / 5.79 |
| Bam               | 0.99 / 6.25 / 11.29 | 0.85 / 0.71 / 12.11 | 0.95 / 3.79 / 6.85 | 0.87 / 4.91 / 8.87 | 0.97 / 3.43 / 6.2 | 0.95 / 8.72 / 15.75 |
| Bangou Kirey      | 0.94 / 0.03 / 5.47 | 0.66 / 0.03 / 5.74  | 0.48 / 0.03 / 7.23 | 0.48 / 0.04 / 8.86 |               |                     |
| Kokorou           | 0.96 / 1.99 / 6.03 | 0.73 / 1.56 / 4.71  | 0.96 / 1.75 / 5.29 | 0.87 / 1.92 / 5.79 | 0.94 / 1.4 / 4.23 |               |
| Seguenega         | 0.99 / 0.07 / 2.83 | 0.91 / 0.12 / 4.72 | 0.37 / 0.17 / 7.0  | 0.9 / 0.15 / 6.03 | 0.87 / 0.16 / 6.27 | 0.9 / 0.17 / 6.84 |
| Seytenga          | 0.92 / 1.55 / 11.11 | 0.87 / 1.6 / 11.46 | 0.93 / 1.33 / 9.49 | 0.91 / 1.43 / 10.25 | 0.9 / 1.8 / 7.15 | 0.92 / 1.43 / 10.23 |
| Toussiana         | > 0.99 / 0.22 / 3.6 | > 0.99 / 0.17 / 2.78 | 0.95 / 0.24 / 3.89 | 0.99 / 0.16 / 2.51 | 0.92 / 0.46 / 7.37 | 0.97 / 0.45 / 7.31 |

3.4 Combining all height-area curves from open source data

When combining the methods based on open source data (Figure 10), the results give height RMSE between 0.05m and 0.25m and height NRMSE between 1.7% and 8.9% with most values below 6%. The volume RMSE is between 0.04Mm³ and 8.72Mm³ with most values below 1.44Mm³, and the volume NRMSE is between 4.2% and 15.8% with most values below 10.3% (Table 3). Except for a few lakes, these results are comparable to that obtained with the Profile ICESat-2/contours method alone.

4 Discussion

4.1 Comparison with the literature

4.1.1 Precision and accuracy of the area-height relationships

Many publications (Schwatke et al., 2020; Busker et al., 2019; Li et al., 2020; Chen et al., 2022) show similar results to those shown in 3.3.1 about the dispersion in the area-height relationships, and reported high values of R² (> 0.90). This is expected as water surface height and area are correlated. Our results with the Height S3/area method (RMSD values between 0.09m and 0.34m, with average being 0.16m) are slightly better that those of...
Figure 10. Combination of height-area curves from ICESat-2-, GEDI- and Sentinel-3-based methods for a) lakes with in-situ data and b) other lakes.
Schwatke et al. (2020) who reported RMSD values between 0.15m and 0.53m, and average
of 0.27m, over 6 Texan lakes having a number of points comparable to that of our curves
(e.g. 32 points or less). Schwatke et al. (2020) used altimetry data from multiple missions
with different accuracy, allowed a time lag of up to 10 days between water surface height and
area data acquisitions, and did not perform time interpolation to generate the matchups,
which may cause slightly larger RMSD.

Regarding the height-area relationship accuracy, most RMSE values are below 0.30m.
Li et al. (2020) obtained RMSE values of 0.06m, 0.47m, 0.76m and 1.20m over four medium-
sized lakes (1-100km$^2$) when validating their height-area curves derived from the combi-
nation of either ICESat, Hydroweb (https://hydroweb.theia-land.fr) (Crétaux et al.,
2011) or G-REALM (https://ipad.fas.usda.gov/cropexplorer/global_reservoir/)
(Birkett et al., 2011) altimetry data with water areas from the Joint Research Center (JRC)
Global Surface Water (GSW) dataset (Pekel et al., 2016). Part of the difference with our re-
sults may be explained by elevation biases between remote sensing and in-situ data reported
in the study of Li et al. (2020).

4.1.2 Precision of the height estimations

The water elevation precision along lake contours has been assessed in Section 3.3.2,
with values ranging between 0.04m and 0.19m, and most values below 0.13m. Five lakes
show a precision better or equal to 0.08m. These values are in line with Arsen et al. (2013)
who reported water contour elevation standard deviations ranging from 0.02m to 0.11m
when intersecting ICESat 170m posting rate banks elevation profiles with water contours
over lake Poopo in Bolivia.

For GEDI, we did not find assessment of the water elevation precision along contour
lines in the literature. If we compare the water contour elevation precision with values
obtained along transects over water from other publications, our results (precision between
0.04m and 0.23m, with most values below 0.13m) are in line with Z. Zhang et al. (2023)
who studied the water level dynamics of Qinghai Lake with GEDI data. The large biases
noted on GEDI profiles from different acquisition dates were also pointed out by Fayad et
al. (2020), and require further investigations.

For Sentinel-3, Taburet et al. (2020) reported a median standard deviation of water
elevation of 0.17m. This is consistent but slightly higher than our results, which is expected
as Taburet et al. (2020) studied thousands of water bodies, including rivers. Also, the use
of the median absolute deviation in our study provides better results compared to using the
standard deviation. More generally, standard deviations of a few centimeters have already
been achieved over larger lakes with radar altimeters previous to Sentinel-3 (Crétaux &
Birkett, 2006). This study shows that such a performance can be achieved on small and
medium-sized lakes as well.

4.1.3 Water area estimations

The MNDWI threshold for water classification has been determined ad hoc for each
lake. Using the same spectral index, we also tested automatic methods based on histogram
analysis such as Otsu (Otsu, 1979) and Minimum Error Thresholding (Kittler & Illingworth,
1986). Both methods assume that the MNDWI distribution is bi-modal with two classes
respectively associated with land and water. The Otsu’s method determines the optimal
threshold as the value which maximizes the inter-class variance and the MET method as-
sumes that the histogram is a mixture of two gaussian-like distributions associated with the
respective classes. Both methods were found to perform poorly in particular for lakes cov-
ered by aquatic vegetation (tri-modal histograms) or for lakes almost dried out (monomodal
histograms for some dates). Consequently, we decided to follow De Fleury et al. (2023) and
use ad hoc MNDWI thresholding. For some lakes, fairly negative threshold values have been
selected to account for aquatic vegetation (Table S1). We acknowledge that spatio-temporal variations in spectral signature of the lake or atmospheric conditions may lead to underestimation or overestimation of the water surface area, but ad hoc thresholding allows for a more consistent time series. The accuracy of the water surface areas has not been directly assessed but the results of Section 3.3.2 indicate that the precision of the water contours elevation is of the order of 0.10m to 0.20m. This, combined with the satisfactory height-area relationships dispersion and accuracy, reflects a good water contours detection accuracy and proves ad hoc MNDWI thresholding to be efficient for our study.

4.1.4 Accuracy of the volume-area relationships

We reported volume NRMSE between 2.3% and 15.8%, with most values below 11%. This is in line with Busker et al. (2019) who validated volume variations derived from the combination of radar altimetry and GSW monthly areas over 18 global lakes and reservoirs and obtained NRMSE between 1.784% and 18.872% with most values below 11% (extrapolated volumes excluded). Schwatke et al. (2020) also obtained similar results with NRMSE (defined as the RMSE divided by the difference of the 95% percentile and the 5% percentile of the height variations) varying between 2.8% and 14.9%, with an average of 8.3%, when validating against in-situ volume variations. The in-situ data used in our study come from various sources (with errors difficult to estimate) and may induce different uncertainties during the comparisons.

4.2 Pros and cons of each method

4.2.1 Pleiades-based methods

Pleiades-based height-area relationships show generally good performance in terms of accuracy, water elevation precision and dispersion. In particular, those derived from the DSM Pleiades method have the advantage of relying on a single data source. However, our study shows that despite their very high spatial resolution, Pleiades DSMs should be subjected to preliminary quality checks for issues related to jitter and high noise due to low pixel correlation, which can introduce errors of several meters. Dried out lake Pleiades DSMs allow characterizing the topography of the whole lake bathymetry but also represent a challenge for the estimation of the lake bottom altitude. Indeed in the absence of water, determining the starting altitude of the height-area relationship is not straightforward as the lake bottom may show high noise. In this study we manually selected a starting altitude from which water areas increase significantly. Alternative options might be to use the elevation from an external water contour intersected with the DSM, or to correct for the amplitude of the noise estimated over a flat area. If the noise is more widely spread over the banks (not only on the lake bottom but also on higher parts of the banks), reducing the starting altitude is mandatory in order not to underestimate the water areas subsequently computed.

The DSM Pleiades/contours method, which combines Pleiades DSMs with water contours, requires an additional data source compared to the DSM Pleiades method but is not affected by the effect of dry lake noise on the starting elevation of the curves, as these are truncated to the minimum water contour extent. More generally, Pleiades DSMs represent the surface elevation, and thus remain affected by all kinds of relief such as vegetation whose footprint on the DSMs is often wider due to smoothing in the DSM generation processing.

4.2.2 Lidar-based methods

Profile ICESat-2/ and Profile GEDI/contours methods are able to generate accurate height-area relationships over small to medium-sized lakes with sometimes a single but more often a few numbers of bank elevation profiles. Furthermore, these relationships are consistent with very high resolution DSM-based curves and highlight the potential of existing lidar altimetry missions for lake volume changes monitoring. We also note that the satis-
factory water elevation precision obtained with ICESat-2 and GEDI data suggests that the
algorithm implemented in the respective operational products used in this study properly
separate echos from tree canopy and ground. Nonetheless, the methods face some limita-
tions. Among them, the height-area relationship quality depends on the lake’s shape and
the attack angle of the lidar altimeter ground tracks with respect to the water contours. The
more parallel to the lake the trajectory is, the bigger the impact of water detection errors on
the resulting contour elevation will be. The location of the lidar profiles is important as well
since it also conditions the sensitivity of the methods to water detection errors (as it could
be the case for dendritic lakes or profiles located close to the shore). The lidar data posting
rates of respectively 60m and 100m represent a limitation with respect to the range of bank
slope that can be observed. A threshold on the bank slope must be applied to prevent
errors induced by linear interpolation of the topography or water detection which is more
challenging as the banks get steeper. Another limitation of ICESat-2 (nominal revisit time
of 91 days, drifting orbit during the first two years of the mission) and GEDI (variable re-
visit time) data is the temporal coverage which conditions the observable volume dynamics.
In addition, GEDI suffers from some degraded acquisition periods (Urbazaev et al., 2022).
Finally, being optical sensors, lidars are not suited to areas with important cloud cover. In
this study we were not significantly impacted by this effect as the dry season, with very low
or absent cloud cover, represents the major part of the year in the study area.

4.2.3 Height S3/area method

As well as lidar data, Sentinel-3 data are less impacted by relief than the Pleiades
DSMs and better separate water from flooded vegetation, as suggested by the comparison
between Height S3/area and Pleiades-based height-area relationships over the Inbanta lake.
One of the advantages of Sentinel-3 data, in addition to having no trouble with cloud cover,
is also the temporal coverage (revisit time of 27 days) which excludes the acquisition dates
dependency associated with the other methods and may allow observing a greater water
volume dynamics. Even more frequent revisit time is possible with Sentinel-6 data (10
days) but the spatial coverage decreases substantially (e.g. only one of the lakes studied
is covered by Sentinel-6). Nonetheless, despite good water surface height precision (below
0.10m for most lakes), the Height S3/area method tends to generate height-area relationships
with more dispersion (Section 3.3.1). In addition to the impact of time interpolation for
matching S2 and S3 data, part of these errors might be attributed to contamination of the
radar waveform by surrounding bright surfaces such as crops, humid soils or neighboring
water bodies which challenge the retracking (Boy et al., 2022).

4.3 Learnings from this study

4.3.1 Characterization of small and shallow water bodies

Overall, the methods were able to derive consistent height-area relationships of small
and medium-sized lakes with areas ranging from tens of hectares to tens of square kilometers
and small height amplitudes about 1.5m. This result represents a step forward for volume
change monitoring of shallow lakes. Indeed, multiple publications in the literature focus on
lakes with higher water level amplitude or use 1m-vertical resolution DEM such as SRTM
data to estimate height-area relationships or volume changes (Fang et al., 2019; S. Zhang
& Gao, 2020; Pan et al., 2013; Yao et al., 2018).

The slope breaks and curvatures consistently observed on the height-area relationships
of some lakes such as Djigo, Kokorou and Tibin (Figure 5) are of particular interest as they
reveal fine shape behaviors. Since multiple existing studies (Gao et al., 2012; Crétaux et
al., 2015; Buskert et al., 2019; Smith & Pavelsky, 2009; S. Zhang & Gao, 2020; Bhagwat et
al., 2019; Fang et al., 2019; Li et al., 2020; Chen et al., 2022), consider linear, quadratic or
power-law regressions to fit the height-area relationship, our observations show that such
assumptions might be unsuited to capture complex shape patterns in the case of small and medium-sized lakes.

4.3.2 Spatial coverage and data accessibility

Pleiades images are commercial data, so they are not open-access. We tested the potential of open-access global DEMs such as SRTM data to produce height-area relationships. For this, the DEM filling method has been used on the SRTM DEM of each of the sixteen lakes studied. With the exception of the Tibin reservoir, which is among the largest studied lakes (mean area of 15.39 km$^2$) and was not impounded yet during the SRTM acquisition, the resulting height-area relationships showed a general disagreement with all other methods, as they were almost systematically steeper. Moreover, the 1-m vertical resolution of SRTM, as well as that of other global DEMs such as the ALOS Global Digital Surface Model (AW3D30) or the ASTER Global Digital Elevation Map (GDEM), is insufficient to capture water surface height variations of a few meters that we commonly observe. GLO-30 Copernicus DEM has a better vertical resolution but represents a 2011-2015 averaged topography from multiple DEMs derived from the TanDEM-X mission and acquired with different water levels. Hence, bank topography must be regarded carefully as it may contain contributions from water.

Due to the spatial coverage limitation of the conventional altimetry missions, none of the studied lakes are included in the global databases such as Hydroweb, G-REALM or the Database for Hydrological Time Series of Inland Waters (DAHITI, https://dahiti.dgfi.tum.de/en) (Schwatke et al., 2015). De Fleury et al. (2023) intersected Sentinel-3A and Sentinel-3B altimeter ground tracks with the lakes maximum water extent from GSW dataset over Central Sahel and estimated a total number of only 150 lakes below the tracks, which is far below the several thousands of water bodies found in the region by Pi et al. (2022). Moreover, the inter-track distance of other altimetry missions such as Sentinel-6 is larger than that of Sentinel-3. This emphasizes the limited spatial coverage of the radar altimeters.

Multi-beams lidar altimetry data from ICESat-2 and GEDI missions allows bypassing the limitations mentioned above by providing open-access surface elevation data with enhanced spatial coverage compared to that of radar altimetry missions. Indeed, Chen et al. (2022) showed for example that the ICESat-2 ATL13 product allowed observing 2 to 7 times more global water bodies than what the traditional altimetry missions can do. The ATL13 product being spatially limited by a shape mask derived from existing inland water bodies databases (Jasinski et al., 2023), it is likely that the ATL08 product used in our study allows for an even better spatial coverage.

4.3.3 Combination of methods based on open-access data

We showed that combining the methods based on non-commercial data gave results comparable to that obtained with the Profile ICESat-2/contours method alone, so the benefit in terms of accuracy is not substantial. However, combining different methods mitigates some of the limitations of each method and provides more robust curves. The temporal coverage (sub-monthly revisit time) of radar altimetry data and the spatial coverage of lidar data improve the height-area curves extent and the number of water bodies observed, respectively. Thus, the combination of radar and lidar altimetry data provides an open source solution for upsampling volume dynamics analysis to a wider range of lakes, as the methods are easily transferable to other lakes. This could be of particular interest for the monitoring of ungauged lakes or lakes with outdated in-situ data.
5 Conclusion

The height-area relationships of sixteen lakes and reservoirs in West Africa have been derived from four different methods. These methods used different data sources such as Pleiades DSMs, Sentinel-2 optical imagery, ICESat-2 and GEDI lidar altimetry and Sentinel-3 radar altimetry. We found a generally good agreement with in-situ data (most height RMSE values below 0.30m and volume NRMSE values below 11%) and among the methods. With the exception of the Sentinel-3-based method which tends to produce higher dispersions, all methods provide curves with very low noise (fit RMSD values below 0.10m for most lakes). Fine shape patterns were consistently observed over small height amplitudes, highlighting the ability of the different methods to monitor shallow lakes with non-linear bathymetric behaviors. We found satisfactory water elevation precisions, with values close to 0.20m using Pleiades DSMs and slightly better values of the order of 0.13m or less using the other methods. We identified inherent limitations in terms of data quality, surface features, spatio-temporal coverage and data accessibility. This analysis suggests that lidar-based methods combined with radar altimetry data show similar performance to high-resolution DSMs-based methods and therefore have great potential for estimating water volume changes over lakes and reservoirs in this region. Furthermore, benefiting from its wide-swath Ka-band radar interferometer (KaRIN), the Surface Water and Ocean Topography (SWOT) mission, launched on December 16, 2022, will be able to observe 90% of the inland areas and all lakes larger than 250 x 250m$^2$ (requirements) located between 78°N and 78°S (Biancamaria et al., 2016). With a minimum revisit time of 21 days, SWOT will thus provide volume change estimates for the majority of the lakes and reservoirs in the study area, further expanding the number of water bodies that could be addressed by remote sensing. The H-A-V relationships derived in this study will provide a valuable database to assess SWOT performances in this area.

Open Research Section

Data Availability

The in-situ water surface elevation data on Bangou Kirey and Agoufou lakes are available in the AMMA-CATCH observatory database (www.amma-catch.org, DOI: https://doi.org/10.2136/vzj2018.03.0062). For the height-volume relationships of Bam, Seguenega and Sceytenga reservoir, please contact the Institut International d’Ingénierie de l’Eau et de l’Environnement (2IE, ousmane.yonaba@2ie-edu.org, tazen.fowe@2ie-edu.org). The height-area relationships of the Kokorou lake and Toussiana reservoir have been extracted respectively from Baba et al. (2019) and Sanogo and Dezetter (1997).


The Ice, Cloud and land Elevation Satellite-2 (ICESat-2) L3A Land and Vegetation height data product (ATL08) is accessible on the National Snow and Ice Data Center (NSIDC) website (https://nsidc.org/data/atl08/versions/6). The Global Dynamics Ecosystem Investigation (GEDI) L2A Geolocated Elevation and Height Metrics (GEDI02_A) are downloaded from the NASA Land Processes Distributed Active Archive Center (LP DAAC, https://lpdaac.usgs.gov/products/gedi02_av002/).

The dataset containing the height-area-volume relationships of the remote sensing-based methods is provided as a CSV file accessible through https://dataverse.ird.fr/privateurl.xhtml?token=ac61adc6-254a-4ccc-9061-7a6d1bd21612. The dataset also includes the in-situ data-based height-area-volume relationship of the Arzuma reservoir. In
order to allow a direct comparison, the provided relationships are all unbiased with respect to the DSM Pleiades method.

Acknowledgments
This work was supported by CNES through the APR program funding the SPLASH project, in the framework of the pre-launch activities related to the SWOT mission. Occitanie Region and Collecte Localisation Satellites (CLS) also supported this work by funding Félix Girard’s PhD thesis. We acknowledge CNES and Airbus DS for providing the Pleiades images, and the AMMA-CATCH observatory for in-situ data supply in Niger and Mali. We are very grateful to Nicolas Taburet and Nicolas Picot for discussions on the altimetry data, to Etienne Berthier for sharing his expertise on DSM processing and analysis, to Guillaume Favreau for sharing his knowledge of water bodies in Niger, and to Jean-Marie Dipama for information on reservoirs in Burkina Faso.

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Supporting Information for "Comparison of methods to derive the height-area relationship of shallow lakes in West Africa using remote sensing"

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Contents of this file

1. Table S1

Introduction

Supporting information with a table containing the information and data availability on the lakes studied.

Table S1.
<table>
<thead>
<tr>
<th>Location</th>
<th>Coordinates</th>
<th>Lake area (km²)</th>
<th>MNDWI threshold</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Agoufou</td>
<td>15.37°N, -1.47°E</td>
<td>1.98</td>
<td>0.09</td>
<td>(Grippa et al., 2019; Gal et al., 2016; Gardelle et al., 2010)</td>
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<tr>
<td>Arzuma</td>
<td>12.22°N, -1.31°E</td>
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<td>-0.04</td>
<td>(De Fleury et al., 2023)</td>
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<tr>
<td>Babou</td>
<td>12.88°N, -1.61°E</td>
<td>0.60</td>
<td>-0.10</td>
<td>(De Fleury et al., 2023)</td>
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<td>Bam</td>
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<td>(De Fleury et al., 2023)</td>
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<td>Bangou Kirey</td>
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<td>0.09</td>
<td>(Touré et al., 2016)</td>
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<td>Bangui Mallam</td>
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<td>(Gardelle et al., 2010)</td>
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<td>(Baba et al., 2019)</td>
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<td>Manga</td>
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<td>North Tanvi</td>
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<td>(De Fleury et al., 2023)</td>
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<td>South Tanvi</td>
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<td>Toussiana</td>
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<td>0.00</td>
<td>(De Fleury et al., 2023)</td>
</tr>
<tr>
<td>Arizona</td>
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<td>2.07</td>
<td>-0.10</td>
<td>(De Fleury et al., 2023)</td>
</tr>
</tbody>
</table>

**Legend:**
- **DGRE:** Depth-Ground Elevation Reference System
- **ICESat-2:** Ice Cloud counter-Earth Satellite
- **GEDI:** Global Elevation Data and Imaging System
- **Pleiades:** Pan-European Lidar and Imaging System
- **SRTM:** Shuttle Radar Topography Mission

**Notes:**
- The table includes lake area, MNDWI threshold, and references for each location.
- The data was collected between February 28, 2024, and April 15, 2024.
References


February 28, 2024, 4:08pm