Characterizing Volcanic Ash Density and its Effects on Dispersion Forecasts

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Volcanic ash clouds are carefully monitored as they present a significant hazard to humans and aircraft. The primary tool for forecasting the transport of ash from a volcano is dispersion modelling. These models make a number of assumptions about the size, sphericity and density of the ash particles. Few studies have measured the density of ash particles or explored the impact that the assumption of ash density might have on the output of a dispersion model. In this paper, the raw apparent density of 23 samples taken from 15 volcanoes are measured with gas pycnometry, and a negative linear relationship is found between the density and the silica content. For the basaltic ash samples, densities were measured for different particle sizes, showing that the density is approximately constant for particles smaller than 100 μm. There is a deviation in density of up to 25% from the operational model currently used by the London Volcanic Ash Advisory Centre (VAAC); by inputting the measured density-size relationship into a numerical simulation, up to 18% difference in ash fallout time was found, with the VAAC model overestimating ash removal times.
Characterizing Volcanic Ash Density and its Effects on Dispersion Forecasts

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Key Points:
\begin{itemize}
  \item The density of volcanic ash is measured as a function of particle size for a range of eruptions.
  \item Silica content and particle size negatively correlate with density.
  \item The density of particles smaller than 100 µm is approximately constant but is dependent on silica content.
\end{itemize}

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Abstract

Volcanic ash clouds are carefully monitored as they present a significant hazard to humans and aircraft. The primary tool for forecasting the transport of ash from a volcano is dispersion modelling. These models make a number of assumptions about the size, sphericity and density of the ash particles. Few studies have measured the density of ash particles or explored the impact that the assumption of ash density might have on the output of a dispersion model. In this paper, the raw apparent density of 23 samples taken from 15 volcanoes are measured with gas pycnometry, and a negative linear relationship is found between the density and the silica content. For the basaltic ash samples, densities were measured for different particle sizes, showing that the density is approximately constant for particles smaller than 100 µm. There is a deviation in density of up to 25% from the operational model currently used by the London Volcanic Ash Advisory Centre (VAAC); by inputting the measured density-size relationship into a numerical simulation, up to 18% difference in ash fallout time was found, with the VAAC model overestimating ash removal times.

1 INTRODUCTION

Volcanic ash is composed of hard, silicic and abrasive fragments of rock, minerals, glass. During explosive volcanic eruptions, dissolved gases in magma are heated and expand abruptly, shattering a large amount of magma and rock materials into pyroclast fragments (Kenedi, 2000). These pyroclasts can be categorized according to diameter into ash (< 2 mm), lapilli (2-64 mm), bombs (> 64 mm) (Fisher & Schmincke, 1984). The size of these particles often have the same order of magnitude as the gas bubble that shattered them, and since there is a lower limit of the size of gas bubbles, ash smaller than a few microns are rarely found (Sparks & Wilson, 1976; Rust & Cashman, 2011).

Volcanic ash is harmful to humans when inhaled (Gislason et al., 2011; Horwell & Baxter, 2006; Horwell, 2007), and it poses a risk to aviation even at a large distance from the vent (Casadevall, 1994; Dunn & Wade, 1994; Pieri et al., 2002; Guffanti & Tupper, 2015). For example, during the 2010 Eyjafjallajökull eruption, a large area of airspace over Europe was closed for several days to minimize the risk to aviation, causing significant financial losses (Rincon, 2011). This eruption provided the impetus for further development of existing dispersion models, measurements, and approaches to manage these hazards. (Beckett et al., 2020).

The London Volcanic Ash Advisory Centre (VAAC) is responsible for providing analysis of volcanic ash dispersion in the North Atlantic and Arctic area surrounding countries including the United Kingdom and Iceland. Together with other VAACs around the world, it use a range of measurements, satellite observations, and models to study eruptions, with the primary objective of mitigating aviation risk from ash clouds (Beckett et al., 2020).

The size, shape and density of ash particles have all been shown to influence the maximum travel distance of volcanic ash (Beckett et al., 2015). However, density is usually assigned an assumed value due to limited measurements. The London VAAC uses a constant density of 2.3 g cm\(^{-3}\) in their operational model, NAME (Beckett et al., 2020). The ash density is also assumed when estimating the total mass of ash from satellite data (Beckett et al., 2017). In addition, when exploiting the Doppler shift of ash particles for determining the fall velocity and hence particle-size distribution (PSD), the results are very sensitive to the assumptions on density (Bonadonna et al., 2011).

There are multiple definitions of density (Webb & Orr, 1997; Vogel et al., 2017). The following definitions are adopted here:
• Bulk density takes the total volume enveloping the entire particle sample, including void between particles.
• Apparent / skeletal density takes the volume of the particle including closed pores (pores that are sealed off from the outside) but excluding open pores.
• Dense-rock-equivalent (DRE) / true density takes the volume of the particle excluding both open and closed pores. It measures the net density of the solid fraction.

While travelling in the atmosphere, air molecules may seep into the open pores but not the closed pores of ash particles. Therefore the aerodynamically meaningful density comes from the skeletal structure. Unless otherwise stated, this work uses density to mean the apparent density.

In this study, the density of 22 ash samples from 15 volcanoes measured with a pycnometer, are presented. The measured densities are compared with the ash composition, and for some of the samples, against the particle size. Finally, the impacts of applying these measured properties of density in dispersion models is explored.

2 BACKGROUND

2.1 Current knowledge on density

Variations in density may originate from i) composition, and ii) porosity inside the particle. Ash particles generally follow the composition of the magma they originate from. They can be classified by a total alkali-silica (TAS) diagram, which plots $K_2O/Na_2O$ (alkaline) versus $SiO_2$ (silica) content for volcanic rocks. Alkalinity in volcanic ash is relatively low, such that it is sufficient to group ash into four major types of magma based on silica content (Krishnan et al., 2017). In terms of percentage $SiO_2$ by weight, they are basalts (41-54%), andesites (54-63%), dacites (63-70%), and rhyolites (65-75%) (M. Wilson, 1989). The boundaries are not clear-cut: for example “basalt-andesites” would describe a transitional composition between the two categories. Vogel et al. (2017) used water pycnometry to show that the DRE density decreases with a linear trend as silica content increases, suggesting that silica content can be the dominant predictor of density of non-porous pyroclasts.

While silica-rich magma has higher dissolved gas content, it is also more viscous, enabling more explosive eruptions (Parfitt & Wilson, 2009). This process further introduces gas into the solidifying pyroclast, causing the pumice and ash formed from these magma to be more porous. Porosity and particle size are also closely related. If a large porous pyroclast breaks down into smaller pieces, the larger fragments could encapsulate more and larger closed pores and hence have a lower density. Therefore, a decreasing density is expected with increasing size for a given ash composition.

Fine particles can travel a long distance in air before falling out, and fuse with larger grains that act as a core in a process known as aggregation (Rossi et al., 2021). This effect altering the particle size and density, but it is prominent only when the particle concentration is high (Del Bello et al., 2017), so any identified aggregates are measured separately.

Many prior studies used simplified density-size models: for example, L. Wilson and Huang (1979) studied clasts collected from the equatorial Pacific and S˜ ao Miguel, Portugal; measuring the dimensions of particles individually. They presented a model which fixed the densities for large (>300 µm) and small (<88 µm) particles, and fitted densities for intermediate sizes with linear interpolation (shown in Figure 1 as ‘General model’).

In the basaltic range, Beckett et al. (2015) established a density model based on scattered data from Eyjafjallajökull in Bonadonna et al. (2011). It used a piece-wise lin-
car fit to interpolate the sparse data, and is referred to as ‘EYJ 2010 model’ in Figure 1 and the rest of this paper.

Figure 1. Summary of representative current models and data relating apparent density $\rho$ and particle diameter $d$.

In the andesitic range, Bonadonna and Phillips (2003) presented another model (‘andesitic model’ in Figure 1), similarly interpolated, based on scattered data from the 1991 eruption of Mount Hudson in Scasso et al. (1994). The original data measured how the mean particle diameter and the apparent density of unsieved ash samples varied with distance from the vent. The samples consisted of a mix of all ash sizes, and the data points for the two measured quantities were attributed to different distances; therefore, only a rough trend line can be inferred by relating the lines of best fit, and is presented in Figure 1 as ‘andesitic data fit’.

In the rhyolitic range, Bonadonna and Phillips (2003) interpolated a similar model based on scattered data from Askja, provided in Sparks et al. (1997); this model is presented in Figure 1 as ‘rhyolitic model’. Pistolesi et al. (2015) measured density using water pycnometry of ash from the 2011 Cordón Cautle eruption, Chile. They showed an approximately linear decrease between log diameter and density for pyroclast diameters between 500 and 16,000 $\mu$m (‘rhyolitic data fit’ in Figure 1), providing some support for linear models. However, water pycnometry does not measure apparent density well, and the minimum particle size measured was 500 $\mu$m, which is larger than a lot of ash produced.

Measurements of larger pyroclasts have been more abundant than ash. For example, Sparks et al. (1981) measured larger pyroclasts from the 1875 Askja eruption, and found that density generally decreases with size for diameters between 11,000 to 90,000 $\mu$m. Despite these findings, the detailed relationship between particle size and density has remained incomplete. In many cases, the diameter coverage was partial; some relied on other assumed relationships or water pycnometry.
2.2 Fall Velocity and Time of flight

The general expression for drag force $F_D$ on a particle with cross-sectional area $A$, travelling at velocity $v$ in a fluid with density $\rho_f$ and dynamic viscosity $\eta$ is:

$$F_D = \frac{1}{2} C_D \rho_f A v^2$$  \hspace{1cm} (1)

where $C_D$ represents the drag coefficient. The particle reaches terminal velocity when its own weight balances out with this drag force and buoyancy. Assuming a spherical particle with diameter $D$, apparent density $\rho$ and gravitational acceleration $g$:

$$\frac{4}{3} \pi \left(\frac{d}{2}\right)^3 (\rho - \rho_t) g = \frac{1}{2} C_D \rho_f A v^2$$  \hspace{1cm} (2)

implying that the terminal velocity $v_T$ is

$$v_T = \sqrt{\frac{4}{3C_D} \rho - \rho_t \frac{d}{\rho_t} g}$$  \hspace{1cm} (3)

$C_D$ itself depends on the Reynold’s number $Re$, defined as

$$Re = \frac{vd\rho_t}{\eta}$$  \hspace{1cm} (4)

White and Majdalani (2006) describes the drag coefficient for spherical particles for $Re$ between 0 and $2 \times 10^5$ with

$$C_D = \frac{24}{Re} + \frac{6}{1 + \sqrt{Re}} + 0.4$$  \hspace{1cm} (5)

In general, ash particles are sufficiently small such that terminal velocity can be treated as a constant fall velocity (also known as settling velocity). Therefore, this set of equations explicitly determines the settling velocity of spherical particles (and hence the time of flight and maximum drift distance). A non-spherical particle falls at a lower speed than its spherical equivalent, increasing the dispersion range (Beckett et al., 2015). For example, a 30 $\mu$m particle with sphericity $\Psi = 0.4$ travel 30% further than its spherical counterpart.

3 METHODOLOGY

Apparent density measurements were conducted using a nitrogen gas pycnometer. Gas pycnometry applies the ideal gas law to determine the skeletal volume of samples in a chamber by varying the size of the chamber and measuring the pressure change (Webb & Orr, 1997). Nitrogen is used to best study the apparent density and permeability of the ash particles in the atmosphere (open pores that are smaller than its molecular size will be discounted). Water vapour affects both the actual density and the ideal gas law calculations, so the ash samples were dried in a 98°C oven for over 48 hours to ensure moisture was sufficiently evaporated. While humidity varies in the atmosphere, this study aims to provide a standardized perspective by measuring the dry density.

Two sets of measurements were conducted:

1. The density of 23 unsieved raw ash samples originating from 15 volcanoes around the world were measured. Table 1 and Figure 2 present their locations and spec-
ify the abbreviations used for the samples. To ensure fair representation, the original jars of raw ash were gently mixed by rotation. When extracting samples to measure in the pycnometer, large (\sim 8 \text{ mm}) outliers were not included. The details of the samples are recorded in Reed (2016) alongside silica content.

2. Volcanic ash is most commonly basaltic (Walker, 1993), and our basaltic samples are large enough to be further sieved for measurements. In particular, samples from Mount Aso (VA1), Eyjafjallajökull (VA7), and Grímsvötn (VA4, 5) were sieved into different diameter groups. For larger particles (> 2 \text{ mm in diameter}), particles were handpicked and measured with a caliper. Densities were then measured for each particle size sample. For Grímsvötn, two sets of samples, from close (200 m from vent) to distal region (50 km from vent) are measured. There is a one-week interval between the collection dates of these two samples.

4 RESULTS

4.1 Unsieved ash density

Table 2 presents the skeletal densities of the 23 unsieved ash samples. Mass percentage of SiO_2 content values were measured using X-ray fluorescence (XRF) analysis by G. Prata et al. (2019). Figure 3 shows the measured unsieved ash density \( \rho_{us} \) versus silica content (%SiO_2). Higher silica content correlates to a lower density in a linear relationship,

\[
\rho_{us} = -0.016(\% \text{SiO}_2) + 3.54. \quad (6)
\]

The function between DRE density \( \rho_{DRE} \) and silica content measured by Vogel et al. (2017) is

\[
\rho_{DRE} = -0.019(\% \text{SiO}_2) + 3.90. \quad (7)
\]

Given the similarity of these correlations and \( \rho_{us} \) having a lower offset than \( \rho_{DRE} \) suggest porosity plays a systematic role in determining ash density.

4.2 Density-size distribution

Figure 4 shows the measured relationships between particle size and density for Eyjafjallajökull, Grímsvötn, and Mount Aso ash samples. The densities follow a similar pattern being constant at lower particle sizes, and then decreasing as the size increases. To fit the data, two candidate models were tried: piece-wise linear (PL), and smooth piece-
Table 1. Raw unsieved ash density

<table>
<thead>
<tr>
<th>Volcano (Abbrev.)</th>
<th>No.</th>
<th>Type</th>
<th>Distance from vent</th>
<th>Collection date</th>
<th>Estimated eruption</th>
<th>% SiO₂</th>
<th>( \rho_{us} ) / g cm(^{-3} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mount Aso, Japan (ASO)</td>
<td>VA1</td>
<td>Basaltic</td>
<td>&lt; 400 m</td>
<td>1993</td>
<td>1993</td>
<td>52.6</td>
<td>2.80</td>
</tr>
<tr>
<td>Eyjafjallajökull, Iceland (EYJ)</td>
<td>VA2</td>
<td>Basaltic</td>
<td>6 km</td>
<td>17/4/2010</td>
<td>2010</td>
<td>55.6</td>
<td>2.65</td>
</tr>
<tr>
<td>Eyjafjallajökull, Iceland (EYJ)</td>
<td>VA3</td>
<td>Basaltic</td>
<td>-</td>
<td>4/2010</td>
<td>14/4/2010</td>
<td>57.8</td>
<td>2.68</td>
</tr>
<tr>
<td>Eyjafjallajökull, Iceland (EYJ)</td>
<td>VA7</td>
<td>Basaltic</td>
<td>5 km</td>
<td>13/6/2010</td>
<td>19-20/5/2010</td>
<td>58.5</td>
<td>2.57</td>
</tr>
<tr>
<td>Eyjafjallajökull, Iceland (EYJ)</td>
<td>VA8</td>
<td>Basaltic</td>
<td>4.5 km</td>
<td>13/6/2010</td>
<td>19-20/5/2010</td>
<td>59.2</td>
<td>2.66</td>
</tr>
<tr>
<td>Eyjafjallajökull, Iceland (EYJ)</td>
<td>VA9</td>
<td>Basaltic</td>
<td>5 km</td>
<td>13/6/2010</td>
<td>19-20/5/2010</td>
<td>58.8</td>
<td>2.62</td>
</tr>
<tr>
<td>Eyjafjallajökull, Iceland (EYJ)</td>
<td>VA15</td>
<td>Basaltic</td>
<td>-</td>
<td>15-16/5/2010</td>
<td>2010</td>
<td>58.0</td>
<td>2.68</td>
</tr>
<tr>
<td>Grímsvötn, Iceland (GRI)</td>
<td>VA4</td>
<td>Basaltic</td>
<td>200 m</td>
<td>1/6/2011</td>
<td>21-28/5/2011</td>
<td>49.1</td>
<td>2.76</td>
</tr>
<tr>
<td>Grímsvötn, Iceland (GRI)</td>
<td>VA5</td>
<td>Basaltic</td>
<td>50 km</td>
<td>25/5/2011</td>
<td>21-28/5/2011</td>
<td>49.4</td>
<td>2.76</td>
</tr>
<tr>
<td>Mount Etna, Italy (ETN)</td>
<td>VA6</td>
<td>Basaltic</td>
<td>10 km</td>
<td>27-30/12/2002</td>
<td>10/2022-1/2023</td>
<td>47.0</td>
<td>2.58</td>
</tr>
<tr>
<td>Mount Etna, Italy (ETN)</td>
<td>VA10</td>
<td>Basaltic</td>
<td>-</td>
<td>1/7/2001</td>
<td>10/2022-1/2023</td>
<td>47.6</td>
<td>2.83</td>
</tr>
<tr>
<td>Mount Etna, Italy (ETN)</td>
<td>VA14</td>
<td>Basaltic</td>
<td>26 km</td>
<td>1/11/2002</td>
<td>10/2022-1/2023</td>
<td>47.1</td>
<td>2.85</td>
</tr>
<tr>
<td>Chaitén, Chile (CHA)</td>
<td>VA11</td>
<td>Rhyolitic</td>
<td>-</td>
<td>2008</td>
<td>2008</td>
<td>73.2</td>
<td>2.36</td>
</tr>
<tr>
<td>Mount Tongariro, New Zealand (TON)</td>
<td>VA16</td>
<td>Andesitic</td>
<td>-</td>
<td>2012</td>
<td>2012</td>
<td>59.4</td>
<td>2.60</td>
</tr>
<tr>
<td>Askja, Iceland (ASK)</td>
<td>VA17</td>
<td>Rhyolitic</td>
<td>-</td>
<td>1981</td>
<td>1875</td>
<td>70.7</td>
<td>2.35</td>
</tr>
<tr>
<td>Fontana Tephra, Nicaragua (FLD)</td>
<td>VA18</td>
<td>Basalt-andesitic</td>
<td>-</td>
<td>-</td>
<td>Late Pleistocene</td>
<td>-</td>
<td>2.62</td>
</tr>
<tr>
<td>Nisyros, Greece (NIS)</td>
<td>VA19</td>
<td>Rhyo-dacitic</td>
<td>-</td>
<td>2011</td>
<td>-</td>
<td>69.7</td>
<td>2.42</td>
</tr>
<tr>
<td>Mount Okmok, Alaska, USA (OKM)</td>
<td>VA20</td>
<td>Basalt-andesitic</td>
<td>-</td>
<td>7/2008</td>
<td>7/2008</td>
<td>-</td>
<td>2.74</td>
</tr>
<tr>
<td>Augustine, Alaska, USA (AUG)</td>
<td>VA21</td>
<td>Andesitic</td>
<td>-</td>
<td>13/1/2006</td>
<td>2005-2006</td>
<td>-</td>
<td>2.64</td>
</tr>
<tr>
<td>Mount Spurr, Alaska, USA (SPU)</td>
<td>VA22</td>
<td>Basalt-andesitic</td>
<td>-</td>
<td>8/1992</td>
<td>6-8/1992</td>
<td>-</td>
<td>2.73</td>
</tr>
<tr>
<td>Mount Redoubt, Alaska, USA (RED)</td>
<td>VA23</td>
<td>Andesite-dacitic</td>
<td>-</td>
<td>1990</td>
<td>1989-1990</td>
<td>-</td>
<td>2.68</td>
</tr>
<tr>
<td>Campi Flegrei, Italy (CFL)</td>
<td>VA24</td>
<td>Basaltic</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2.42</td>
</tr>
</tbody>
</table>

All \( \rho_{us} \) have a 2% uncertainty. The list of respective magma and ash type is gathered from Miyabuchi et al. (2006); Keiding and Sigmarsson (2012); Haddadi et al. (2017); Andronico et al. (2009); Lara (2009); Field et al. (2008); Cole et al. (2018); Sparks et al. (1981); Wehrmann et al. (2006); Longchamp et al. (2011); Francalanci et al. (1995); Larsen et al. (2013, 2010); Eichelberger et al. (1995); Nye et al. (1994); Esposito et al. (2018).
Figure 3. Unseived ash density versus silica content. A line of best-fit can be described by $ho_{us} = -0.016(\%SiO_2) + 3.54$. An obvious outlier (lower left) has been removed from the fit. It is a sample from Mount Etna which contains a large amount of biomass that is hard to remove. Uncertainties in SiO$_2$ are taken as 1%, the typical maximum uncertainty of XRF analysis (Rousseau, 2001). Uncertainty in $\rho$ is 2%.

wise quadratic (SPQ). Writing $x = \log d$ where $d$ is in $\mu$m, these models are specified respectively as:

$$
\rho = \begin{cases} 
  k & x < x_0 \\
  m(x - x_0) + k & x \geq x_0
\end{cases}
$$

(8)

$$
\rho = \begin{cases} 
  k & x < x_0 \\
  m(x - x_0)^2 + k & x \geq x_0
\end{cases}
$$

(9)

Naturally one would expect a smooth transition between the flat and the sloping parts of the function, but owing to the preferable simplicity of the PL model, smoothness can be compromised. For the SPQ model, smoothness is demanded by setting the formula in this form. Both models have three parameter degrees of freedom ($k$, $m$, $x_0$). A reduced chi-squared test is performed to determine the better model for each source. The best model for each one is (in g cm$^{-3}$):

Eyjafjallajökull (SPQ, $\chi^2 = 0.143$):

$$
\rho = \begin{cases} 
  2.68 & x < 2.78 \\
  -0.39(x - 2.78)^2 + 2.68 & x \geq 2.78
\end{cases}
$$

(10)

Grímsvötn (Proximal—200 m from vent) (SPQ, $\chi^2 = 0.150$):

$$
\rho = \begin{cases} 
  2.85 & x < 1.99 \\
  -0.33(x - 1.99)^2 + 2.85 & x \geq 1.99
\end{cases}
$$

(11)

Grímsvötn (Distal—50 km from vent) (SPQ, $\chi^2 = 0.848$):

$$
\rho = \begin{cases} 
  2.81 & x < 1.94 \\
  -0.24(x - 1.94)^2 + 2.81 & x \geq 1.94
\end{cases}
$$

(12)
Figure 4. Particle density-size distribution for Eyjafjallajökull (EYJ), Grímsvötn (GRI), and Mount Aso (ASO). Models by London VAAC and one assumed by Bonadonna et al. (2011) ("EYJ 2010 model") are overlaid on the diagrams, alongside lines of best fit following either a piece-wise linear or a smooth piece-wise quadratic function. Large circle markers indicate regular samples; squares and small circles indicate small (<10 particles) and single-particle samples. A cross in the second diagram indicates aggregates. Only the regular samples are used in fitting the functions. The fourth diagram shows the ratio of the measured density fit versus the referenced two models.

Aso (PL, $\chi^2 = 0.204$):

$$\rho = \begin{cases} 
2.71 & x < 2.64 \\
-0.23(x - 2.64) + 2.71 & x \geq 2.64 
\end{cases} \tag{13}$$

The constant portions confirm again that the higher the silica content, the lower the DRE density.

For Eyjafjallajökull, the samples were collected 6 km away from the vent. The measurements of fine ash plateaus to a similar DRE density as the EYJ 2010 model and previous studies. A striking difference is that the density starts decreasing at a much larger diameter (around 600 µm) than the EYJ 2010 model assumed (10 µm). In fact, measurements from all three sources support a later turning point than the previous models.

For Grímsvötn, the density plots are similar for ash samples collected at 200 m and 45 km from vent, suggesting that the density is unlikely to be sensitive to sampling lo-
cation (cf. grain size distribution). This would also suggest that one does not need to collect an excessive amount of samples to characterize ash density from an eruption.

For Aso, a PL model is adopted, contrary to the prior two sources. However, the difference in function is most likely statistical, as the $\chi^2$ evaluated with the two candidate functions are very close. The sample contains a mix of different colours, suggesting a wide range of compositions which may vary in abundance in difference size groups.

The measurements show that individual variations in density can be quite large. This is unsurprising as the existence of pores in a particle is probabilistic. Bonadonna and Phillips (2003) suggest that while pumice particle density would decrease substantially, lithic particles, which are a minor composition in ash, have a constant density. This is consistent with our data. Aggregates are also denser than individual particles on the same size, as they are composed of fine particles held together with much smaller closed pores.

Although silica-rich ash (e.g. Aso) are more porous, density falls off slower. Together with the observation from the silica content before, this suggests the dual role of pores—while more pores might lead to a hollower structure (lower density), to a certain extent the open pores might be populous enough to connect through the inner pores, discounting them from the particle volume and increasing density.

5 IMPLICATIONS

To assess how the new density measurements will affect model results Equations (1)-(5) were used to estimate settling velocity for spherical ash particles. Figure 5 shows settling velocity as a function of particle diameter for the EYJ 2010 model, the VAAC model, and the new density data. There is a maximum of 40% difference between the model predictions in the ash range.

![Figure 5](image)

Figure 5. Settling velocity $v_T$ versus particle diameter $d$ calculated using the new density measurements and the predictions of the VAAC and EYJ 2010 models. The second diagram shows the ratio between the calculated $v_T$ and the model predictions.

Equations (1)-(5) are used to compute the results in this section. Fig. 5 shows how settling velocity would change as a function of particle diameter—from the EYJ 2010 model, the VAAC model, and our data. The order of magnitude is unaltered by the new data; however it reveals a maximum of 40% difference from the previous model predictions in the ash range.
This substantially modifies the relationship between fall velocity and size. One direct impact of this is the in-situ measurement of particle-size distribution based on Doppler’s effect. A 40% difference in attributed fall velocity could lead to a two-fold difference in PSD determination.

Equally important is its effect on ash dispersion models. Beckett et al. (2015) compared the EYJ 2010 model and the VAAC model at particle diameters of 30 and 100 µm using NAME. At these sizes, densities from these two models differ by 4-9%. This leads to a 4-8% difference in \( v_T \) and a 4% simulated difference in maximum distance \( D \) reached by the particles for the Eyjafjallajökull eruption. For the same volcanic source, the new density measurements show a 17% difference from VAAC values for both these sizes, implying a 14-16% difference in \( v_T \). This suggests a change in \( D \) above 10%. The fact that VAAC currently uses the same density for all events causes an even larger difference for some sources—for example, the measured ash densities from Grímsvötn would give a 20-23% difference in \( v_T \) from the VAAC model.

An alternative method to assess density effects is through calculating the time of flight of particles. Grímsvötn ash density is used in this simulation as it deviated the most from the VAAC model. Its distal density distribution is adopted here. Neglecting aggregation, Figure 6 shows the time \( t_{\text{fallout}} \) it takes for ash of different diameters to fall from an initial height of 20 km. The lower panel also shows the ratio of this fallout time predicted by the various distributions. Results show that the measured ash would fall-out up to 18% quicker than the VAAC model. For example, 10 µm fine ash would be removed from the plume five days earlier than the VAAC prediction, which is a significant modification for decision-making such as airspace closures.

**Figure 6.** Fallout time of characterized distal ash from Grímsvötn (GRI), in comparison with the VAAC model. In addition, a model (GRI unsieved) where the unsieved ash density (Table 1) is kept constant is compared here. Atmospheric data at different altitudes are interpolated from the US Standard Atmosphere (NASA, 1976).

A direct impact of the changed relationship between fall velocity and size is a change in the measurement of particle-size distribution based on the Doppler effect (Bonadonna et al., 2011). A 40% difference in attributed fall velocity could lead to a two-fold difference in the PSD. Satellite retrievals of ash using infrared measurements will also be impacted by improved estimates of density as the estimate of mass loading is a linear function of density. For example, A. Prata et al. (2022) used a density of 2.3 g cm\(^{-3}\) to estimate mass loading for the 2019 Raikoke eruption. Measurements of airfall ash give a
SiO\textsubscript{2} content of \textasciitilde50\% (Smirnov et al., 2021) implying an ash density from Equation 6 of 2.74 g cm\textsuperscript{-3}, i.e. a 18\% difference in the estimate of mass loading.

6 CONCLUSION

Density measurements of ash particles with nitrogen gas pycnometry have revealed a notable deviation from previous models. Measured density decreases for larger particle due to increased closed pores. However, this decrease takes place prominently only for diameter greater than 100 \(\mu\)m, before which the density remains constant at the DRE value. In the basaltic ash range studied, this behaviour leads to a settling velocity deviation of up to 25\% from the current VAAC constant-density model, and up to 40\% from other previous models, demonstrating the importance of characterizing ash density in dispersion forecasts and other velocity-sensitive tasks.

7 Open Research

The density measurement data are available in the submitted supplementary materials.

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