

Comminution-induced Transient Frictional Behavior in Sheared Granular Halite

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Abstract

Drastic grain comminution is frequently observed in upper-crust faults and large rock avalanche deposits. Here we report our model experiments to elucidate the possible role of grain comminution in dry granular friction. We sheared halite (NaCl) grains with a ring-shear configuration at a constant slip rate under various normal stresses and investigated the post-slip structures of the experimental fault zones using micro X-ray computed tomography. Consequently, distinct frictional behaviors were observed: a constant friction regime at small slip displacements and a frictional weakening regime at large displacements. The characteristic slip lengths for the two regimes decreased with increasing normal stress and were characterized by approximately the same exponent, regardless of the initial grain size. We developed a theoretical model that considered the production, saturation, and overflow of fine particles in the shear zone and successfully reproduced the transient frictional behavior in the experiments.

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1 **Comminution-induced Transient Frictional Behavior in Sheared Granular Halite**

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12
13 **Key Points:**

- 14 • Sheared granular halite exhibits constant friction at small slip displacements and
15 substantial weakening at large displacements.
- 16 • Characteristic slip lengths for constant friction and weakening decrease with normal
17 stress and are characterized by similar exponents.
- 18 • The production, saturation, and overflow of fine particles in the shear zone are key
19 factors determining transient frictional behavior.

20

21 **Abstract**

22 Drastic grain comminution is frequently observed in upper-crust faults and large rock
23 avalanche deposits. Here we report our model experiments to elucidate the possible role of grain
24 comminution in dry granular friction. We sheared halite (NaCl) grains with a ring-shear
25 configuration at a constant slip rate under various normal stresses and investigated the post-slip
26 structures of the experimental fault zones using micro X-ray computed tomography.
27 Consequently, distinct frictional behaviors were observed: a constant friction regime at small slip
28 displacements and a frictional weakening regime at large displacements. The characteristic slip
29 lengths for the two regimes decreased with increasing normal stress and were characterized by
30 approximately the same exponent, regardless of the initial grain size. We developed a theoretical
31 model that considered the production, saturation, and overflow of fine particles in the shear zone
32 and successfully reproduced the transient frictional behavior in the experiments.

33

34 **Plain Language Summary**

35 Grain comminution and structural evolution are common in natural settings, including
36 earthquake faults and landslides. However, their role in granular friction remains poorly
37 understood. We experimentally sheared breakable NaCl grains to simulate the processes in the
38 growing fault zones and visualized their microstructures using micro- X-ray computed
39 tomography (CT). Two distinct frictional behaviors were observed: a constant regime showing a
40 high friction coefficient at small slip displacements, and a weakening regime with a substantial
41 drop in friction at large slip displacements. The characteristic slip lengths for the two regimes
42 decrease with increasing normal stress. Micro-observations revealed fine particles and extremely

43 localized shear planes. It was inferred that the frictional evolution was characterized by grain
44 comminution mechanisms that continuously produce fine particles. Fine particles with low
45 rolling friction serve as the interstitial granular fluid and accumulated in the porous medium once
46 the shear started. The constant regime was dominated by sliding friction between large grains
47 and terminated when the comminuted fine particles fully saturated the shear zone. Subsequently,
48 the overflow of fine particles led to weakening by decreasing the effective normal stress between
49 the large grains. We describe these processes using a simple theoretical model and reproduce the
50 frictional behaviors.

51

52 **1 Introduction**

53 The constitutive properties and frictional behavior of faults are key factors in
54 understanding diverse faulting processes. Many experimental studies have been conducted using
55 various configurations such as double direct shear (e.g., Dieterich, 1972; 1978), rotary shear
56 (e.g., Weeks and Tullis, 1985; Tsutsumi and Shimamoto, 1997), triaxial loading (e.g., von
57 Kármán, 1911; Brace and Byerlee, 1966; Shimamoto et al., 1980), and large-scale biaxial friction
58 (e.g., Dieterich, 1981; Yamashita et al., 2015; McLaskey and Yamashita, 2017). In these
59 experimental studies, the shear zone thickness was in the order of several millimeters and could
60 not increase owing to restricted slip displacement or gouge confinement. In contrast, the gouge
61 thickness in natural faults is usually much greater than that in experimental faults (e.g., Engelder,
62 1974; Robertson 1982; Scholz, 1987; Chambon et al., 2006) and the energy dissipation and
63 rupture processes within a thick layer differ from those at a distinct interface (Sibson, 2003).
64 Furthermore, while most experimental configurations include gouges sandwiched between

65 consolidated host rocks, few studies have investigated the effects of unconsolidated and highly
66 porous rocks and sediments, which are frequently involved in upper crust fault (e.g., Chester and
67 Logan, 1986; Faulkner et al., 2010) and subduction zones (e.g., Polet and Kanamori, 2000;
68 Kitajima and Saffer, 2014).

69 The cataclastic process is active in faulting processes and stimulates intense fracturing
70 and crushing of grains (e.g., Borg et al., 1960; Griggs and Handin, 1960; Engelder, 1974; Kimura
71 et al., 2007; Fossen, 2010). Apart from earthquake faults, large rock avalanches are another
72 significant geophysical phenomenon that often exhibit thick deposits accompanied by extreme
73 grain size reduction (e.g., Heim, 1932; Davies et al., 1999; Davies and McSaveney, 2002, 2009;
74 Crosta et al., 2007) and results in large runouts (e.g., Heim, 1932; Hsü, 1975; Davies, 1982;
75 Davies et al., 1999; Legros, 2002). Although their geometries, boundary conditions, and stress
76 levels differ significantly from those of earthquake faults, shearing of dense granular flow is
77 common (e.g., Siman-Tov and Brodsky, 2018), and the fine particles produced are considered to
78 play an important role in the friction of the fault zone.

79 In this study, we aim to elucidate the mechanisms of grain comminution and structural
80 evolution in a growing fault zone that developed in an unconsolidated and porous granular
81 medium. Friction experiments were performed using a ring shear apparatus (Sassa et al., 2004)
82 and a large volume of breakable grains. Halite (NaCl) has been frequently used as an analog for
83 fault gouges because it reveals a wide variety of deformation mechanisms (e.g., Shimamoto,
84 1986; Hiraga and Shimamoto, 1987; Bos and Spiers, 2002; Kim et al., 2010; Noda and
85 Shimamoto, 2010, 2012; Buijze et al., 2017) and is suitable for experimentally studying the
86 frictional properties of grain comminution in faults. Notably, large and thick experimental fault
87 zone was observed within the granular medium, as discussed in this paper. We then followed the

88 key mechanisms of grain comminution by combining frictional measurements, post-slip
89 structural observations, and data analyses. Finally, we propose a theoretical model for the
90 saturation and overflow of comminuted fine particles to interpret and reproduce our
91 observations.

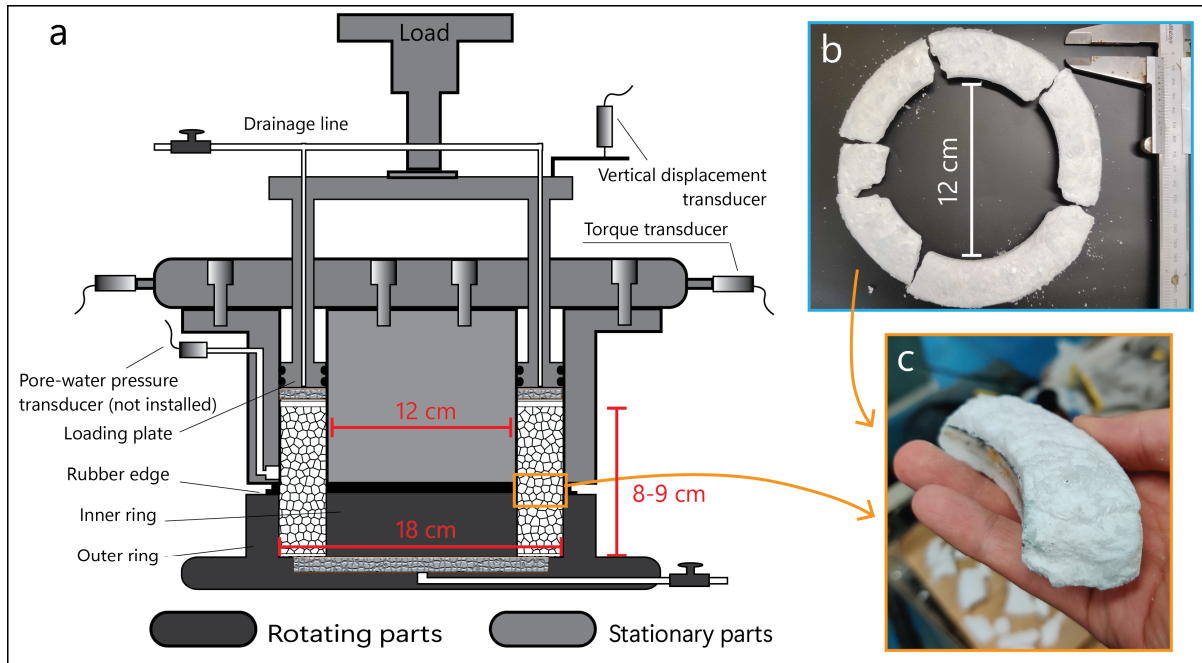
92

93 **2 Materials and Methods**

94 Angular-shaped granular halite (NaCl) with two different initial sizes, namely coarse-
95 grained halite (~2-5 mm) and fine-grained halite (~0.425-0.85 mm), were used as model granular
96 materials.

97 The experimental setup is schematically shown in Figure 1a. The ring-shear apparatus
98 has previously been used in the studies of landslide behavior (e.g., Sassa and Lee, 1993; Sassa et
99 al., 1996; 2004). Detailed specifications are outlined by Sassa et al. (2004). In each test,
100 approximately 1.5 kg of granular halite were evenly distributed in a ring-shear box (outer and
101 inner diameters of 18 and 12 cm, respectively, with a 10.9 cm maximum sample height). The
102 upper shear box was stationary, while the lower shear box was spinning. The rubber edges were
103 glued to the lower shear box separation to prevent grain leakage. The halite samples were
104 sheared at a constant slip rate of 0.05 cm/s under three levels of normal stress: 0.2, 0.6, and 1.0
105 MPa. All experiments were completed in room-dry conditions (humidity ~50%) at 24°C. We
106 applied 2 m slip displacement (Table S1 in the Supporting Information) unless otherwise noted.
107 After each test, we carefully took out blocks from the shear zone. The shear-zone samples were
108 cohesive and hard, as shown in Figures 1b and 1c. Post-experiment structural analyses of the
109 halite fault zone were performed for three baseline runs in coarse-grained media using high-

110 resolution micro X-ray CT (Versa XRM-500 X-ray microscope). More details are provided in
 111 the “Expanded Methods” section and Table S1 in the Supporting Information.



112
 113 **Figure 1. Ring-shear configuration and shear zones after testing.** (a) Schematic of Ring-shear
 114 apparatus. (b) Top view of shear zone blocks for coarse-grained medium. (c) A shear zone block
 115 of coarse-grained medium.

116

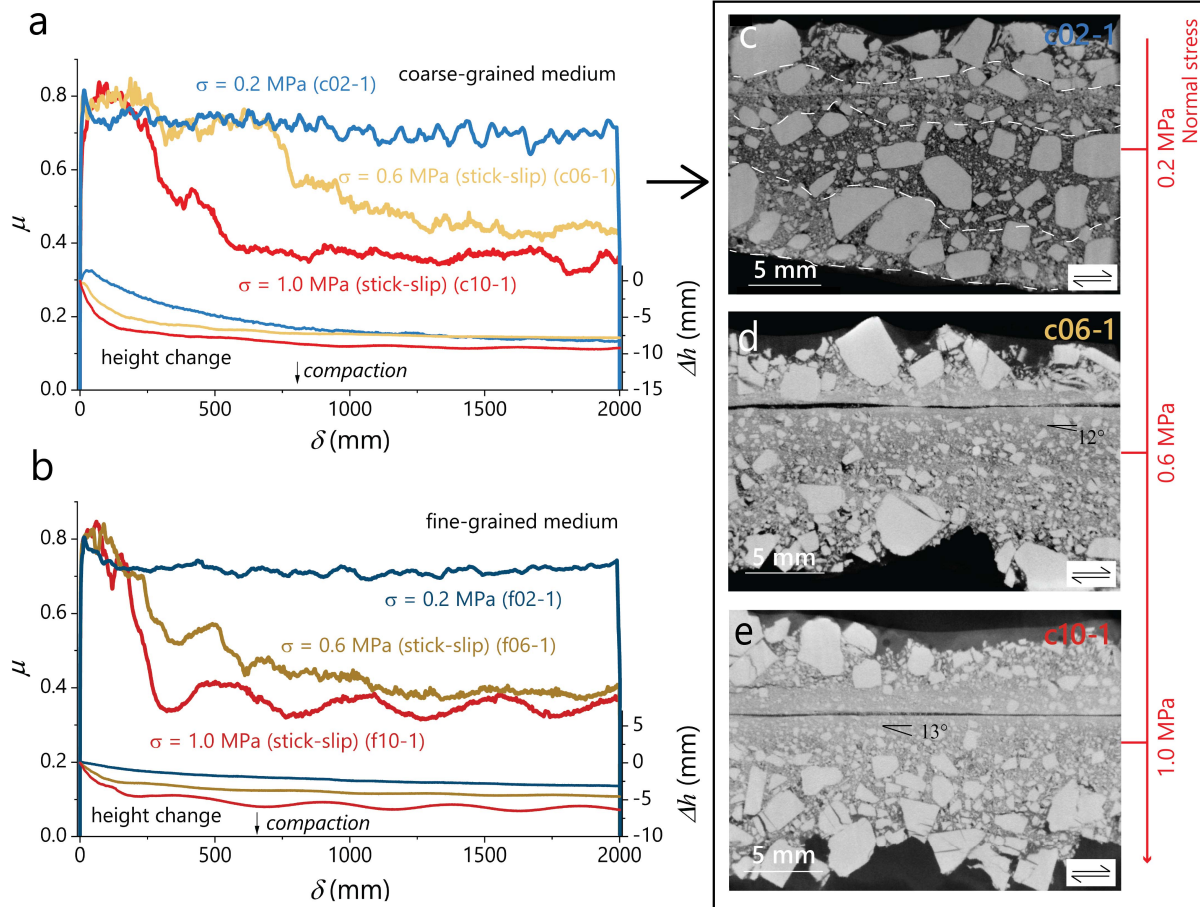
117 3 Results

118 3.1 Frictional behavior

119 Figure 2 shows representative frictional behavior and micro X-ray CT observations. We
 120 used the moving average to smooth the data and emphasize the transient frictional behavior, as
 121 shown in Figures 2a (coarse-grained medium) and 2b (fine-grained medium). A comparison of
 122 raw and processed data is provided in the Supporting Information (Figure S1). Here, we present
 123 the evolution of the friction coefficient (μ) and sample height change (Δh) against the slip

124 displacement (δ). As shown in Figure 2a, all samples showed an increase in friction in the initial
125 loading stage. For the experimental run performed under the lowest normal stress ($\sigma = 0.2$ MPa),
126 the friction coefficient reached its peak and then remained at $\mu \approx 0.7$ until the test ended. The
127 sample exhibited dilation and switched to continuous compaction after reaching the peak
128 friction. In contrast, under intermediate normal stress ($\sigma = 0.6$ MPa), the friction started to
129 weaken at a slip displacement of approximately 660 mm. Finally, substantial weakening was
130 observed at a steady-state value $\mu \approx 0.43$. In addition, the height change indicated compaction
131 during the initial phase. Under maximum normal stress ($\sigma = 1.0$ MPa), the friction remained
132 relatively stable for a small displacement of ~ 200 mm. Rapid weakening was then initiated, and
133 friction evolved to a significantly lower value of $\mu \approx 0.36$. The results of the fine-grained media
134 are also shown in Figure 2b and are comparable to those of the coarse-grained media. The total
135 change in height in the fine-grained medium was smaller than that in the coarse-grained medium.

136 Notably, substantial weakening occurred at small displacements when the normal stress
137 was high, indicating that the evolution of friction was dependent on the normal stress. To
138 observe frictional weakening under the lowest normal stress (0.2 MPa), we conducted friction
139 experiments at large slip displacements (Figure S2 in Supporting Information). Consequently,
140 weakening occurred after a significantly large slip displacement of ~ 7 m in the coarse-grained
141 medium and ~ 5 m in the fine-grained medium.



142

143 **Figure 2. Representative frictional behaviors and micro-CT images.** Frictional behaviors in
 144 coarse-grained (a) and fine-grained (b) media. Friction coefficient and height change plotted
 145 against slip displacement under different normal stresses. Cross sections of shear zone from
 146 experimental run after 2 m slip displacement, under (c) 0.2 MPa, (d) 0.6 MPa, and (e) 1.0 MPa.

147

148 3.2 Microstructures

149 Micro X-ray cross-sectional images (parallel to the shear direction) after 2 m slip
 150 displacement in the coarse-grained medium are shown in Figures 2c, 2d, and 2e. Drastic
 151 comminution processes were also observed. Many fine particles accumulated within a broad

152 domain, and their size was smaller than tens of microns, which is beyond the scanning
153 resolution.

154 For the samples under 0.2 MPa, bright areas with a high density (circled with dashed
155 lines) were observed, and the shear zone suggested characteristics of cataclasis between the
156 bright and dense areas, as shown in Figure 2c. Although some voids were observed between the
157 large grains, the large grains were loosely surrounded by comminuted fine particles.

158 The structures of the samples under large normal stress were significantly different, in
159 which the progressive production of fine particles and well-developed shear planes were
160 observed (Figures 2d and 2e). The shear planes were considerably flat with mild waviness. An
161 evident shear texture was observed, with grain alignments of approximately 12-13°. A small
162 number of fine particles remained in the gap between the slip surfaces, suggesting the local
163 detachment of the upper and lower surfaces during motion. Generally, grains near the shear
164 planes were intensively comminuted and densely compacted, whereas some large grains
165 remained intact along the sliding surface.

166

167 **4 Discussion**

168 **4.1 Data analysis**

169 Two distinct frictional behaviors were identified in our experimental observations. A
170 similar observation consisting of two regimes for crushable materials was reported by Hu et al.
171 (2022). In Figure 3a, we describe our simple model, which comprises an initial constant regime
172 and a weakening regime against slip displacement. Frictional evolution $\mu(\delta)$ is given by the
173 following equation:

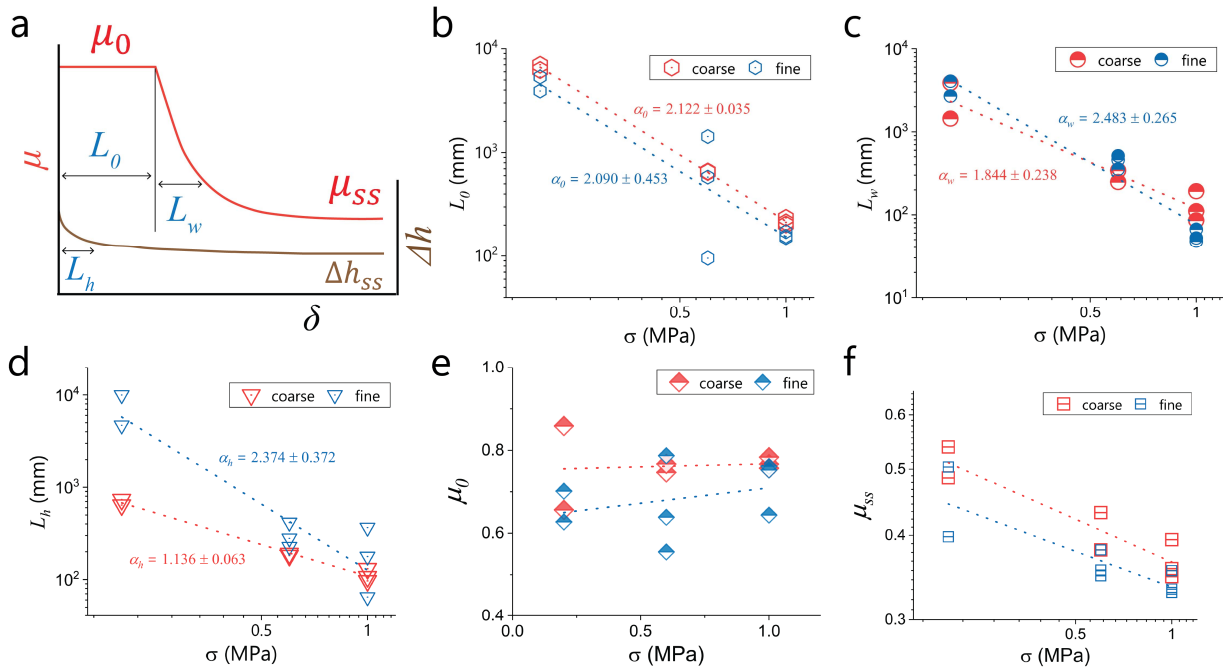
$$\mu(\delta) = \begin{cases} \mu_0, & \delta < L_0 \\ (\mu_0 - \mu_{ss}) \exp\left(-\frac{\delta - L_0}{L_w}\right) + \mu_{ss}, & \delta \geq L_0 \end{cases} \quad (1)$$

174 where μ_0 and μ_{ss} are the coefficients of friction in the initial and steady states, respectively, and
 175 L_0 and L_w are the characteristic slip lengths for the constant and weakening regimes,
 176 respectively.

177 Similarly, the equation for height change $\Delta h(\delta)$ is given by:

$$\Delta h(\delta) = \Delta h_{ss} \left[1 - \exp\left(-\frac{\delta}{L_h}\right) \right], \quad (2)$$

178 where Δh_{ss} refers to the steady-state value of the height change, and L_h scales the characteristic
 179 length for the height decay.



180

181 **Figure 3. Effects of normal stress on characteristic slip lengths and frictional parameters.**

182 (a) Fitting of a frictional curve. The characteristic slip lengths for (b) the constant regime, (c)

183 weakening regime, and (d) height change against normal stress. (e) Constant friction coefficient
184 and (f) Steady-state friction coefficient against normal stress.

185

186 The parameters in Equations (1) and (2) were estimated using nonlinear least-squares
187 fitting (Table S1). The characteristic lengths L_0 , L_w , and L_h were plotted against normal stress σ
188 in Figures 3b, 3c, and 3d, respectively. They are all anticorrelated to σ . We obtained $L_0 \sim \sigma^{-\alpha_0}$,
189 $L_w = \sigma^{-\alpha_w}$ and $L_h \sim \sigma^{-\alpha_h}$, where α_0 , α_w , and α_h are constants. $\alpha_0 \approx 2$ and $\alpha_w \approx 2$ were
190 approximately obtained from the fitting, regardless of the initial grain sizes. In contrast, α_h
191 exhibited large variability based on the grain size.

192 In addition, μ_0 is independent of σ , as shown in Figure 3e. This agrees with Byerlee's or
193 Coulomb-Amonton's law of friction. In contrast, μ_{SS} decreased with increasing σ , as seen in
194 Figure 3f, suggesting that the two regimes are governed by different physical processes. μ_{SS} was
195 generally lower in the fine-grained medium than in the coarse-grained medium. Note that some
196 strengthening occurred at large slip displacements only under low-normal-stress conditions (e.g.,
197 run f02-2 in Figure S2). The experiments were conducted under room-dry conditions. Because
198 NaCl is sensitive to moisture, moisture may assist in cohesion among grains, especially during
199 significant grain size reduction. Additionally, cementation in the resultant shear zone blocks (see
200 Figures 1b and 1c) may work similarly, which provides interesting topics for future studies.

201 **4.2 Theoretical modeling**

202 One outstanding characteristic of our experiments was that during grain comminution,
203 many fine particles were produced in situ, filling the voids. The comminution rate was high
204 when the normal stress was large. The initial large friction was due to large angular grains, and

205 steady-state friction was dominated by the friction of rounded fine particles, as spherical grains
 206 tend to have significantly low friction (e.g., Mair et al., 2002; Salerno et al., 2018). To
 207 understand the observed behavior and reproduce its characteristic features, we developed a
 208 theoretical model.

209 First, we considered the slip-displacement-dependent evolution of friction as follows:

$$\mu(\delta) = \frac{\sigma_{eff}(\delta)}{\sigma} \mu_0 + \left(1 - \frac{\sigma_{eff}(\delta)}{\sigma}\right) \mu_{ss}, \quad (3)$$

210 where μ_0 is the friction coefficient for the constant regime and is dominated by sliding friction of
 211 angular-shaped large grains, and μ_{ss} is the steady-state friction coefficient due to the rolling
 212 friction of rounded fine particles. $\sigma_{eff}(\delta)$ denotes the effective normal stress supported by large
 213 grains, which is considered equal to the applied normal stress σ in the early stage and decreases
 214 to zero with the progressive production of fine particles.

215 Subsequently, we introduce a wear process to consider the fine particles produced. To
 216 describe the wear process, we applied Archard's adhesion wear theory in tribology (Archard,
 217 1953). In Archard's theory, wear volume Q is proportional to applied normal force F_N and

$$Q(\delta) = C \frac{F_N}{\sigma_Y} \delta, \quad (4)$$

218 sliding distance δ as:

219 where C is a dimensionless constant and σ_Y is the yield strength of the frictional material.

220 Archard assumed that the real contact area was formed by plastic deformation of the asperities.

221 The yield strength σ_Y of halite is $\sim 10\text{-}30$ MPa at room temperature (Picard et al., 2018), and its

222 plastic deformation is significant in our experiments. Since F_N can be expressed by $F_N = A_0 \sigma$,

223 where A_0 and σ are the nominal area of the ring-shaped shear zone and normal stress,
 224 respectively, Equation (4) can be re-written as the following formula:

$$Q(\delta) = CA_0 \frac{\sigma}{\sigma_Y} \delta, \quad (5)$$

225 For a granular medium, we assumed that the slip was evenly accommodated in multiple (N)
 226 layers within the shear zone. Thus, the real contact area becomes N times that of a single layer,
 227 and the slip in each layer is given by δ/N . In addition, we consider the effective normal stress
 228 for large grains and replace σ with σ_{eff} . Thus, Equation (5) can be expressed as:

$$Q(\delta) = CNA_0 \frac{\sigma_{eff}}{\sigma_Y} \frac{\delta}{N} = CA_0 \frac{\sigma_{eff}}{\sigma_Y} \delta. \quad (6)$$

229 Equation (6) is a smooth extension of Archard's equation for granular systems. Furthermore, we
 230 modified Equation (6) to fit our experimental data as follows:

$$Q(\delta) = CA_0 \left(\frac{\sigma_{eff}}{\sigma_Y} \right)^\alpha \delta. \quad (7)$$

231 Note Equation (7) recovers the original Archard's theory when $\alpha = 1$.

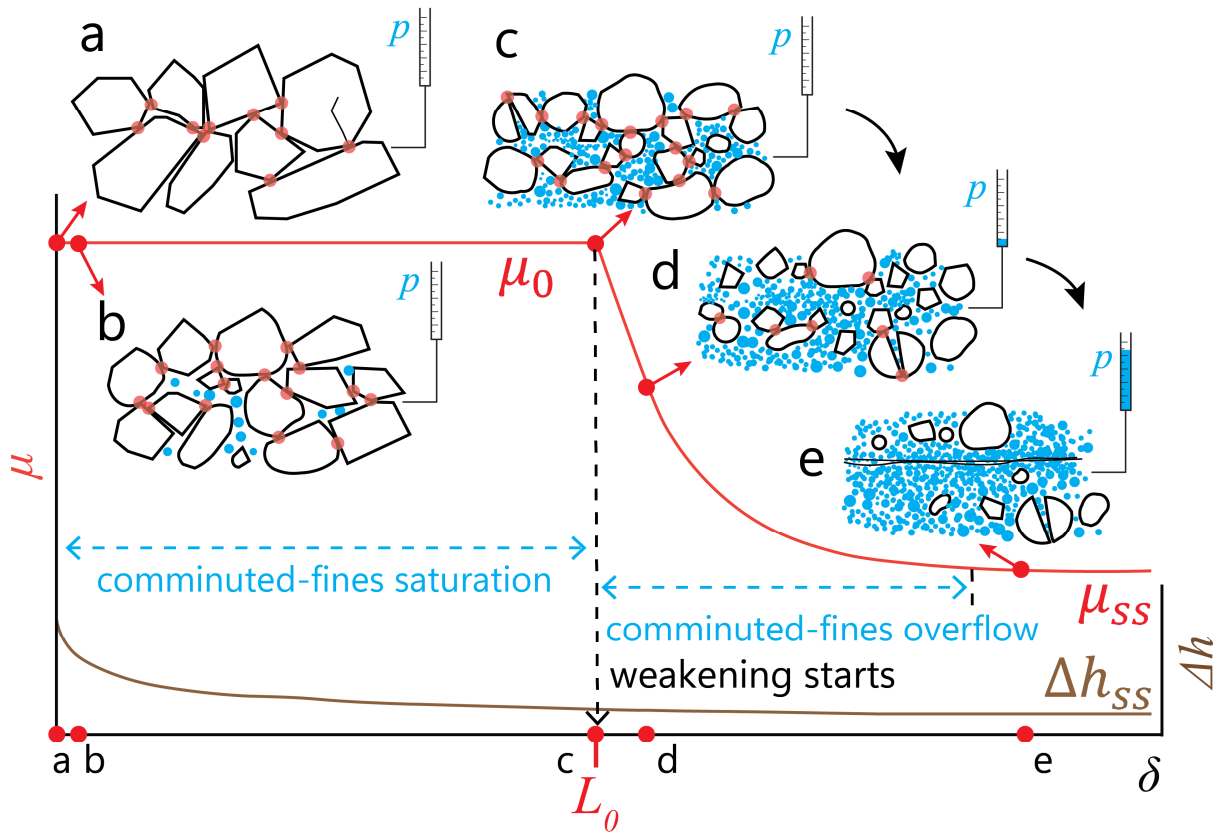
232 Next, we inferred that the comminuted fine particles accumulated in the voids between
 233 large grains during shearing (see Figure 4). Assume that the large grains were closely compacted
 234 as a porous medium (Figure 4a) with a constant packing fraction ϕ , within a shear zone of a
 235 given thickness, we have:

$$V_{void} = \frac{1-\phi}{\phi} V_{grain}, \quad (8)$$

236 and

$$V_{total} = \frac{1}{\phi} V_{grain}, \quad (9)$$

237 where V_{grain} , V_{void} , and $V_{total} = V_{grain} + V_{void}$ denote the grain, void, and bulk volumes,
 238 respectively, within a predefined shear zone.



239
 240 **Figure 4. Weakening mechanisms.** (a) Angular grains are compacted initially (red circles
 241 denote contacts between large grains) with zero pseudo fluid pressure ($p = \sigma - \sigma_{eff}$). (b)
 242 Intensive comminution starts once shear is imposed. (c) During shearing, angular large grains
 243 generate fine particles, which fill the voids between large grains at L_0 . (d) Fine particles are
 244 continuously generated by grain comminution, overflow the shear zone, and decrease the
 245 effective normal stress between large grains. (e) Large grains are completely separated, and an
 246 extremely localized fine particle layer is formed.

247

248 The comminution of large grains was immediately initiated as shearing started (Figure
 249 4b), and fine particles continued to accumulate in the voids within the shear zone until the
 250 comminuted fine particles saturated the entire shear zone (Figure 4c) at $\delta = L_0$. The saturation
 251 condition can be described by the balance between the void and wear volumes and by
 252 approximating the volume fraction of the fine grains by the same value ϕ :

$$\frac{1}{\phi} Q(L_0) = \frac{1-\phi}{\phi} (V_{grain,0} - Q(L_0)). \quad (10)$$

253 where $V_{grain,0}$ is the initial volume of large grains. Using Equations (9) and (10), $Q(L_0)$ can be
 254 written as

$$Q(L_0) = \frac{\phi(1-\phi)}{2-\phi} A_0 h_0, \quad (11)$$

255 where h_0 denotes the initial height of the sample. By substituting Equation (7) into Equation (11)
 256 and $\sigma_{eff} = \sigma$ in this constant regime, L_0 is obtained as:

$$L_0 = \frac{h_0 \phi(1-\phi)}{c} \left(\frac{\sigma}{\sigma_Y} \right)^{-\alpha}. \quad (12)$$

257 This result is consistent with our experimental results: $L_0 \sim \sigma^{-2}$ for $\alpha = 2$. The effect of initial
 258 grain size seems to be small, as shown in Figure 3b. The two media may have different
 259 characteristic shear-zone thicknesses, which may be defined by the shear-box dimensions, initial
 260 grain size, and normal stress. This may explain why the y-intercept yields a difference of
 261 approximately 40% (Figure 3b). Therefore, the characteristic thickness of the shear zone was
 262 postulated, and the motion of the fine particles was confined to this region. To simplify our
 263 analysis, we neglected dynamic effects, such as the loss of fine particles from the shear zone.

264 In addition, assuming that the sample compaction during shear can be attributed to height
 265 decay in the shear zone,

$$V_{total}(\delta) = A_0 \Delta h(\delta) = \frac{1}{\phi} (V_{grain,0} - Q(\delta)). \quad (13)$$

266 $\Delta h(\delta)$ is expressed as:

$$\Delta h(\delta) = -\frac{c}{\phi} \left(\frac{\sigma}{\sigma_Y} \right)^\alpha \delta. \quad (14)$$

267 We analyzed the dependence of $\Delta h(\delta)$ on normal stress σ and particle size d by estimating the
268 initial height decay slope $\left. \frac{d\Delta h}{d\delta} \right|_{\delta=0} = -\Delta h_{ss}/L_h$ (Figure S3 in the Supporting Information).

269 $-\Delta h_{ss}/L_h$ appear to be proportional to σ^2 and $d^{0.3}$, which also realizes $\alpha = 2$ in Equation (14).

270 After saturation of fine particles in the shear zone, weakening started at $\delta = L_0$. We
271 assumed that the comminution mechanism operated continuously and that the effective normal
272 stress σ_{eff} decreased linearly with the wear volume, as follows:

$$\frac{dQ(\delta)}{d\delta} = \alpha - \beta Q(\delta), \quad \delta > L_0 \quad (15)$$

273 where α and β are constants. At the weakening point where saturation occurs, $Q = Q(L_0)$ and
274 $\sigma_{eff} = \sigma$ are satisfied. Assume that the wear volume Q is m times $Q(L_0)$, namely $Q = mQ(L_0)$,
275 when a steady state is achieved ($\frac{dQ}{d\delta} = 0$ and $\sigma_{eff} = 0$). Substituting Equation (15) into the
276 differential form of Equation (7), we obtain:

$$\frac{dQ(\delta)}{d\delta} = \frac{CA_0}{m-1} \left(\frac{\sigma}{\sigma_Y} \right)^\alpha \left(m - \frac{Q(\delta)}{Q(L_0)} \right). \quad (16)$$

277 Integration leads to:

$$\ln\left(\frac{m - \frac{Q(\delta)}{Q(L_0)}}{m - 1}\right) = -\frac{CA_0}{(m-1)Q(L_0)}\left(\frac{\sigma}{\sigma_Y}\right)^\alpha (\delta - L_0), \quad \delta > L_0. \quad (17)$$

278 By substituting Equations (7) and (16) into Equation (17), we obtain:

$$\frac{\sigma_{eff}(\delta)}{\sigma} = \exp\left[-\frac{\delta - L_0}{\alpha(m-1)L_0}\right], \quad \delta > L_0. \quad (18)$$

279 By substituting Equation (18) into Equation (3), we obtain:

$$\mu(\delta) = \mu_{ss} + (\mu_0 - \mu_{ss})\exp\left[-\frac{\delta - L_0}{\alpha(m-1)L_0}\right], \quad \delta > L_0. \quad (19)$$

280 The characteristic length $L_w = \alpha(m-1)L_0$ is hitherto realized for the weakening regime. Using
281 Equation (12), we obtain:

$$L_w = \alpha(m-1)\frac{h_0}{C}\frac{\phi(1-\phi)}{2-\phi}\left(\frac{\sigma}{\sigma_Y}\right)^{-\alpha}. \quad (20)$$

282 We compared our theoretical calculations with the experimental results; the exponent $\alpha = 2$ is
283 again obtained, and $L_w \approx 0.5L_0$ (see Table S1) is recovered when $m = 5/4$.

284 The deviation of the exponent α ($= 2$ in our experiments) from the original Archard
285 theory ($= 1$) is not clear at this time. More detailed analyses are required in future studies.

286

287 **4.3 Shear localization mechanisms**

288 The above-mentioned model theoretically represents the normal stress-dependent
289 weakening behavior determined by grain comminution mechanisms. However, describing the
290 shear localization observed in the microstructures is insufficient. The microstructure revealed by
291 the micro-CT scan, shown in Figures 2c, 2d, and 2e, is similar to that observed in faults (e.g.,

292 Chester and Logan, 1986; Chester and Chester, 1998; Jefferies et al., 2006; Heilbronner and
293 Keulen, 2006) and rock avalanche deposits (e.g., Davies et al., 1999; Crosta et al., 2007;
294 McSaveney and Davies, 2007; Perinotto et al., 2015), in which layers of comminuted particles of
295 various sizes and shapes are heterogeneously distributed in the shear zone.

296 One possible explanation is that while the sliding of large grains was initially distributed
297 within the characteristic shear zone, a localized region developed near the shear box separation
298 after the shear zone was saturated and compacted. The grains within this narrow domain undergo
299 intensive comminution. This positive feedback enhances the localization and results in an
300 extremely localized shear plane within the thin layer of fine grains, as shown in Figure 4e.

301 Another explanation is the grain segregation mechanism, which leads to characteristic
302 textures such as inverse grading in rock avalanche deposits (e.g., Dunning, 2006; Crosta et al.,
303 2007; Dufresne et al., 2016) and natural and experimental fault zones (Boullier et al., 2009; Ujiie
304 and Tsutsumi, 2010). Siman-Tov and Brodsky (2018) reported gravity-independent segregation
305 in experimental granular flows, where fine particles migrated symmetrically away from the
306 source and affected the velocity structure. Based on the CT images, the dense upper layer and
307 immature shear plane suggested upward migration (Figure 2c). The thick lower half of the shear
308 zone suggests the role of the gravity-induced void-filling mechanism, possibly enhanced by
309 stick-slip motions, where fine particles preferentially fall into the voids, as shown in Figures 2c,
310 2d, and 2e. Therefore, in situ comminuted fine particles can segregate from the source region and
311 stabilize subsequent flow, which also leads to shear localization, as illustrated in Figure 4e. The
312 migration of fine particles was likely dominated by the characteristic thickness, resulting in hard
313 shear zone blocks within the granular medium (Figures 1b and 1c).

314

315 **5 Conclusions**

316 Friction experiments were performed on granular halite using a ring shear apparatus. We
317 found that grain comminution was a key mechanism for determining the frictional behavior of a
318 sheared granular system involving breakable grains. We proposed a simple mechanism for grain
319 comminution: the generated fine particles gradually saturate the porous shear zone of the
320 granular medium in a constant friction regime, and the overflow of fine particles leads to
321 frictional weakening owing to the decrease in the effective normal stress between large grains
322 and the interstitial flow of fine particles. In addition, we found that the intrinsic comminution and
323 microstructure are similar to those of natural fault zones and rock avalanche deposits, suggesting
324 their relevance and important implications for natural shear zones.

325 However, several problems remain unsolved: for instance, in situ observations of
326 comminution behavior are lacking, and the mechanism responsible for determining the exponent
327 $\alpha = 2$ and description of shear localization dynamics remain unknown. These results will be
328 reported in future studies.

329

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335

336 **Open Research**

337 The complete dataset and fitting code used in this study are available from Zenodo
338 (<https://doi.org/10.5281/zenodo.7898496>). The figures were created using the open-source
339 Python function matplotlib.pyplot, Origin 2023b, and Adobe Illustrator.

340

341 **Author Contributions**

342 Chengrui Chang (CC), Chao Huang (CH) and Yohei Hamada (YH) conducted the
343 experiments. Hiroyuki Noda (HN) and Tetsuo Yamaguchi (TY) developed theoretical models.
344 CC and TY drafted the manuscript. All authors participated in the discussion and review of the
345 documents.

346 **References**

- 347 Archard, J. F. (1953). Contact and Rubbing of Flat Surfaces. *Journal of Applied Physics*,
348 24(8), 981–988. <https://doi.org/10.1063/1.1721448>
- 349 Borg, I., Friedman, M., Handin, J., & Higgs, D. V. (1960). Chapter 6: Experimental
350 Deformation of St. Peter Sand: A Study of Cataclastic Flow. In *Geological Society of*
351 *America Memoirs* (Vol. 79, pp. 133–192). Geological Society of America.
352 <https://doi.org/10.1130/MEM79-p133>
- 353 Bos, B., & Spiers, C. J. (2002). Fluid-assisted Healing Processes in Gouge-bearing Faults:
354 Insights from Experiments on a Rock Analogue System. *Pure and Applied*
355 *Geophysics*, 159(11–12), 2537–2566. <https://doi.org/10.1007/s00024-002-8747-2>
- 356 Boullier, A.-M., Yeh, E.-C., Boutareaud, S., Song, S.-R., & Tsai, C.-H. (2009). Microscale
357 anatomy of the 1999 Chi-Chi earthquake fault zone. *Geochemistry, Geophysics,*
358 *Geosystems*, 10(3), Q03016. <https://doi.org/10.1029/2008GC002252>
- 359 Brace, W. F., & Byerlee, J. D. (1966). Stick-Slip as a Mechanism for Earthquakes. *Science*,
360 153(3739), 990–992. <https://doi.org/10.1126/science.153.3739.990>
- 361 Buijze, L., Niemeijer, A. R., Han, R., Shimamoto, T., & Spiers, C. J. (2017). Friction
362 properties and deformation mechanisms of halite(-mica) gouges from low to high
363 sliding velocities. *Earth and Planetary Science Letters*, 458, 107–119.
364 <https://doi.org/10.1016/j.epsl.2016.09.059>
- 365 Chambon, G., Schmittbuhl, J., Corfdir, A., Orellana, N., Diraison, M., & Géraud, Y. (2006).
366 The thickness of faults: From laboratory experiments to field scale observations.
367 *Tectonophysics*, 426(1–2), 77–94. <https://doi.org/10.1016/j.tecto.2006.02.014>
- 368 Chester, F. M., & Logan, J. M. (1986). Implications for mechanical properties of brittle faults
369 from observations of the Punchbowl fault zone, California. *Pure and Applied*
370 *Geophysics PAGEOPH*, 124(1–2), 79–106. <https://doi.org/10.1007/BF00875720>

- 371 Chester, F. M., & Chester, J. S. (1998). Ultracataclasite structure and friction processes of the
 372 Punchbowl fault, San Andreas system, California. *Tectonophysics*, 295(1–2), 199–
 373 221. [https://doi.org/10.1016/S0040-1951\(98\)00121-8](https://doi.org/10.1016/S0040-1951(98)00121-8)
- 374 Crosta, G. B., Frattini, P., & Fusi, N. (2007). Fragmentation in the Val Pola rock avalanche,
 375 Italian Alps. *Journal of Geophysical Research: Earth Surface*, 112(F1), F01006.
 376 <https://doi.org/10.1029/2005JF000455>
- 377 Davies, T. R., & McSaveney, M. J. (2002). Dynamic simulation of the motion of fragmenting
 378 rock avalanches. *Canadian Geotechnical Journal*, 39(4), 789–798.
 379 <https://doi.org/10.1139/t02-035>
- 380 Davies, T. R., & McSaveney, M. J. (2009). The role of rock fragmentation in the motion of
 381 large landslides. *Engineering Geology*, 109(1–2), 67–79.
 382 <https://doi.org/10.1016/j.enggeo.2008.11.004>
- 383 Davies, T. R., McSaveney, M. J., & Hodgson, K. A. (1999). A fragmentation-spreading
 384 model for long-runout rock avalanches. *Canadian Geotechnical Journal*, 36(6), 1096–
 385 1110. <https://doi.org/10.1139/t99-067>
- 386 Davies, T. R. H. (1982). Spreading of rock avalanche debris by mechanical fluidization. *Rock*
 387 *Mechanics*, 15(1), 9–24. <https://doi.org/10.1007/BF01239474>
- 388 Dieterich, J. H. (1972). Time-dependent friction in rocks. *Journal of Geophysical Research*,
 389 77(20), 3690–3697. <https://doi.org/10.1029/JB077i020p03690>
- 390 Dieterich, J. H. (1978). Time-Dependent Friction and the Mechanics of Stick-Slip. In J. D.
 391 Byerlee & M. Wyss (Eds.), *Rock Friction and Earthquake Prediction* (pp. 790–806).
 392 Basel: Birkhäuser. https://doi.org/10.1007/978-3-0348-7182-2_15
- 393 Dieterich, J. H. (1981). Potential for geophysical experiments in large scale tests.
 394 *Geophysical Research Letters*, 8(7), 653–656.
 395 <https://doi.org/10.1029/GL008i007p00653>

- 396 Dufresne, A., Bösmeier, A., & Prager, C. (2016). Sedimentology of rock avalanche deposits –
 397 Case study and review. *Earth-Science Reviews*, 163, 234–259.
 398 <https://doi.org/10.1016/j.earscirev.2016.10.002>
- 399 Dunning, S. A. (2006). The grain size distribution of rock-avalanche deposits in valley-
 400 confined settings. *Italian Journal of Engineering Geology and Environment*, (2006),
 401 117–121. <https://doi.org/10.4408/IJEGE.2006-01.S-15>
- 402 Engelder, J. T. (1974). Cataclasis and the Generation of Fault Gouge. *Geological Society of*
 403 *America Bulletin*, 85(10), 1515. [https://doi.org/10.1130/0016-
 404 7606\(1974\)85<1515:CATGOF>2.0.CO;2](https://doi.org/10.1130/0016-7606(1974)85<1515:CATGOF>2.0.CO;2)
- 405 Faulkner, D. R., Jackson, C. A. L., Lunn, R. J., Schlische, R. W., Shipton, Z. K., Wibberley,
 406 C. A. J., & Withjack, M. O. (2010). A review of recent developments concerning the
 407 structure, mechanics and fluid flow properties of fault zones. *Journal of Structural*
 408 *Geology*, 32(11), 1557–1575. <https://doi.org/10.1016/j.jsg.2010.06.009>
- 409 Fossen, H. (2010). *Structural Geology*. Cambridge: Cambridge University Press.
 410 <https://doi.org/10.1017/CBO9780511777806>
- 411 Griggs, D., & Handin, J. (1960). Chapter 13: Observations on Fracture and a Hypothesis of
 412 Earthquakes. In *Geological Society of America Memoirs* (Vol. 79, pp. 347–364).
 413 Geological Society of America. <https://doi.org/10.1130/MEM79-p347>
- 414 Heilbronner, R., & Keulen, N. (2006). Grain size and grain shape analysis of fault rocks.
 415 *Tectonophysics*, 427(1–4), 199–216. <https://doi.org/10.1016/j.tecto.2006.05.020>
- 416 Heim, A. (1932). *Bergsturz und Menschenleben*. Zürich: Fretz und Wasmuth, 218.
- 417 Hiraga, H., & Shimamoto, T. (1987). Textures of sheared halite and their implications for the
 418 seismogenic slip of deep faults. *Tectonophysics*, 144(1), 69–86.
 419 [https://doi.org/10.1016/0040-1951\(87\)90009-6](https://doi.org/10.1016/0040-1951(87)90009-6)

- 420 Hsü, K. J. (1975). Catastrophic Debris Streams (Sturzstroms) Generated by Rockfalls.
421 *Geological Society of America Bulletin*, 86(1), 129. [https://doi.org/10.1130/0016-](https://doi.org/10.1130/0016-7606(1975)86<129:CDSSGB>2.0.CO;2)
422 [7606\(1975\)86<129:CDSSGB>2.0.CO;2](https://doi.org/10.1130/0016-7606(1975)86<129:CDSSGB>2.0.CO;2)
- 423 Hu, W., Xu, Q., McSaveney, M., Scaringi, G., Huang, R., Wang, G., et al. (2022). Fluid-Like
424 Behavior of Crushed Rock Flows. *Journal of Geophysical Research: Earth Surface*,
425 127(10). <https://doi.org/10.1029/2021JF006523>
- 426 Jefferies, S. P., Holdsworth, R. E., Shimamoto, T., Takagi, H., Lloyd, G. E., & Spiers, C. J.
427 (2006). Origin and mechanical significance of foliated cataclastic rocks in the cores of
428 crustal-scale faults: Examples from the Median Tectonic Line, Japan. *Journal of*
429 *Geophysical Research: Solid Earth*, 111(B12). <https://doi.org/10.1029/2005JB004205>
- 430 Kim, J.-W., Ree, J.-H., Han, R., & Shimamoto, T. (2010). Experimental evidence for the
431 simultaneous formation of pseudotachylite and mylonite in the brittle regime.
432 *Geology*, 38(12), 1143–1146. <https://doi.org/10.1130/G31593.1>
- 433 Kimura, G., Kitamura, Y., Hashimoto, Y., Yamaguchi, A., Shibata, T., Ujiie, K., & Okamoto,
434 S. (2007). Transition of accretionary wedge structures around the up-dip limit of the
435 seismogenic subduction zone. *Earth and Planetary Science Letters*, 255(3–4), 471–
436 484. <https://doi.org/10.1016/j.epsl.2007.01.005>
- 437 Kitajima, H., & Saffer, D. M. (2014). Consolidation state of incoming sediments to the
438 Nankai Trough subduction zone: Implications for sediment deformation and
439 properties. *Geochemistry, Geophysics, Geosystems*, 15(7), 2821–2839.
440 <https://doi.org/10.1002/2014GC005360>
- 441 Legros, F. (2002). The mobility of long-runout landslides. *Engineering Geology*, 63(3–4),
442 301–331. [https://doi.org/10.1016/S0013-7952\(01\)00090-4](https://doi.org/10.1016/S0013-7952(01)00090-4)

- 443 Mair, K., Frye, K. M., & Marone, C. (2002). Influence of grain characteristics on the friction
444 of granular shear zones. *Journal of Geophysical Research: Solid Earth*, 107(B10),
445 ECV 4-1-ECV 4-9. <https://doi.org/10.1029/2001JB000516>
- 446 Mclasley, G. C., & Yamashita, F. (2017). Slow and fast ruptures on a laboratory fault
447 controlled by loading characteristics. *Journal of Geophysical Research: Solid Earth*,
448 122(5), 3719–3738. <https://doi.org/10.1002/2016JB013681>
- 449 McSaveney, M., & Davies, T. (2007). Rockslides and their motion. In *Progress in Landslide*
450 *Science* (pp. 113–133). Berlin, Heidelberg: Springer. [https://doi.org/10.1007/978-3-](https://doi.org/10.1007/978-3-540-70965-7_8)
451 [540-70965-7_8](https://doi.org/10.1007/978-3-540-70965-7_8)
- 452 Noda, H., & Shimamoto, T. (2010). A rate- and state-dependent ductile flow law of
453 polycrystalline halite under large shear strain and implications for transition to brittle
454 deformation. *Geophysical Research Letters*, 37(9), L09310.
455 <https://doi.org/10.1029/2010GL042512>
- 456 Noda, H., & Shimamoto, T. (2012). Transient behavior and stability analyses of halite shear
457 zones with an empirical rate-and-state friction to flow law. *Journal of Structural*
458 *Geology*, 38, 234–242. <https://doi.org/10.1016/j.jsg.2011.08.012>
- 459 Perinotto, H., Schneider, J., Bachèlery, P., Le Bourdonnec, F., Famin, V., & Michon, L.
460 (2015). The extreme mobility of debris avalanches: A new model of transport
461 mechanism. *Journal of Geophysical Research: Solid Earth*, 120(12), 8110–8119.
462 <https://doi.org/10.1002/2015JB011994>
- 463 Picard, D., Dimanov, A., & Raphanel, J. L. (2018). Plastic behavior of halite single-crystals
464 at different temperatures and strain rates: New insights from in-situ experiments and
465 full field measures. *Materials Science and Engineering: A*, 732, 284–297.
466 <https://doi.org/10.1016/j.msea.2018.07.009>

- 467 Polet, J., & Kanamori, H. (2000). Shallow subduction zone earthquakes and their
468 tsunamigenic potential. *Geophysical Journal International*, 142(3), 684–702.
469 <https://doi.org/10.1046/j.1365-246x.2000.00205.x>
- 470 Robertson, E. C. (1982). Continuous formation of gouge and breccia during fault
471 displacement. In: The 23rd U.S Symposium on Rock Mechanics (USRMS)
- 472 Salerno, K. M., Bolintineanu, D. S., Grest, G. S., Lechman, J. B., Plimpton, S. J., Srivastava,
473 I., & Silbert, L. E. (2018). Effect of shape and friction on the packing and flow of
474 granular materials. *Physical Review E*, 98(5), 050901.
475 <https://doi.org/10.1103/PhysRevE.98.050901>
- 476 Sassa, K., & Lee, J.-H. (1993). Measurement of the apparent friction angle during motion by
477 the high-speed ring shear apparatus. *Landslides*, 30(1), 1-10_1.
478 <https://doi.org/10.3313/jls1964.30.1>
- 479 Sassa, K., Fukuoka, H., Scarascia-Mugnozza, G., & Evans, S. (1996). Earthquake-Induced-
480 Landslides: Distribution, Motion and Mechanisms. *Soils and Foundations*,
481 36(Special), 53–64. https://doi.org/10.3208/sandf.36.Special_53
- 482 Sassa, K., Fukuoka, H., Wang, G., & Ishikawa, N. (2004). Undrained dynamic-loading ring-
483 shear apparatus and its application to landslide dynamics. *Landslides*, 1(1), 7–19.
484 <https://doi.org/10.1007/s10346-003-0004-y>
- 485 Scholz, C. H. (1987). Wear and gouge formation in brittle faulting. *Geology*, 15(6), 493.
486 [https://doi.org/10.1130/0091-7613\(1987\)15<493:WAGFIB>2.0.CO;2](https://doi.org/10.1130/0091-7613(1987)15<493:WAGFIB>2.0.CO;2)
- 487 Shimamoto, T. (1986). Transition between frictional slip and ductile flow for halite shear
488 zones at room temperature. *Science*, 231(4739), 711–714.
489 <https://doi.org/10.1126/science.231.4739.711>
- 490 Shimamoto, T., Handin, J., & Logan, J. M. (1980). Specimen-apparatus interaction during
491 stick-slip in a triaxial compression machine: A decoupled two-degree-of-freedom

- 492 model. *Tectonophysics*, 67(3–4), 175–205. <https://doi.org/10.1016/0040->
493 [1951\(80\)90234-6](https://doi.org/10.1016/0040-1951(80)90234-6)
- 494 Sibson, R. H. (2003). Thickness of the Seismic Slip Zone. *Bulletin of the Seismological*
495 *Society of America*, 93(3), 1169–1178. <https://doi.org/10.1785/0120020061>
- 496 Siman-Tov, S., & Brodsky, E. E. (2018). Gravity-Independent Grain Size Segregation in
497 Experimental Granular Shear Flows as a Mechanism of Layer Formation.
498 *Geophysical Research Letters*, 45(16), 8136–8144.
499 <https://doi.org/10.1029/2018GL078486>
- 500 Tsutsumi, A., & Shimamoto, T. (1997). High-velocity frictional properties of gabbro.
501 *Geophysical Research Letters*, 24(6), 699–702. <https://doi.org/10.1029/97GL00503>
- 502 Ujiie, K., & Tsutsumi, A. (2010). High-velocity frictional properties of clay-rich fault gouge
503 in a megasplay fault zone, Nankai subduction zone. *Geophysical Research Letters*,
504 37(24). <https://doi.org/10.1029/2010GL046002>
- 505 von Kármán. (1911). Festigkeitsversuche unter allseitigem Druck. *Zeitschrift de Vereines*
506 *deutscher Ingenieure*, 55, 1749.
- 507 Weeks, J. D., & Tullis, T. E. (1985). Frictional sliding of dolomite: A variation in constitutive
508 behavior. *Journal of Geophysical Research: Solid Earth*, 90(B9), 7821–7826.
509 <https://doi.org/10.1029/JB090iB09p07821>
- 510 Yamashita, F., Fukuyama, E., Mizoguchi, K., Takizawa, S., Xu, S., & Kawakata, H. (2015).
511 Scale dependence of rock friction at high work rate. *Nature*, 528(7581), 254–257.
512 <https://doi.org/10.1038/nature16138>

513

514 **References from the Supporting Information**

- 515 Kawakata, H., Cho, A., Kiyama, T., Yanagidani, T., Kusunose, K., & Shimada, M. (1999).
516 Three-dimensional observations of faulting process in Westerly granite under uniaxial

517 and triaxial conditions by X-ray CT scan. *Tectonophysics*, 313(3), 293–305.

518 [https://doi.org/10.1016/S0040-1951\(99\)00205-X](https://doi.org/10.1016/S0040-1951(99)00205-X)

519 Raynaud, S., Fabre, D., Mazerolle, F., Geraud, Y., & Latière, H. J. (1989). Analysis of the
520 internal structure of rocks and characterization of mechanical deformation by a non-
521 destructive method: X-ray tomodensitometry. *Tectonophysics*, 159(1–2), 149–159.

522 [https://doi.org/10.1016/0040-1951\(89\)90176-5](https://doi.org/10.1016/0040-1951(89)90176-5)