Solar wind parameters influencing magnetosheath jet formation: low and high IMF cone angle regimes

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Key Points:

- Jet formation is sensitive to SW parameters during high IMF cone angles (quasi-$\perp$), but not during low cone angles (quasi-||)
- Quasi-|| (quasi-$\perp$) jets have an intrinsic size of $\sim 0.3 R_E$ ($\sim 0.1 R_E$) parallel to flow
- Quasi-$\perp$ jet formation is related to shock dynamics amplified by higher $\beta$ and $M_A$

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Abstract
Magnetosheath jets are localized flows of enhanced dynamic pressure that are frequently observed downstream of the Earth’s bow shock. They are significantly more likely to occur downstream of the quasi-parallel shock than the quasi-perpendicular shock. However, as the quasi-perpendicular geometry is a more common configuration at the Earth’s subsolar bow shock, quasi-perpendicular jets comprise a significant fraction of the observed jets. We study the influence of solar wind conditions on jet formation by looking separately at jets during low and high interplanetary magnetic field (IMF) cone angles. According to our results, jet formation commences when Alfvén Mach number $M_A \gtrsim 5$. We find that during low IMF cone angles (downstream of the quasi-parallel shock) other solar wind parameters do not influence jet occurrence. However, during high IMF cone angles (downstream of the quasi-perpendicular shock) jet occurrence is higher during low IMF magnitude, low density, high plasma beta ($\beta$), and high $M_A$ conditions. The distribution of quasi-parallel (quasi-perpendicular) jet sizes parallel to flow peaks at $\sim 0.3 R_E (\sim 0.1 R_E)$. Some quasi-perpendicular jets formed during high $\beta$ and $M_A$ are particularly small. We show examples of quasi-perpendicular shock crossings to better understand the influence of $\beta$ and $M_A$ conditions on jet observations. Our results suggest that jets form as part of the quasi-perpendicular shock dynamics amplified by high solar wind $M_A$ and $\beta$. Such jets seem to be observed in the transition region of the shock, but not deeper in the magnetosheath.

1 Introduction
Magnetosheath jets are dynamic pressure enhancements that sporadically emerge from the Earth’s bow shock and are then observed in the magnetosheath (see the review by Plaschke et al., 2018, and the references therein). These are very common structures as one satellite can observe them many times per hour. Their sizes vary with the largest ones being comparable to the size of the Earth (Plaschke et al., 2016, 2020). Many studies have linked jets to low interplanetary magnetic field (IMF) cone angle (the acute angle between the Sun-Earth line and the magnetic field) conditions (e.g., Archer & Horbury, 2013; Plaschke et al., 2013; Vuorinen et al., 2019; LaMoury et al., 2021). At the subsolar magnetosheath, the cone angle approximates the nominal $\theta_{Bn}$ at the bow shock, as the curvature of the shock is small in this region. Thus, these results imply that jets are most frequent when the subsolar magnetosheath is downstream of a quasi-parallel bow shock region.

This trend in jet occurrence has implications for jet formation mechanisms — namely that they are most likely related to the nature of the quasi-parallel shock and to the presence of the foreshock. For example, foreshock transients such as short large amplitude structures (SLAMS; Schwartz, 1991) or foreshock compressive structures (FCS) in general can pass through the bow shock and be observed as dynamic pressure enhancements in the magnetosheath (Karlsson et al., 2015; Palmroth et al., 2018; Suni et al., 2021). In addition, Hietala et al. (2009) and Hietala and Plaschke (2013) argued that jets can emerge from a rippled quasi-parallel shock surface, when solar wind flowing through a ripple is less decelerated than the flow through the surrounding shock area. Recently, Raptis et al. (2022) showed direct evidence of a jet forming during the reformation process of the quasi-parallel shock, as solar wind was trapped downstream between the old and newly-forming shock surface. A minority of jets can also be attributed to solar wind discontinuities interacting with the Earth’s bow shock (Archer et al., 2012).

A non-negligible fraction of jets do occur during high IMF cone angles downstream of the quasi-perpendicular shock. The quasi-perpendicular geometry is in fact a much more common configuration for the subsolar bow shock (see Figure 1a introduced in Section 2). This results in the number of jets downstream of quasi-parallel and quasi-perpendicular shocks being more comparable in data sets consisting of many years of dayside magne-
tosheath observations (see Figure 1). Interplanetary shocks at 1 AU and planetary bow shocks beyond Earth are also frequently quasi-perpendicular. More attention has been recently paid to these jets in the quasi-perpendicular magnetosheath. Raptis et al. (2020) studied jets (enhancements of total dynamic pressure) in the quasi-perpendicular magnetosheath along with quasi-parallel and boundary jets (between the two regimes). They divided these jets downstream of the quasi-perpendicular shock into two categories: quasi-perpendicular jets and encapsulated jets (jets which look like quasi-parallel jets but are observed in the quasi-perpendicular magnetosheath). They argued that encapsulated jets are most likely formed at the quasi-parallel shock but they travel in the magnetosheath and can later be observed in the quasi-perpendicular region. Raptis et al. (2020) found quasi-perpendicular jets to be shorter in duration and weaker in speed, density, and dynamic pressure. Kajdić et al. (2021) studied total dynamic pressure enhancements in the quasi-perpendicular magnetosheath and reported four different types of events, which resulted in jet-like enhancements: reconnection exhausts, magnetic flux tubes connected to the quasi-parallel shock, mirror-mode waves, and non-reconnecting current sheets. Overall, the knowledge of how quasi-perpendicular jets form is still very poor. While it is believed that at the quasi-parallel shock rippling (Hietala et al., 2009; Hietala & Plaschke, 2013) and shock reformation (Raptis et al., 2020) can lead to jet formation, it is not clear whether these or similar mechanisms can lead to jets also at the quasi-perpendicular shock, where the scales of such processes are typically much smaller.

Understanding how solar wind conditions affect jet formation can help us investigate how they form. The IMF cone angle had long been considered as the only parameter controlling magnetosheath occurrence (e.g., Plaschke et al., 2013). Now that even larger data sets are available, mainly thanks to Time History of Events and Macroscale Interactions during Substorms (THEMIS; Angelopoulos, 2008) and Magnetospheric Multiscale Mission (MMS; Burch et al., 2016) missions’ dayside configurations, this picture is becoming more complicated. Recently, LaMoury et al. (2021) studied separately the solar wind conditions affecting the formation of jets and their ability to propagate to the magnetopause by separating the data into regions close to the bow shock and close to the magnetopause. The subset close to the bow shock can be considered to be dominated by formation effects, while the near-magnetopause subset is also affected by propagation effects. They reported that, in addition to IMF cone angle, the solar wind conditions favorable for jet formation are low IMF strength ($B$), low density ($n$), low dynamic pressure ($P_{\text{dyn}}$), high plasma beta ($\beta$), and high Alfvén Mach number ($M_A$). Koller et al. (2022) studied the occurrence of magnetosheath jets during large-scale solar wind structures. They found that jet occurrence was increased by $\sim 50\%$ during stream-interaction regions and high-speed streams, but decreased by $\sim 50\%$ during coronal mass ejections’ sheath regions and magnetic ejecta. This was attributed to different plasma and magnetic field characteristics of the different large scale structures affecting jet formation. However, Vuorinen et al. (submitted) investigated THEMIS observations over solar cycle 24, and their results suggest that the yearly jet occurrence rates do not change strongly across a solar cycle and are dominated by cone angle effects.

In this paper, we study the solar wind influence on jet formation in more detail. We focus on jets that are generated at the Earth’s bow shock and have a significant earthward velocity component. These jets may have the possibility to impact the magnetopause and consequently perturb the magnetosphere and the ionosphere. In particular, we statistically investigate the two regimes, low and high IMF cone angles, separately, as they are linked to the two well-established distinct shock regimes: quasi-parallel and quasi-perpendicular, respectively. We find that low IMF cone angle jet formation is not controlled by other solar wind parameters, but during high IMF cone angles certain solar wind conditions (e.g., high $M_A$ and $\beta$) are more favorable for jet formation. First, we introduce the data and methods applied in this study. Second, we present the statistical results and show examples of jet observations at multiple quasi-perpendicular shock
crossings of different upstream \( \beta \) and \( M_A \) conditions. Finally, we discuss the implications and caveats followed by the conclusions of this study.

2 Data and Methods

![Figure 1](image_url). Percentages of the THEMIS (a–c) magnetosheath (MSH) observations and (d–f) jet observations in the three different IMF cone angle bins. Panels (g–i) show the average number of observed jets per hour of magnetosheath observations. The left-most column (a,d,g) uses all MSH and jet data, the middle column (b,e,h) includes only data close to the bow shock (\( F \geq 0.5 \)), and the right-most column (c,f,i) only data close to the magnetopause (\( F \leq 0.25 \)).

We investigate subsolar magnetosheath data from the THEMIS probes (Angelopoulos, 2008) from the years 2008–2020. We use data from the Fluxgate Magnetometer (FGM; Auster et al., 2008) and the Electrostatic Analyzer (ESA; McFadden et al., 2008). The statistical data set uses on-board moment data and all observations have been interpolated to a common 1-s cadence. This is a relevant step to note when considering jet durations and comparisons with other missions. This particular THEMIS magnetosheath and jet data set has been created using the algorithm presented by Plaschke et al. (2013) (see their paper for details) and was first used by Koller et al. (2022). It is publicly available (Koller et al., 2021). At the end of this paper, we present a few examples of shock crossings. In these examples, we use THEMIS ground data (available during fast survey mode intervals). We also look at Magnetospheric Multiscale Mission (MMS) spacecraft data of two different bow shock crossings. We use fluxgate magnetometer (Russell et al., 2016) data and burst-resolution Fast Plasma Instrument (FPI; Pollock et al., 2016) ion data. The high cadence of MMS observations allows us to investigate the shock crossings in significantly better temporal detail than THEMIS.

The main jet criterion is that at some point in a magnetosheath jet, the earthward dynamic pressure has to exceed half of the solar wind dynamic pressure. The jet interval is defined as the period when the earthward dynamic pressure in the magnetosheath is larger than one quarter of the solar wind dynamic pressure. Within 1-minute intervals around the jet interval, \( V_X \) (in GSE coordinates) in the magnetosheath has to exceed \( V_X(t_0)/2 \) (\( t_0 \) is the time when the dynamic pressure ratio reaches its peak within the jet). This ensures that jets exhibit an increase in earthward flow speed. Note that this criterion means that not every enhancement of dynamic pressure is considered a jet.
The measurements at \( t_0 \) of each jet represent the jet observations in our statistical study. The solar wind conditions for each of the magnetosheath (and jet) measurements are obtained from the OMNI high-resolution 1-min data set (King & Papitashvili, 2005). However, we apply a running average of the five preceding minutes to obtain a more reliable estimate of the general solar wind conditions at the time of jet formation.

As demonstrated by LaMoury et al. (2021), it is important to disentangle solar wind influence on jet formation and jet propagation. Thus, we only use data from the outermost half of the magnetosheath close to the bow shock. We select the data by assigning each THEMIS observation a relative radial position \( F \) in the magnetosheath (magnetopause at \( F = 0 \) and bow shock at \( F = 1 \))

\[
F = (r - r_{MP})/(r_{BS} - r_{MP})
\]

by applying Shue et al. (1998) magnetopause model and Merka et al. (2005) bow shock model. Here \( r \) is the geocentric distance of the spacecraft. \( r_{BS} \) and \( r_{MP} \) are the geocentric distances of the model bow shock and magnetopause, respectively, measured along the line connecting the spacecraft and the center of the Earth. We use the constraint \( F \in [0.5, 1.1] \), because we want to maximize the number of observations to obtain the best possible statistics. The jet occurrence has not decreased significantly before half-way (\( F = 0.5 \)) through the magnetosheath (not shown here, but can be seen in Figure 1 of LaMoury et al., 2021), implying that propagation effects are not yet significant. There are uncertainties both in the bow shock and magnetopause models and in the OMNI data, which is why we accept values up to \( F = 1.1 \), where the jet occurrence quickly decreases.

In order to study the quasi-parallel and quasi-perpendicular regimes separately, we divide the observations by the IMF cone angle

\[
\alpha = \arccos (|B_X|/|B|) \in [0^\circ, 90^\circ],
\]

where \( B_X \) is the \( X \) component of the magnetic field vector in GSE coordinates. The cone angle distributions of jet and magnetosheath (MSH) observations of the data set are shown in Figure 1 for the whole data set and also separately for observations close to the model bow shock and close to the model magnetopause. Quasi-parallel (quasi-perpendicular) regime is represented by low (high) cone angles \( \leq 30^\circ \) (\( \geq 60^\circ \)). Vuorinen et al. (2019) showed that for these extreme ranges of cone angles, the jet occurrence rates are spatially uniform in the subsolar region. For the intermediate values (30°, 60°), one part of the subsolar magnetosheath is downstream of the quasi-parallel and the other downstream of the quasi-perpendicular shock, and thus the jet occurrence rate varies spatially. To clearly separate these two regimes, we exclude the data with such intermediate cone angles. Figure 1 displays that close to the bow shock, where we are focusing on in this study, 27% of jets in the THEMIS data occurred during low IMF cone angles and 19% occurred during high IMF cone angles. In contrast, only 10% of MSH observations were taken during low IMF cone angle conditions and 53% during high IMF cone angles. This illustrates that jets are much more common during low IMF cone angles, but as high IMF cone angle conditions are more frequent at Earth, quasi-perpendicular jets make up a significant portion of jets in the Earth’s magnetosheath.

We apply Bayes’ theorem

\[
P(\text{jet}|\text{conditions}) = \frac{P(\text{conditions}|\text{jet})P(\text{jet})}{P(\text{conditions})}
\]

to calculate conditional probabilities, i.e., normalized jet occurrence rates under different solar wind conditions. The probabilities on the right-hand side of the equation can be estimated using the observations: \( P(\text{jet}) = N_{\text{jet}}/N_{msh}, \) \( P(\text{conditions}) = N_{msh}(\text{conditions})/N_{msh}, \) and \( P(\text{conditions}|\text{jet}) = N_{\text{jet}}(\text{conditions})/N_{\text{jet}}. \) Thus, the equation becomes

\[
P(\text{jet}|\text{conditions}) = \frac{N_{\text{jet}}(\text{conditions})}{N_{msh}(\text{conditions})}
\]
3 Results

3.1 THEMIS Statistical Results

![Figure 2](image-url)

**Figure 2.** Distributions showing the normalized occurrence rates of jets (jets distribution normalized by the magnetosheath distribution) as functions of OMNI IMF and solar wind parameters: (a) IMF magnitude, (b) speed, (c) density, (d) $\beta$, (e) dynamic pressure, (f) ion temperature, (g) magnetosonic Mach number, (h) Alfvén Mach number, (i) sonic Mach number, (j) fast magnetosonic Mach number, (k) IMF vector standard deviation, and (l) IMF magnitude standard deviation. The distributions are shown separately for observations during low ($[0^\circ, 30^\circ]$; blue) and high IMF cone angles ($[60^\circ, 90^\circ]$; orange). The error bars denote 95% proportional confidence intervals.
In Figure 2, we present the normalized distributions of jet occurrence as a function of the OMNI solar wind parameters. The blue histograms represent low IMF cone angles ($\lesssim 30^\circ$) and the orange histograms represent high IMF cone angles ($\gtrsim 60^\circ$). There seems to be a threshold for jet formation, as it is effectively suppressed for very low $\beta \lesssim 0.5$ and $M_A \lesssim 5$ conditions for both quasi-parallel and quasi-perpendicular regimes. However, during low IMF cone angle conditions, there are only 2–3 h of magnetosheath data in these low $\beta$ and $M_A$ bins. Overall, we can see that for low IMF cone angles (downstream of the quasi-parallel shock), the distributions are relatively flat (within error bars), while there are clear trends in many distributions for high IMF cone angles. A flat histogram indicates that the parameter has no influence on jet formation, as we see no preference in the data for any particular values. However, trends in the histograms indicate that there is a preference, i.e., jets are more often observed during certain solar wind conditions. The results indicate that conditions favorable for jet formation during high IMF cone angles (downstream of the quasi-perpendicular shock) are especially: low $B$, low $n$, high $\beta$, and high Mach numbers (except for sonic Mach number). Also low $P_{\text{dyn}}$, high $V$, and high $T$ seem to be favorable for quasi-perpendicular jet occurrence. Although not shown here, similar results for solar wind conditions are obtained when looking at short- and long-duration jets separately.

Figure 3. Distributions of (a) jet duration, (b) jet length parallel to $v(t_0)$, and (c) $P_{\text{dyn},X}$ ratio between the magnetosheath value and the solar wind value at $t_0$. The distributions are shown separately for low IMF cone angles (solid blue), high IMF cone angles (solid orange), and high IMF cone angles with SW $\beta < 2$ (dotted orange).

In Figure 3, we show the distributions of jet durations, lengths parallel to the jet propagation direction $v(t_0)$, and the ratio of jet and solar wind earthward dynamic pressure for low (blue solid line) and high (orange solid line) IMF cone angles separately. During high IMF cone angles, the jets tend to be clearly smaller (both in duration and parallel length; Figures 3a&b). The quasi-perpendicular jet size distribution peaks at $\sim 0.1 R_E$. Small jets are much less common during low IMF cone angles, and the size distribution of quasi-parallel jets peaks at $\sim 1.5 s$ and $\sim 0.3 R_E$. Jets are also weaker during high IMF cone angles as can been in Figure 3c. We have additionally included the histograms representing jets observed during high IMF cone angle and $\beta < 2$ conditions. We can see that for parallel lengths, this histogram is more similar to the distribution of jets during low IMF cone angles. This shows that for high IMF cone angle conditions or the quasi-perpendicular shock, high $\beta > 2$ (or high $M_A$, although not shown here) in particular increases the formation of small jets. This does not account for the whole difference in jet occurrence rates for low and high $\beta$, as jets of all sizes are more common during high $\beta$. There is no such difference in the distributions of jet strengths ($MSH/SW$ dynamic pressure ratios) between low and high $\beta$ conditions.
3.2 Examples of Quasi-Perpendicular Bow Shock Crossings During Different $\beta$ and $M_A$ Conditions

To better understand the statistical results for jets during high IMF cone angles, we present examples of quasi-perpendicular shock crossings observed by THEMIS and MMS during different solar wind $\beta$ and $M_A$ conditions. We show four events, which show us how the structure of the shock changes with increasing $\beta$ and $M_A$, and how that relates to observations of downstream jets. We move from low to high $\beta$ and $M_A$. We use the Plaschke et al. (2013) jet algorithm to look for jets in the data. Two of the events (Event 2 and Event 3) are THEMIS multi-spacecraft events, in which we can confirm the quasi-perpendicular geometry and $\beta$ and $M_A$ conditions with simultaneous local upstream measurements instead of relying only on OMNI measurements.

Figure 4 shows Event 1: MMS1 was crossing from the solar wind to the magnetosheath on March 4, 2019, around ~22:42 UT. MMS1 was located at [15.4, −3.2, 1.8]RE (in GSE). Both OMNI and local measurements in the solar wind show a quasi-perpendicular geometry. The ion spectrogram also shows a lack of $>10$ keV ions consistent with this. We estimate $\theta_B n = 65^\circ$ for OMNI and $71^\circ$ for local upstream measurements, respectively, using Merka et al. (2005) bow shock model. Local measurements from the upstream region 22:41–22:42 yield solar wind $\beta = 1.7$ and $M_A = 5.7$, which are in relatively close agreement with OMNI ($\beta = 0.65$ and $M_A = 6.0$). These represent low $\beta$ and $M_A$ conditions for jets (see Figure 2 statistics). We note that density and temperature observations of MMS FPI instrument can be unreliable in the solar wind due to the narrowness of the solar wind beam, and thus there is uncertainty especially in $\beta$. The left panel of Figure 4 shows an overview of the with data resampled to 0.5 s cadence. We see a relatively abrupt quasi-perpendicular shock crossing with foot, overshoot, and undershoot signatures. The downstream region of the shock exhibits little structure, and the Plaschke et al. (2013) algorithm finds one small and weak jet (highlighted in magenta) for this data.

The right panel of Figure 4 is a zoom-in into the magnetosheath. For direct comparison with the statistical THEMIS data set, we show the measurements downsampling to 3 s and then interpolated to 1 s (thick lines). The instrument data rate measurements (FGM: 62.5 ms, FPI: 150 ms) are shown in thin lines. The Plaschke et al. (2013) algorithm finds two very small jets when applied on instrument burst level data, but no detection when using the data downsampled to 3 s and interpolated to 1 s. Note that in this event, the OMNI dynamic pressure is lower than the local upstream dynamic pressure, which means that these jets would likely not be identified if we used the local measurements for the threshold.

Next, we look at Event 2 observations by THEMIS A, D, and E spacecraft on May 11, 2015, around ~21:00 UT. The spacecraft were all located near the bow shock nose. These locations are shown in Figure 5. THEMIS A was in the solar wind, THEMIS E crossed the bow shock from the magnetosheath to the solar wind, and THEMIS D was in the magnetosheath (see Figure 6). Figure 5 also shows a model bow shock shape (Merka et al., 2005) and the estimated bow shock normal at the point closest to THEMIS E. We have plotted the average magnetic field vectors during 20:57–21:02 UT measured by OMNI and by THEMIS A in the solar wind. We see that the bow shock was clearly very perpendicular: $\theta_B n = 84^\circ$ based on THEMIS A observations and $\theta_B n = 89^\circ$ based on OMNI observations. The solar wind $\beta$ and $M_A$ were, respectively, 5.5 and 16 according to OMNI and 2.4 and 8.5 according to local THEMIS A observations in the upstream. We note that temperature observations of THEMIS ESA instrument can be unreliable in the solar wind due to the narrowness of the solar wind beam, and thus there is uncertainty especially in $\beta$.

Figure 6 shows the measurements from these three locations. THEMIS A observes no foreshock and quite steady solar wind. Nearby THEMIS E crosses from the magnetosheath into the solar wind with a shock transition region in between. This transition region is structured with more variations in magnetic field, density, and velocity com-
pared the magnetosheath proper that was observed before. Two 15–20 s and three smaller jets can be identified within this transition region. THEMIS D further in the magnetosheath observes the much less structured and higher temperature magnetosheath proper. Figure 7 is a zoom-in of THEMIS E observations during the quasi-perpendicular transition region. Here the data are interpolated to 1 s cadence to be comparable with the statistical data set. Note that changing the cadence of the data changes the lengths of the jet intervals. The first two jets exhibit significant increases in earthward flow velocity, while the other jets are driven by density increases. The first jet is a strong one in terms of its earthward dynamic pressure ratio ($\sim 90\%$) while the others are weak.

Next, let us look at Event 3 observations by THEMIS B and C on August 10, 2009, around $\sim 20:10$ UT. Figure 8 shows the positions of the spacecraft, and the observed magnetic field orientations by OMNI and THEMIS C in the solar wind at 20:10–20:15. Figure 9 shows the observations of THEMIS C in the upstream and THEMIS B crossing the bow shock from the magnetosheath to the solar wind. The solar wind $\beta$ and $M_A$ were, respectively, 170 and 93 according to OMNI and 100 and 55 according to local THEMIS C observations in the upstream. The IMF magnitude is remarkably low in this event, as THEMIS C is observing $B \sim 1$ nT. Because the $M_A$ is so extremely high, the Merka et al. (2005) bow shock model does not produce realistic bow shock shape anymore (in Figure 8 we have plotted a model bow shock shape with a higher magnetic field magnitude $B = 2$ nT for illustration). However, we can estimate $\theta_{Bn}$ with the IMF cone angle. OMNI measurements yield an IMF cone angle of $86^\circ$ and the local THEMIS C observations yield the same value. As the THEMIS B and C spacecraft are observing the subsolar region, $\theta_{Bn}$ has to be very high with this perpendicular field. The lack of $> 10$ keV ions in the ion energy spectrogram is again consistent with this.

While THEMIS C observes relatively steady upstream conditions, THEMIS B crossing the bow shock observes a prolonged transition of magnetosheath plasma to the solar wind plasma (Figure 9). This shock crossing exhibits a train of high-amplitude magnetic field enhancements in the upstream region, which grow larger towards the shock. Note the arrow on the top of the THEMIS B panel, which indicates the beginning of the magnetosheath interval in which we search for jets. One very short-duration jet and two $\sim 20$ s jets can be identified within this interval with the ground reduced ESA data. Figure 10 is a zoom-in to THEMIS B observations downstream during 20:09:20–21:15:20 UT. In this interval, right downstream of the shock, the flow velocity has already decreased substantially and the density has increased, but there are still high-amplitude variations in magnetic field and density. The second jet exhibits a high increase in earthward velocity. Before this zoom-in window, THEMIS B observes magnetosheath with less variations and higher temperature (see Figure 9). We again interpret this as the shock having a structured transition layer, which also contains jets, and deeper in the magnetosheath these variations have dissipated.

In Figure 11, we present Event 4: MMS1 burst observations of another very high $\beta \sim 70$ and $M_A \sim 60$ quasi-perpendicular bow shock crossing on November 25, 2017, around $\sim 23:40$ UT. This event serves as an extreme example of how the quasi-perpendicular magnetosheath can exhibit a high degree of structuring during high solar wind $\beta$ and $M_A$, and how it is resolved by high-resolution MMS measurements. The data in the left panel (with the exception of the ion spectrogram) have been downsampled to 2-s cadence. This bow shock crossing and its upstream structure has been studied in detail by Petrukovich and Chugunova (2021), but they did not focus on the magnetosheath downstream of the shock. Petrukovich and Chugunova (2021) calculated the $\theta_{Bn}$ to be $68^\circ$ based on OMNI observations and $59^\circ$ based on local measurements in the upstream region, yielding a quasi-perpendicular geometry. We can see a periodic train of high-amplitude magnetic field and density enhancements in the upstream region and at the extended shock crossing. Petrukovich and Chugunova (2021) placed the shock crossing at 23:38 UT, when the mag-
The fluctuations are also present in the downstream. Their period is $\sim 20$ s. However, no jets can be identified in this data as the variations in $V_X$ component are too low in these timescales. Note that we only execute the search when there are OMNI solar wind dynamic pressure observations available for the preceding minute, here within 23:27–23:33 UT. The right-hand panel shows a zoom-in to the magnetosheath. Here the thicker lines represent data first downsampled to a 3-s resolution and then interpolated to a 1-s cadence, to be directly comparable with the data used to construct the THEMIS jet data set. Again, no jets are found using this data. The thinner lines represent the data at instrument resolutions (FGM: 62.5 ms, FPI: 150 ms). The jet detection algorithm identifies many of these density enhancements as jets in the burst-resolution plasma data. This is due to short timescale (a few seconds) variations in $V_X$, which allow them to fulfill the Plaschke et al. (2013) criteria. Again, deeper in the magnetosheath (before the zoomed-in window), the level of fluctuations is much lower and jets are not identified.

### 4 Discussion

On top of the now well-established link between jets and low IMF cone angles, or the quasi-parallel shock, LaMoury et al. (2021) found additional parameters affecting jet formation. They concluded that low $B$, low $n$, high $\beta$, and high $M_A$ are favorable conditions for jet generation. According to our detailed study, these results apply to jets forming during high IMF cone angle conditions. During low IMF cone angles, other solar wind parameters do not have a significant influence on jet occurrence. However, jet occurrence is very effectively suppressed for very low $\beta \lesssim 0.5$ and $M_A \lesssim 5$ conditions for both quasi-parallel and quasi-perpendicular regimes (although there is statistical uncertainty for the quasi-parallel case). This corresponds relatively well with the threshold ($M_A \sim 2–3$) where the shock becomes subcritical and ceases to reflect particles (Burgess et al., 2012; Kennel et al., 1985). In other words, substantial ion reflection seems to be a key ingredient for jet formation. Tinoco-Arenas et al. (2022) studied 2D local hybrid simulations of shocks with parameters close to these threshold values. They used $\beta = 0.5$ and varied $\theta_{BN}$ and $M_A$. They found jets within the whole parameter range $M_A \in [4.28, 7.42]$.

Separating the data to low and high IMF cone angles is important as most jets are observed during lower IMF cone angles and most magnetosheath measurements are made during higher cone angles. Thus, when normalizing the jet data by the magnetosheath data (i.e., calculating conditional probabilities; Eq. 4) without this distinction (as in LaMoury et al., 2021), the results will be exhibiting differences in solar wind characteristics during low and high IMF cone angles rather than only in jet occurrence rates. Classifying the data by cone angles removes this effect and allows us to better compare the occurrence rates during different solar wind conditions. Goncharov et al. (2020) also studied jets in the quasi-parallel and quasi-perpendicular dayside magnetosheath, including flank observations, with slightly different jet criteria and a smaller MMS data set. They did not normalize for relative radial position in the magnetosheath, i.e., separate formation and propagation. They also did not separate the normalizing magnetosheath data into these two regimes, which we argue is important because otherwise we end up comparing lower IMF cone angle jet observations mostly to higher IMF cone angle magnetosheath observations. Their results suggested that jets are more common during higher magnetic field magnitude, solar wind speed, $M_A$, and $\beta$. The last two results are in agreement with our results (but only for the quasi-perpendicular case), but the first two are not. The favorability they observed for higher solar wind speed may be explained by their criterion for higher dynamic pressure jets and by propagation effects (LaMoury et al., 2021). Similarly, high magnetic field magnitude is favorable for jet propagation deep into the magnetosheath.
We also statistically studied the durations of jets, their lengths parallel to their propagation direction, and their dynamic pressure ratios (i.e., strengths). We find that the durations of quasi-parallel jets peak at a little more than 10 s duration. This is comparable to the period of ULF waves in the terrestrial ion foreshock. According to our results, quasi-perpendicular jets tend to be smaller than quasi-parallel ones, which agrees with previous studies (e.g., Raptis et al., 2020; Goncharov et al., 2020). We also find that quasi-perpendicular jets tend to have a lower $P_{\text{dyn},X}$ MSH/SW ratio, meaning that they are weaker, as also found by Raptis et al. (2020). When taking a low plasma beta subset ($\beta < 2$) of the high IMF cone angle set, we find that they seem to be more similar to low IMF cone angle jets in their size distribution. The high beta quasi-perpendicular subset ($\beta \geq 2$) represents the newly resolved population of the smallest jets. However, jets of all sizes are more common during high $\beta$.

While OMNI data allow us to link every magnetosheath observation to a solar wind measurement, this data set is known to contain uncertainty (e.g., Walsh et al., 2019; Vokhmyanin et al., 2019). OMNI data are combined from multiple spacecraft at L1 and then propagated to the Earth’s bow shock. While this data are very useful for large statistical studies where errors can be assumed to average out, one cannot blindly trust it when looking at individual events. Because quasi-perpendicular jets have significantly lower occurrence rate than quasi-parallel jets, a number of the high IMF cone angle jets in this data set have certainly been misclassified, and in reality they have formed at the quasi-parallel shock. For individual events, it is important to use local upstream measurements to verify the shock geometry. Similarly, the bow shock model (Merk et al., 2005) and the magnetopause (Shue et al., 1998) model contain uncertainty. We note the models have ranges of solar wind values where they are valid, and thus the leftmost and rightmost bins in Figure 2 are most unreliable in terms of $F$ values. The assumption that data with $F \in [0.5, 1.1]$ are close to the bow shock may therefore not strongly hold in these bins.

We provided four examples of multi-spacecraft quasi-perpendicular shock crossings with varying $\beta$ and $M_A$ to give context on how the quasi-perpendicular shock transition changes with increasing $\beta$ and $M_A$ and how these dynamics may be linked to jet formation. We used local upstream observations including simultaneous two-point measurements by THEMIS to verify the steady quasi-perpendicular geometry and the high $\beta$ and $M_A$ in the solar wind. With increasing $\beta$ and $M_A$ the shock transition becomes more extended. Note, however, that the observed duration depends on the relative motion between the shock and the spacecraft. The so-called transition region exhibits high-amplitude variations particularly in magnetic field magnitude and density. There is no clear anticorrelation between magnetic field magnitude and density, so we do not consider these mirror mode waves, which are typical in the quasi-perpendicular magnetosheath proper. In contrast, the magnetic field and density are often enhanced together. There are also enhancements of dynamic pressure and some of these can be identified as earthward jets by the Plaschke et al. (2013) criterion. These jets are indeed present in the shock transition region but were not recorded in our examples deeper in the magnetosheath. A statistical investigation also revealed that quasi-perpendicular jets during high $M_A$ solar wind conditions typically occur very close to the model bow shock (not shown). Thus, these type of jets are probably not very likely to go on and impact the magnetopause, perhaps as they dissipate in the transition region.

Previous observations of the Earth’s quasi-perpendicular bow shock during high $M_A$ (Sundberg et al., 2017; Madanian et al., 2021) and high $\beta$ (Petrukovich & Chugunova, 2021) (high $M_A$ and high $\beta$ are tied to each other at Earth’s heliocentric distance) show that such shock crossings are extended and exhibit high magnitude structures both upstream and downstream. These structures form upstream due to reflected ion dynamics, which become important for dissipating energy in these conditions. Sundberg et al. (2017) presented Cluster observations from three quasi-perpendicular shock crossings,
and suggested that the observed non-stationarities of the shock could be due to the ion
Weibel instability. Petrukovich and Chugunova (2021) concluded that the observed struc-
tures are not mirror mode waves typically observed in the quasi-perpendicular magne-
tosheath. They claimed that they are most likely due to shock reformation, although they
did not provide any direct evidence. Madanian et al. (2021) named these upstream struc-
tures “proto-shocks”, which are a part of quasi-periodic shock reformation. They con-
cluded that these structures are created by the reflected ions at the edge of the foot, and
then they grow non-linearly while they convect towards the shock. These proto-shocks
slow down the incoming solar wind and influence the reflection of particles from the shock
(this is also seemingly happening in our Events 3 and 4, although not shown here). All
these studies suggest that while such reformation structures are present, the main shock
layer never disappears. Sulaiman et al. (2015) studied several high \( M_A \) Saturn’s bow shock
crossings and showed that there is a reformation cycle typically at a period of \( \sim 26\% \)
of the ion gyroperiod. Sundberg et al. (2017), Madanian et al. (2021), and Petrukovich
and Chugunova (2021) found similar reformation structures with periods close to this
value. This also fits well with the timescales of upstream structures seen in Events 3 and
4 shown in our study. While typically the quasi-perpendicular shock reformation length
and time scales are small in comparison to scales commonly associated with magnetosheath
jets, this period can become of the order of tens of seconds when the IMF magnitude be-
comes very low (\( \lesssim 1 \) nT).

The quasi-perpendicular shock can also exhibit ripples that move along the shock
surface (e.g., Lowe & Burgess, 2003; Johlander et al., 2016; Madanian et al., 2021). Lowe
and Burgess (2003) found their frequencies to be around a couple times the upstream
ion gyrofrequency in their 2D hybrid simulations. Johlander et al. (2016) studied rip-
ples at a shock crossing observed by MMS and found the ripple frequency to be three
times the upstream ion gyrofrequency. Timescales of both the reformation cycle and rip-
ples are dependent on the upstream ion gyrofrequency, and therefore these timescales
increase for lower upstream magnetic field magnitude (for higher \( \beta \) and \( M_A \) conditions).
This fits well with our statistical results that jets downstream of the quasi-perpendicular
shock (or during high IMF cone angles) are significantly more common when the IMF
magnitude is low (and \( \beta \) and \( M_A \) are high). This indicates that the quasi-perpendicular
shock dynamics amplified and temporally/spatially enlarged by high \( \beta \) and high \( M_A \) up-
stream conditions can also lead to the formation of jets as a by-product. As quasi-parallel
jet formation has been suggested to be related to bow shock rippling (Hietala et al., 2009;
Hietala & Plaschke, 2013) and Raptis et al. (2022) showed that quasi-parallel shock ref-
Ormation can lead to downstream jets, already known, or similar, mechanisms could pos-
sibly explain jet formation at quasi-perpendicular shocks, as well.

Recently, Omidi et al. (2021) studied the spatial and temporal structure of a high
\( M_A \) quasi-perpendicular shock with a global 2.5D simulation. Their simulation results
indicate that upstream structures, such as previously reported for these type of shocks,
can emerge in spacecraft data due to a surface wave moving along a shock and the shock
crossing the spacecraft numerous times. These results highlight an important and inher-
ent issue of disentangling temporal and spatial variations when analyzing single-spacecraft
data. More detailed multi-spacecraft studies are needed to discard possible misclassifi-
cations of bow shock crossings as jets and to study how jets move with respect to the
surrounding plasma. This would help us understand their nature and formation: whether
they are related to ripples moving along the shock and/or whether they are related to
the processing of the solar wind at the structures of the reformation cycle and whether
they can propagate far from the shock towards the magnetopause. We attempted to per-
form an MMS timing analysis for the dynamic pressure fluctuations of Event 4, but the
shorter-scale fluctuations made it impossible for us to cross-correlate the signals accu-
rately. We note that the width of the shock transition region, and also the jets within,
is dependent on the speed of the spacecraft moving in space and/or on the speed of the
shock as it moves across the spacecraft.
Finally, we have highlighted that the time resolution of observations can have an effect on whether a jet algorithm classifies a certain structure as a jet. Thus, different data sets may yield relatively more or fewer jets due to differences in cadences. This is important to consider when comparing or combining data from different instruments and missions.

5 Conclusions and Summary

In this study, we have statistically studied how solar wind conditions influence jet occurrence in the two regimes of low and high IMF conditions using an extensive THEMIS spacecraft data set from the years 2008–2020. This allows us to better understand jet formation at the quasi-parallel and quasi-perpendicular shocks, respectively. Jet formation is observed to commence for $\beta \gtrsim 0.5$ and $M_A \gtrsim 5$ for both shock geometries. We found that during low IMF cone angles, jet occurrence close to the bow shock is not sensitive to the other solar wind parameters. In contrast, during high IMF cone angle conditions, jet formation changes as a function of other solar wind parameters: quasi-perpendicular jets are more frequently observed when the IMF magnitude is low, the SW speed is high, the SW density is low, the plasma beta is high, and the Alfvén Mach number is high.

The quasi-perpendicular jets have an intrinsic scale size: the distribution of sizes (parallel to flow) peaks at $\sim 15$ s and $\sim 0.3 R_E$. The jets formed during high IMF cone angles (or at the quasi-perpendicular shock) are smaller in size and weaker in dynamic pressure than those observed during low IMF cone angles. In particular, these small jets tend to form during high $\beta$ and $M_A$ conditions.

We presented examples of quasi-perpendicular shock crossings during different solar wind $\beta$ and $M_A$ conditions, illustrating that when these parameters increase, the shock dynamics change and the shock transition becomes more extended in agreement with previous studies. In particular, we showed the shock transition region exhibits large-amplitude variations not only in the magnetic field and density, but also in dynamic pressure. Earthward magnetosheath jets were consequently found in this transition region. They may be related to the reformation of the quasi-perpendicular shock, as the reformation and rippling time scales become larger for decreasing magnetic field magnitude (or increasing $\beta$ and $M_A$). Deeper in the magnetosheath the plasma structuring has dissipated and at least in these particular events we did not see jets there. This indicates that these types of quasi-perpendicular jets are not expected to be geoeffective. However, they are a part of high $\beta$ and high $M_A$ shock dynamics, and their relevance may be more significant at shock environments where the magnetic field obliquity, $\beta$, and $M_A$ are frequently higher.

We note that future multi-spacecraft studies are needed to clarify how these jets propagate, and consequently to confirm that they are not simply signatures of the shock moving across the spacecraft due to surface waves.

Open Research

THEMIS and OMNI data can be accessed via, e.g., NASA’s Coordinated Data Analysis Web (https://cdaweb.gsfc.nasa.gov/). The magnetosheath and jet data set used in this study can be found at Koller et al. (2021).

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Event 1

Figure 4. MMS1 observations on March 4, 2019 (Event 1). (a) OMNI IMF cone angle, (b) OMNI solar wind β and $M_A$, (c) ion omni-directional energy spectrogram, (d) magnetic field magnitude, (e) magnetic field GSE components, (f) ion number density, (g) ion velocity magnitude and GSE components, (h) ion total, parallel, and perpendicular temperatures, and (i) total and GSE $-X$ aligned dynamic pressures with $1/2$ (orange) and $1/4$ (magenta) of OMNI solar wind dynamic pressure. The magenta shading indicates a jet found using the Plaschke et al. (2013) jet criteria. The black arrow on top shows the selected upstream edge of the magnetosheath window in which we search for jets. In the left panel, the data are downsampled to 0.5 s cadence, and one jet is found with this cadence. In the zoomed-in panel on the right, thin lines show instrument resolution: survey mode for FGM and burst mode for FPI. Two jets were found using this FPI data. Thick lines show the data first downsampled to 3 s cadence and then interpolated to 1 s to be directly comparable to the statistical THEMIS data set. No jets were found using this data.
Figure 5. OMNI measurements for Event 2 on May 11, 2015: (a) IMF cone angle, (b) $\beta$ and $M_A$. The locations of THEMIS A, D, and E spacecraft during 20:57–21:02 UT in the GSE (c) $X$–$Y$ plane and (d) $X$–$Z$ plane. The black line represents a model bow shock (Merka et al., 2005). The black arrows represent the model bow shock normal vectors at the point closest to THEMIS E. Gray arrows represent the average magnetic field vectors observed by OMNI and THEMIS A in the solar wind.

Figure 6. THEMIS A, E, and D observations for Event 2. (a) ion omni-directional energy spectrogram, (b) magnetic field magnitude, (c) magnetic field GSE components, (d) ion number density, (e) ion velocity magnitude and GSE components, (f) ion total, parallel, and perpendicular temperatures, and (g) total and GSE $-X$ aligned dynamic pressures with $1/2$ (orange) and $1/4$ (magenta) of OMNI solar wind dynamic pressure. The magenta shading indicates a jet found using the Plaschke et al. (2013) jet criterion on reduced level ESA data.
Figure 7. A zoom-in of THEMIS E observations for Event 2 in the same format as in Figure 6. The plasma data have been interpolated to 1 s cadence to match the cadence of the statistical data set. The magenta shading indicates a jet found using the Plaschke et al. (2013) jet criterion on this 1-s cadence data.

Figure 8. OMNI measurements for Event 3 on August 10, 2009: (a) IMF cone angle, (b) $\beta$ and $M_A$. The locations of THEMIS B and C spacecraft during 20:10–20:15 UT in the GSE (c) $X$–$Y$ plane and (d) $X$–$Z$ plane. The black line represents a model bow shock (Merka et al., 2005) for reference, but the model is calculated for $B = 2$ nT that is larger than the observed value, as the model is not reliable for the observed values $B \lesssim 1$ nT. The black arrows represent the model bow shock normal vectors at the point closest to THEMIS B. Gray arrows represent the average magnetic field vectors observed by OMNI and THEMIS C in the solar wind.
Figure 9. THEMIS C and B observations for Event 3 in the same format as in Figure 6. The magenta shading indicates a jet found using the Plaschke et al. (2013) jet criterion on the ESA reduced level data. The black arrow on top shows the selected upstream edge of the magnetosheath window in which we search for jets.
Figure 10. A zoom-in of THEMIS B observations for Event 3 in the same format as in Figure 6. The plasma data have been interpolated to 1 s cadence to match the cadence of the statistical data set. The magenta shading indicates a jet found using the Plaschke et al. (2013) jet criterion on this 1-s cadence data.
Figure 11. MMS1 crossing the Earth’s bow shock from the magnetosheath to the solar wind on November 25, 2017, (Event 4) in the same format as Figure 4. The black arrow on top shows the selected upstream edge of the magnetosheath window in which we search for jets. In the left panel, the data are downsampling to 2s cadence. No jets were found using this cadence. In the zoomed-in panel on the right, thin lines show instrument resolution data: survey mode for FGM and burst mode for FPI. Many jets were found using this data. Thick lines show data first downsampled to 3s cadence and then interpolated to 1s to be directly comparable to the statistical THEMIS data set. No jets were found when using this data.