Benefits of Fully Focused SAR Altimetry to Coastal Wave Height Estimates: A Case Study in the North Sea

Florian Schlembach\textsuperscript{1}, Frithjof Ehlers\textsuperscript{2}, Marcel Kleinherenbrink\textsuperscript{2}, Marcello Passaro\textsuperscript{2}, Denise Dettmering\textsuperscript{1}, Florian Seitz\textsuperscript{1}, and Cornelis Slobbe\textsuperscript{2}

\textsuperscript{1}Deutsches Geodätisches Forschungsinstitut
\textsuperscript{2}Geoscience and Remote Sensing

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Abstract

Estimating the three geophysical variables significant wave height (SWH), sea surface height, and wind speed from satellite altimetry continues to be challenging in the coastal zone because the received radar echoes exhibit significant interference from strongly reflective targets such as mud banks, sheltered bays, ships etc. Fully focused SAR (FF-SAR) processing exhibits a theoretical along-track resolution of up to less than half a metre. This suggests that the application of FF-SAR altimetry might give potential gains over unfocused SAR (UF-SAR) altimetry to resolve and mitigate small-scale interferers in the along-track direction to improve the accuracy and precision of the geophysical estimates. The objective of this study is to assess the applicability of FF-SAR-processed Sentinel-6 Michael Freilich (S6-MF) coastal altimetry data to obtain SWH estimates as close as possible to the coast. We have developed a multi-mission FF-SAR processor and applied the coastal retracking algorithm CORALv2 to estimate SWH. We assess different FF-SAR and UF-SAR processing configurations, as well as the baseline Level-2 product from EUMETSAT, by comparison with the coastal, high-resolution SWAN-Kuststrook wave model from the Deltares RWsOS North Sea operational forecasting system. This includes the evaluation of the correlation, the median offset, and the percentage of cycles with high correlation as a function of distance to the nearest coastline. Moreover, we analyse the number of valid records and the L2 noise of the records. The case study comprises five coastal crossings of S6-MF that are located along the Dutch coast and the German coast along the East Frisian Islands in the North Sea. We find that the FF-SAR-processed dataset with a Level-1b posting rate of 140 Hz shows the greatest similarity with the wave model. We achieve a correlation of \( \sim 0.8 \) at 80\% of valid records and a gain in precision of up to 29\% of FF-SAR vs UF-SAR for 1-3 km from the coast. FF-SAR shows, for all cycles, a high correlation of greater than or equal to 0.8 for 1-3 km from the coast. We estimate the decay of SWH from offshore at 30 km to up to 1 km from the coast to amount to 26.4\% \( \pm \) 3.1\%. 

\begin{figure}
\centering
\includegraphics[width=\textwidth]{figure1.png}
\caption{Example figure}
\end{figure}
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Florian Schlembach (florian.schlembach@tum.de); Frithjof Ehlers; Marcel Kleinherenbrink; Marcello Passaro; Denise Dettmering; Florian Seitz; Cornelis Slobbe

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Estimating the three geophysical variables significant wave height (SWH), sea surface height, and wind speed from satellite altimetry continues to be challenging in the coastal zone because the received radar echoes exhibit significant interference from strongly reflective targets such as mud banks, sheltered bays, ships etc. Fully focused SAR (FF-SAR) processing exhibits a theoretical along-track resolution of up to less than half a metre. This suggests that the application of FF-SAR altimetry might give potential gains over unfocused SAR (UF-SAR) altimetry to resolve and mitigate small-scale interferers in the along-track direction to improve the accuracy and precision of the geophysical estimates.

The objective of this study is to assess the applicability of FF-SAR-processed Sentinel-6 Michael Freilich (S6-MF) coastal altimetry data to obtain SWH estimates as close as possible to the coast.

We have developed a multi-mission FF-SAR processor and applied the coastal re-tracking algorithm CORALv2 to estimate SWH. We assess different FF-SAR and UF-SAR processing configurations, as well as the baseline Level-2 product from EU-METSAT, by comparison with the coastal, high-resolution SWAN-Kuststrook wave model from the Deltares RWsOS North Sea operational forecasting system. This includes the evaluation of the correlation, the median offset, and the percentage of cycles with high correlation as a function of distance to the nearest coastline. Moreover, we analyze the number of valid records and the L2 noise of the records. The case study comprises five coastal crossings of S6-MF that are located along the Dutch coast and the German coast along the East Frisian Islands in the North Sea.

We find that the FF-SAR-processed dataset with a Level-1b posting rate of 140 Hz shows the greatest similarity with the wave model. We achieve a correlation of ∼0.8 at 80% of valid records and a gain in precision of up to 29% of FF-SAR vs UF-SAR for 1-3 km from the coast. FF-SAR shows, for all cycles, a high correlation of greater than or equal to 0.8 for 1-3 km from the coast. We estimate the decay of SWH from offshore at 30 km to up to 1 km from the coast to amount to 26.4%±3.1%.
1. Introduction

Wave height monitoring in the open ocean is widely used in ocean weather forecasting (Cavaleri et al., 2012), climate studies (Timmermans et al., 2020; Stopa et al., 2016), and other scientific studies such as for the air-sea interactions of surface-breaking waves (Melville, 1996). The information about wave heights is also relevant for applications such as industrial shipping route planning. Moreover, the knowledge of wave heights in the coastal zone is of particular interest as about 23-37% of the world’s population lives within 100 km of the shoreline (Glavovic et al., 2022). Hence, wave heights in the coastal zone have to be taken into consideration for coastal risk assessment studies.

One way to measure wave heights globally is with satellite radar altimetry, which has been in use for over three decades to obtain estimates of sea level and sea state. The measurement principle of satellite radar altimetry is based on measuring the echoes of a transmitted frequency-modulated pulse as a function of two-way travel time. From the shape of the returned/received and processed pulse echoes and their amplitudes, the three geophysical variables sea surface height (SSH), significant wave height (SWH), and wind speed can be derived. The SWH is defined as four times the standard deviation of the sea surface elevation (Holthuijsen, 2007).

The most recent operational satellite altimetry processing is called unfocused synthetic aperture radar (UF-SAR)/Delay-Doppler (DD) processing (Raney, 1998), which is applied to the satellite altimetry missions CryoSat-2 (CS2), Sentinel-3 (S3), and Sentinel-6 Michael Freilich (S6-MF).

Numerous works have addressed the challenges in the field of coastal altimetry (Fenoglio-Marc et al., 2010; Vignudelli et al., 2011; Cipollini et al., 2009, 2011, 2012; Gomez-Enri et al., 2016). Timmermans et al. (2020) assessed extreme wave heights from satellite altimetry, which agree well with in-situ data for up to 5 km from the coast but lack proper spatio-temporal sampling for closer distances to the coast. Coastal SWH observations from satellite altimetry are often discarded or are of bad quality due to coastal interference that originates from strongly reflective targets such as sand or mud banks, sheltered bays, or calm waters close to the shoreline. Schlembach et al. (2022) showed that the correlation of SWH data of the operational baseline product of S3 with in-situ data from buoys amounts to less than 0.20 for closer than 20 km from the coast. Tailored retracking algorithms have been developed to account for the coastal interference, such as ALES (Passaro, 2015), Brown-Peaky (Peng and Deng, 2018) for the conventional low resolution mode (LRM) altimetry, and SAMOSA+ (Dinardo et al., 2018), SAMOSA++ (Dinardo et al., 2020), ALES+SAR (Passaro et al., 2021), RiwiSAR-SAR (Gou and Tourian, 2021), CORS (Garcia et al., 2022), or CORALv1 (Schlembach et al., 2022) for UF-SAR altimetry. The enhanced coastal processing algorithms allow the derivation of relevant wave-related statistics in the coastal zone, e.g. as done by Passaro et al. (2021). They investigated the global attenuation of SWH from offshore at 30 km to >3 km off the coast and found the wave heights are globally, on average, 22% smaller than offshore while using the conventional LRM altimetry with a lower posting rate of 1 Hz (and the ALES retracker (Passaro, 2015)). Nevertheless, the estimation of SWHs in the coastal zone with a distance-to-coast (dist-to-coast) of < 5 km remains challenging, as the quality of the estimates deteriorates (Schlembach et al., 2022).

The capability to measure SWH in the coastal zone even closer to the coast is in high demand, e.g. for studying nearshore effects such as wave energy transformation (Lipmann et al., 1996; Contardo et al., 2018), sediment transport (Elfrink and Baldock, 2002; Chowdhury and Behera, 2017; de Vries et al., 2020), dissipation effects (Wright, 1976; Wang and Kraus, 2005; Bryan and Power, 2020), coastal protection (Pilarscizy, 1990; Charlier et al., 2005) and safety (Arens et al., 2013). The need to approach the coastline even closer is also specified by the current draft of the mission requirement documents of the Copernicus Sentinel-3 Next Generation Topography (S3NG-T) team, which has defined the requirement to give SSH and SWH estimates up to 3 km and, as an enhanced target, up to 0.5 km off the coastline (European Space Agency).

As an evolution of UF-SAR altimetry, fully focused synthetic aperture radar (FF-SAR) altimetry constitutes a novel processing technique initially applied to altimetry data by Egido and...
Smith (2017). It exploits the fully coherent processing of the received radar pulse echoes during the whole target illumination time, by which a theoretical along-track resolution of less than a meter can be achieved for coherent targets. With FF-SAR processing, we expect to acquire SWHs that are less affected by strongly reflective targets in the coastal zone due to its inherently high along-track resolution.

The S6-MF mission offers great potential to apply FF-SAR processing due to its open-burst, interleaved operation mode, i.e. the pulses are continuously transmitted and received in a manner that the reception of the pulses occurs in between the phases of transmission (Donlon et al., 2021). That is, only minor spurious grating lobes (or: target replicas) are expected in the along-track direction at multiples of \( \sim 300 \) m (Ehlers et al., 2022), as compared to the CS2 or S3 missions that exhibit more frequent and stronger grating lobes at \( \sim 90 \) m (Egido and Smith, 2017; Guccione et al., 2018) due to the lacunar sampling/closed-burst operation mode.

This work is a case study to assess the capability of FF-SAR-processed S6-MF coastal altimetry data to obtain SWHs as close as possible to the coastline. In order to achieve this, we formulate the following research objectives:

1. We aim to assess whether the SWH estimation from coastal altimetry data can be further improved by using FF-SAR- instead of UF-SAR-processing.
2. Furthermore, we want to evaluate whether the statistical improvements observed in the coastal SWH estimates are also beneficial in practice for determining key metrics that are relevant for fields such as coastal protection.

To address both, we aim to perform a(n)

- Comparison of the FF-SAR- and UF-SAR-processed altimetry data with a high-resolution wave model data as a function of dist-to-coast
- Evaluation of the quantity and the precision of the altimetry data as a function of dist-to-coast
- Identification and quantification of dissimilarities between the altimetry data and high-resolution wave model data
- Exploitation of nearshore SWH records by the estimation of the change in SWH from offshore towards to the coast

This paper is structured as follows: Section 2 describes the altimetry and wave model data used. Section 3 explains the processing chain of the altimetry data, the methods to compare the altimetry datasets with the wave model and the estimation of the quantity and precision of the altimetry estimates, as well as the metric of the coastal SWH variation. Section 4 presents and discusses the results of the study. Section 5 draws a conclusion and gives an outlook for future work.

## 2. Data

### 2.1. Altimetry

We use S6-MF Level-1a (L1a) and Level-2 (L2) data baseline version F06 in the Non Time Critical (NTC) timeliness. The data was downloaded using the PO.DAAC interface from the NASA Jet Propulsion Laboratory (JPL, 2020). We process the L1a data to acquire two FF-SAR- and one UF-SAR-processed datasets. The processing chain and the settings of the datasets will be described in detail in Section 3.1. In addition, we take the Payload Data Acquisition and Processing High Resolution (PDAP-HR) dataset from the baseline L2 products, which corresponds
to the baseline UF-SAR/HR processing chain as described in the S6-MF L2 product generation specification document (EUMETSAT, 2022b). The PDAP-HR dataset is retracted with the open ocean SAMOSA-based retracker (EUMETSAT, 2022b, Section 4.5.2), which is not optimised for the coastal zone. We, though, include it as a reference to highlight the improvements to the SWH estimates by our processing configurations. The provided swh_ocean_qual flag is used to exclude bad estimates. The residual estimates represent the number of valid records, which are part of our statistical analysis. For the discussion of the offset with respect to the wave model, we also include the Payload Data Acquisition and Processing Low Resolution (PDAP-LR) product from the baseline L2 product, which is processed according to the LR processing chain (EUMETSAT, 2022b, Section 4.5.1).

We use all available S6-MF data of the year 2021 included in the wave model domain (see next section), which corresponds to cycles 5 to 42 and the five passes 18, 44, 120, 196, and 213. All passes apart from 213 are descending, and, in total, 161 overpasses are available. Measurements from up to 31 km from the coast are included. This range was chosen to compute the coastal SWH variation with respect to the offshore SWH around 30 km. We define the outermost contact of the satellite’s nadir locations with land as the coastline to avoid the tidal flats of the Wadden Sea. A map of the collocated data is shown in Figure 1 (a). Figure 1 (b-f) shows the zoomed-in views of the five individual coastal crossings.

Figure 1: The model domain of the SWAN-Kuststrook wave model with its curvilinear grid is shown in (a). Panels b, c, d, e and f display the S6-MF passes 44, 120, 196, 18, and 213, respectively. The white numbers next to each pass indicate the dist-to-coast values, and the white arrows show the flight direction of the satellite. The estimated effective footprints have a size of 300x10000 m (along-track times across-track) and comprise the area on the ground that is estimated to have a major impact on the leading edge (LE) of the multilooked waveform, i.e. on the estimates of the geophysical variables.

Below is a description of the five S6-MF passes analysed in this study.

**Pass 18** goes over the western tip of the Wadden island Juist, Germany. The first two kilometres off the coast are covered by sandbanks, which deteriorates the records due to the strongly reflective characteristic of sandbanks.

**Pass 44** crosses over the English Channel, where the satellite passes the UK shoreline with a minimum distance of ~2 km and goes south to the French north coast close to Calais and
thus comprises two coastal areas. The pass is located on the southwestern edge of the wave model domain. The angle of approach to the coast in the south amounts to approximately $60^\circ$ ($90^\circ$ would mean a perpendicular crossing). 

**Pass 120** is a coastal crossing located south of Rotterdam. The pass almost perpendicularly crosses a large sandbank called Aardappelenbult. The dist-to-coast is manually set to 0.0 km at the outer edge of the sandbank. This segment of the pass is quite a special coastal crossing, as no land intrusion is apparent for the very last radar footprints.

**Pass 196** is the coastal crossing of the Dutch Wadden island Texel. The angle of approach to the coastline is slightly tilted ($\sim 108^\circ$) such that the footprints of the first 1–2 km off the coast are affected by land intrusion.

**Pass 213** crosses the East Frisian Wadden island Baltrum, Germany. Its effective radar footprints are affected by many strongly reflective targets such as sandbanks, inland waters, and land/human infrastructure.

### 2.2. SWAN-Kuststrook Wave Model

To assess the potential of FF-SAR-processed S6-MF coastal altimetry data in the SWH estimation, we compared it with model-derived data. We are aware that wave model data cannot be considered the truth. However, it represents a practical way to evaluate the variability of SWH on a fine scale, such as spatial variations towards the coast, whereas buoys, which are mostly not located at the coast, can only provide pointwise measurements with limited resolution in space and time. We use the SWAN-Kuststrook wave model, which is part of the Deltares RWsOS North Sea operational forecasting system. Simulating WAves Nearshore (SWAN) is a third-generation wave model that simulates random, short-crested wind-waves in coastal regions (Booij et al., 1999) and is developed at the Delft University of Technology. It represents wave evolutions due to wind, white-capping, shoaling, bottom friction, current and depth-induced refraction, diffraction, depth-induced breaking and quadruplet/triad wave-wave-interactions (Day and Dietrich, 2022). The output of the SWAN-Kuststrook wave model is generated by the SWAN software version 41.20A.2, which includes a new set of wave physics (ST6) for the parametrisation of wind input and wind speed scaling, swell dissipation, white-capping, and others (Rogers et al., 2012). The model domain with a snapshot of SWH data is shown in Figure 1 (a) and encompasses the Dutch North Sea, the Dutch Wadden Sea, the Eastern and Western Scheldt, and the German North Sea along the East Frisian Islands. It is a nested model; the boundary conditions are taken from the regional ECMWF-WAM model that has a 0.1$^\circ$ geographical resolution (Janssen, 2011). The water level and current fields come from runs of the hydrodynamic model WAQUA-ZUNO (Gautier and Caires, 2015) and the wind fields from the High Resolution Limited Area Model (HIRLAM) (Undén et al., 2002). The bathymetry data is computed from EMODnet (Consortium, 2018) and Baseline-NL (National Georegister of the Netherlands, 2021) datasets for the deeper parts and near the coast, respectively. The model grid is curvilinear and comprises 991 times 310 points. The grid spacing in the longitudinal and latitudinal directions ranges from 50–1400 m and 35–2600 m, respectively, with the closest grid points being located near the coast to resolve small-scale dynamics. An assessment of the performance of the SWAN-Kuststrook wave model was conducted with in-situ observations data from 50 different locations. The performance was compared to the previously operational SWAN-ZUNO model within a hindcast-based analysis of four extreme events, which yields a relative bias of -1% (SWAN-ZUNO: -12%) and a scatter index of 23% (SWAN-ZUNO: 22%) for the SWH.

We compare the altimetry- and model-derived data at the locations from the EUMETSAT baseline L2 high-resolution product. The wave model data is mapped to the baseline L2 locations using a bilinear interpolation.
Table 1: L2 datasets used in this study. FFSAR-60 and FFSAR-140 are averaged after the retracking to form L2 estimates at a posting rate of 20 Hz, as described in Section 3.1.2. The PDAP-HR and PDAP-LR datasets are taken from the EUMETSAT baseline L2 product.

<table>
<thead>
<tr>
<th>Name</th>
<th>L1b: proc. type</th>
<th>L1b: posting rate [Hz]</th>
<th>L2: retracker</th>
</tr>
</thead>
<tbody>
<tr>
<td>FFSAR-60</td>
<td>FF-SAR</td>
<td>60</td>
<td>CORALv2</td>
</tr>
<tr>
<td>FFSAR-140</td>
<td>FF-SAR</td>
<td>140</td>
<td>CORALv2</td>
</tr>
<tr>
<td>UFSAR-20</td>
<td>UF-SAR</td>
<td>20</td>
<td>CORALv2</td>
</tr>
<tr>
<td>PDAP-HR</td>
<td>UF-SAR</td>
<td>20</td>
<td>SAMOSA-based</td>
</tr>
<tr>
<td>PDAP-LR</td>
<td>LRM</td>
<td>20</td>
<td>MLE4</td>
</tr>
</tbody>
</table>

Table 2: L1b processing parameters used for the FFSAR-60, FFSAR-140, and UFSAR-20 datasets.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Illumination time $T$</td>
<td>2.1 s (FF-SAR) / 2.4 s (UF-SAR)</td>
</tr>
<tr>
<td>Zero-padding-factor</td>
<td>2</td>
</tr>
<tr>
<td>Number of range gates $N_r$</td>
<td>512</td>
</tr>
<tr>
<td>L1b posting rate</td>
<td>FF-SAR: 60/140 Hz, UF-SAR: 20 Hz</td>
</tr>
<tr>
<td>Window applied</td>
<td>None</td>
</tr>
</tbody>
</table>

3. Methods

In this section, we first describe the processing methodology of the altimetry data starting from the L1a product and ending with the SWH estimates (L2 product). Secondly, we describe the statistical analysis to assess the performance of all L2 datasets. Thirdly, we explain the evaluation of the coastal SWH variation of the L2 datasets towards the coastline.

3.1. Processing of Altimetry Data

Here, we describe the details of the Level-1b (L1b) processing, starting from the received pulses and ending in the multilooked power return echo waveforms, from which the three geophysical variables SWH, SSH, and wind speed are estimated in the L2 processing stage, as described in Section 3.1.2. Table 1 lists and summarises the key properties of all datasets used in this study.

3.1.1. Level-1b Processing

We process the received pulse echoes from the L1a products to acquire the return power waveforms at the L1b data level. This is established using a multi-mission FF-SAR processor implementation originally developed for CS2 by Kleinherenbrink et al. (2020), which applies a back-projection algorithm as presented in Egido and Smith (2017). The extension to the S3 and S6-MF missions is described in detail in Ehlers et al. (2022). The FF-SAR processing includes the range cell migration correction (RCMC), the residual video phase (RVP) correction, and the compensation for additional phase jumps and other mission-specific settings (Ehlers et al., 2022). Here, we describe only specific FF-SAR processing parameters that are used for this study and are summarised in Table 2.

The FF-SAR processor obtains a statistically independent, singlelook waveform every $\sim$1 m in the along-track direction while setting a coherent integration time $T = 2.1$ s. The specific setting of $T = 2.1$ s has been evaluated to be the most sensitive within the ESA L2 GPP project (European Space Agency, 2021). The singlelook waveforms are averaged in a process called multilooking, in which non-overlapping singlelook waveforms are averaged to form multilooked
waveforms in distances that correspond to the targeted 60- and 140 Hz L1b posting rates. Both
60 and 140 Hz are odd-numbered multiples of 20 Hz (three and seven) so that the centre of the
averaged 60- and 140 Hz measurements can be georeferenced to the 20 Hz records of the baseline
L2 product.

The UF-SAR-processed L1b products are a by-product of the same FF-SAR processor, which
allows us to mimic the original DD/SAR processing chain (Dinardo et al., 2018). The time for the
coherent integration of the (range- and phase-corrected) pulses of each individual burst is reduced
from the illumination time $T$ to the burst duration, which is different from FF-SAR, where all
pulses over $T$ are coherently integrated. This reduces the theoretical along-track resolution from
$\sim 1$ m to $\sim 300$ m, assuming a static scenario of scatterers within $T$ (Egido and Smith, 2017). The
chosen illumination time of $T = 2.4$ s corresponds to the number of looks (or Doppler beams)
of 322 to be in line with the baseline PDAP product (EUMETSAT, 2022a). The Doppler-
beam stack is acquired by taking the absolute square of the integrated bursts, from which the
UF-SAR-multilooked waveform (as part of the PDAP-HR L1b product) is obtained through
summation over all bursts. We can thus collect (correlated) UF-SAR-multilooked waveforms
every $\sim 1$ m along with each of the FF-SAR-singlelooks (Egido et al., 2020). After picking the
multilooked waveforms at locations that are nearest to the ones of the EUMETSAT baseline
L2 product, we acquire the UFSAR-20 dataset, which closely matches the baseline PDAP-HR
product (after the averaging as explained in the next paragraph), but excluding the spurious
range-walk error, as investigated by Guccione (2008) and Scagliola et al. (2021). Some authors
report an increased precision by averaging consecutive UF-SAR from 40 Hz or 60 Hz posting
rates onto 20 Hz (Dinardo et al., 2015; Egido et al., 2020). However, we find that this step
introduces a correlation between neighbouring 20 Hz records and is thus not considered as viable
option; see Appendix A. Hence, an apparent gain in precision might, in part, be caused by the
effective low-pass filtering of the geophysical estimates and a corresponding loss in resolution,
which is not desired.

3.1.2. Level-2 Processing

The FF-SAR- and UF-SAR-processed L1b multilooked power waveforms are retracked with the
COastal Retracker for SAR ALtimetry version 2.0 (CORALv2) algorithm to extract the SWH
data, as presented in its first version, v1, in Schlenbach et al. (2022) (details on differences below).
As commonly done for the retracking algorithms, CORALv2 performs a least-square fitting
of the theoretical waveform, the SAMOSA2 model, with the received, multilooked waveforms
and extracts the ocean parameters SWH, SSH, and wind speed. The SAMOSA2 model is an
analytical formulation of the power return echoes that takes into account instrument-specific
(e.g. pulse repetition frequency, carrier frequency, transmission and reception bandwidths) and
orbital parameters such as the altitude, altitude rate, velocity etc. In its analytical form, it makes
several approximations, such as the Gaussian approximation of the point target response (PTR)
(Ray et al., 2015). In order to account for these, a sea-state-dependent look-up table (LUT)
is used for the $\alpha_p$ value that is part of the analytical SAMOSA2 model. The approximations
depend, amongst others, on the illumination time $T$ and also the coherent integration time used
in the L1b processing. Hence, we use the $\alpha_p$ LUT from the PDAP baseline (EUMETSAT, 2022a)
for the UF-SAR waveforms, whose illumination time is chosen to be 2.4 s (corresponding to 322
looks) and the coherent integration time to be the burst repetition interval (BRI) (as for the
PDAP-HR product). For FF-SAR, an $\alpha_p$ LUT is generated considering an illumination time of
$T = 2.1$ s and assuming an unambiguous PTR, i.e. no grating lobes (or azimuth-ambiguities)
of the PTR are taken into account (pers. comm. Salvatore Dinardo). This tailored $\alpha_p$ LUT is
then used to fit the SAMOSA zero-Doppler beam against the waveform, as initially presented in
Egido and Smith (2017).

CORALv2 is based on SAMOSA+ (Dinardo et al., 2018) and adds further extensions to
mitigate interference that arises from strongly reflective targets in the across-track direction, as
is typical in the coastal zone. Furthermore, a better quality flag allows for an over 25% increase
in valid estimates closer than 5 km from the coast compared to SAMOSA+ (Schlembach et al.,
2022). CORALv2 has had the following modifications made to it with respect to its first published
version, v1: The adaptive interference mitigation scheme is adjusted such that interference that
arises in front of the leading edge (LE) is also sensed and masked out for the least-square
fitting process. Moreover, the spurious interference gates are excluded from the computation of
the misfit between the fitted, idealised and received waveform, from which the quality flag is
deduced. Another modification is the consideration of the range migration correction (RMC)
mode that has been activated on-board from S6-MF cycle 33 to accommodate the data volume
to be transferred to the ground, which truncates the first ten and roughly the second half of each
multilooked waveform (thus reducing the data rate by a factor of two) (Donlon et al., 2021).
In these cases, only the range gates ranging from 11 to 132 (0-based) are fitted against the
SAMOSA2 model (EUMETSAT, 2022b).

We retrack the different datasets from Table 1 (apart from PDAP-HR) with CORALv2. The
FFSAR-60 and FFSAR-140 are retracked in their corresponding posting rates of 60- and 140 Hz,
respectively. For the sake of comparability of the different datasets and the concurrent exploita-
tion of potential gains, we reduce the FFSAR-60 and FFSAR-140 datasets to 20 Hz by taking
the mean of all estimates around the location of the centre estimate, which coincides with the
baseline L2 location, as defined during the multilooking process described in Section 3.1.1. In the
reduction process, we discard the higher posting rate estimates of 60- and 140 Hz that exhibit a
bad quality flag to exploit the high FF-SAR resolution.

After retracking and reducing the data, we filter out outliers by applying the scaled median
absolute deviation (MAD) factor criterion (Alvera-Azcárate et al., 2012; Schlembach et al., 2020;
Passaro et al., 2021). An estimate is seen as an outlier if its value exceeds the range of median
±3 · 1.4826 · MAD, where median and MAD are calculated on the adjacent 20 records, and
the factor 1.4826 converts the MAD to a standard deviation equivalent for normally distributed
data. In total, 743/18489 (4.0%), 716/18489 (3.9%), and 638/18489 (3.5%) SWH estimates are
removed from the FFSAR-60, FFSAR-140 and UFSAR-20 datasets, respectively. These numbers
are in line with the amount of the scaled MAD criterion-detected outliers found in the Round
Robin retracker comparison in Schlembach et al. (2020) for the baseline SAMOSA-based retracker
(3–5%) in the coastal zone with a dist-to-coast of less than 20 km.

3.2. Statistical Analysis

We divide the statistical analysis into two parts: First, we compare the L2 datasets with the
SWAN-Kuststrook wave model and assess Pearson’s correlation coefficient, the median offset, and
the percentage of cycles for high correlation (PCHC). The correlation is a statistical measure
of the linear relationship between two collocated datasets ranging from -1 to 1. A concurrent
increase/decrease in both thus yields a positive correlation. The median offset is defined as
median(SWH_{L2} − SWH_{model}) and is chosen to determine the accuracy of the dataset with respect
to the wave model. The PCHC is a statistical metric to assess the quality of the records on a
per-cycle-basis, which was developed for the collocation of altimetry data with in-situ data by
Passaro (2015). It evaluates the number of cycles that show a high correlation with another
collocated reference (here, we use the SWAN-Kuststrook wave model) and puts it into relation
to the total number of cycles. Schlembach et al. (2022) assessed a correlation coefficient of
0.82 for a dist-to-coast of less than 5 km for CORALv1 vs a global ERA5-based wave model.
We thus consider a correlation of ≥0.8 as high. The procedure for the computation of the
PCHC is established iteratively: First, the correlation between all altimeter-model record pairs
is computed. If it is below 0.8, the correlation between all altimeter-model pairs is computed for
each cycle individually, and the cycle with the poorest correlation is discarded. This procedure
is repeated until the correlation of all remaining altimeter-model pairs is greater than or equal
to 0.8. The PCHC is thus given as the ratio between the number of remaining cycles and the
total amount of cycles and amounts to 100% in the optimal and 0% in the worst case.

The second part of the statistical analysis evaluates the number of valid records and the L2 noise. The number of valid records is based on the quality flag, which indicates whether an estimate is good or bad and is provided as a product of the retracking algorithms by each of the L2 datasets. For the CORALv2-retracted L2 datasets FFSAR-140/60 and UFSAR-20, the quality flag is given by checking whether the accumulated differences (=misfit) between the bins of the received waveform and the idealised, fitted waveform exceed an empirical threshold value of 4 while excluding the bins that are affected by coastal interference. For further details, refer to Schlembach et al. (2022). The L2 noise is defined as the root-mean-square difference between consecutive 20 Hz measurements, written as

\[ n_{L2} = \sqrt{\frac{\sum_{i=1}^{N} (SWH_{i+1} - SWH_i)^2}{N}} \]  

where \( N \) is the number of records considered for the computation of the L2 noise.

The statistical quantities are computed as a function of dist-to-coast bands, which are chosen as follows: 0 ≤ dist-to-coast < 1 km, 1 ≤ dist-to-coast < 3 km, 3 ≤ dist-to-coast < 5 km, and 5 ≤ dist-to-coast < 10 km (short-hand-noted as 0–1, 1–3, 3–5, 5–10 km).

3.3. Coastal SWH Variation

We define the change in SWH from offshore towards the coast as the coastal SWH variation. To estimate the coastal and offshore wave heights, we take the median SWH of the two coastal 1–3 km and 5–7 km and the offshore 29–31 km dist-to-coast bands, respectively. The choice of the coastal 5–7 km band and the offshore 29–31 km bands are based on the work of Passaro et al. (2021), where the first valid, 1 Hz SWH estimate is selected for the calculus of the coastal SWH variation after discarding the records for the first three kilometres.

The coastal SWH variation ratios \( \Delta_{2-30} \) and \( \Delta_{6-30} \) are given by

\[ \Delta_{2-30/6-30} = \left(1 - \frac{\text{median}(SWH_{1-3/5-7})}{\text{median}(SWH_{29-31})}\right) \times 100 \]  

where \( SWH_{1-3/5-7/29-31} \) are the SWH estimates in the corresponding dist-to-coast bands.

We perform the coastal SWH variation analysis for passes 18, 120, and 196 only, as passes 44 and 213 do not include (collocated) data at a dist-to-coast of around 30 km.

4. Results and Discussion

4.1. Statistical Analysis

In this section, we present the results of the statistical analysis, which are summarised in Figure 2. The column panels of Figure 2 correspond to the statistic metrics: correlation, number of valid records, median offset, PCHC, and L2 noise. The row panels correspond to the statistical quantities in total and for each of the individual passes.

We first compare the altimetry datasets with the SWAN-Kuststroom wave model and assess the correlation, the median offset, and the PCHC. Secondly, we evaluate the intrinsic quantities of the number of valid records and the L2 noise.

4.1.1. Comparison with the SWAN-Kuststroom Wave Model

Correlation From Figure 2 (a), we observe the highest correlation >0.8 between the FF-SAR altimetry and wave model for up to 1 km from the coast, which indicates an increased consistency
between both datasets and suggests an improvement since both datasets are independent. FF-SAR shows slightly greater similarities to the wave model than UF-SAR (1–3 km band: FFSAR-140: 0.82, UFSAR-20: 0.66). While showing a high similarity, the altimetry data might exhibit an offset with respect to the wave model. The assessment of the median offset is evaluated after the analysis of the correlation.

However, for closer than 1 km from the coast, these improvements inevitably depend on the altimeter measurement geometry and are hence more or less pronounced depending on the individual satellite track. Passes 120 and 196 show the least amount of land intrusion in the last few footprints closest to the coastline and thus show the highest correlation with the SWAN-Kuststrook wave model. Moreover, it is noticeable that both FFSAR-140/60 datasets show a better correlation than UFSAR-20 for pass 120. This might be due to the spurious interference that arises from strongly reflective targets in the along-track direction, which FF-SAR might be better capable of resolving due to its inherently high along-track resolution of ∼1 m. This phenomenon will be presented and further discussed in Section 4.2.2.

In general, pass 44 shows deteriorated correlations between all altimetry datasets and the wave model compared to the residual passes. This indicate inaccuracies in the wave model, for which pass 44 lies at the left-most edge of the model domain where modelled data is strongly affected by the boundary conditions from the coarse-grained ECMWF-WAM model.

**Median offset** With the analysis of the median offset, we address how accurately the altimetry datasets estimate SWHs with respect to the SWAN-Kuststrook wave model as a function of the dist-to-coast bands. In the optimal case, no offset should be present. If this is not the case, then a constant offset for different values of dist-to-coast between both is desirable since other metrics can also be compared, e.g. the analysis of the coastal SWH variation, as presented in Section 4.3. A discussion of systematic offsets between the altimetry datasets and the wave model with respect to the open ocean segments of the study (dist-to-coast ≥20 km) and different sea states is given in Section 4.2.

From Figure 2 (c), we observe that all altimetry datasets exhibit higher SWHs than SWAN-Kuststrook. The FF-SAR-processed datasets exhibit, across all passes, a median offset of ∼32 cm for up to 3 km from the coast and ∼27 cm for closer than 3 km from the coast. UFSAR-20 shows a similar offset behaviour towards the coast but ∼13–14 cm lower in magnitude. The offsets for dist-to-coast closer than 1 km from the coast are relatively constant for FF-SAR, whereas there are greater variations for UF-SAR. That is, with respect to the wave model, FF-SAR is capable of estimating SWHs more accurately for closer than 1 km from the coast than UF-SAR and as accurate for up to 3 km from the coast.

The difference in offsets between FF-SAR and UF-SAR is as expected and due to the fitting of the FF-SAR-processed waveforms against the SAMOSA2 zero-Doppler beam that was generated with a so-called unambiguous PTR approximation (European Space Agency, 2021). The used α_p LUT was thus generated under the assumption of an ideal PTR without considering any grating lobes (Ehlers et al., 2022), which might cause parts of the additional offset. Another part of the offset might be caused by the fitting of the SAMOSA2 zero-Doppler beam itself and the stronger dependence of FF-SAR on vertical wave velocities (Buchhaupt et al., 2021). If the sea surface were static, then the SAMOSA2 zero-Doppler beam waveform would be an appropriate model function (Ehlers et al., 2022). With increasing vertical velocities, the scatterers’ signal is moved in the along-track direction and smeared in range such that the waveforms are widened, which causes an overestimation of SWH.

**Percentage of Cycles with High Correlation** The PCHC represents the ratio of the cycles that show a high correlation of greater than or equal to 0.8 and the total number of cycles, as described in Section 3.2. In Figure 2 (d), the PCHC across all passes is shown. The PCHC is related to the correlation shown in the left panels of Figure 2, which is evaluated over all
Figure 2: Statistical analysis of the SWH estimates for the FFSAR-60, FFSAR-140, UFSAR-20 and PDAP-HR datasets for all and each of the individual passes. The column panels show the Pearson correlation coefficients, the number of valid records, the median offset, PCHC and L2 noise in the dist-to-coast bands 0–1, 1–3, 3–5, and 5–10 km, respectively. The row panels of the plots correspond to all passes, pass 18, 44, 120, 186, and 213, respectively.

collocated altimeter-wave model records, whereas the PCHC considers the correlations of the collocations cycle-wise. That is, if the correlation values of a dist-to-coast band are close to 0.8, the PCHC value will also be high, as some cycles might exceed a correlation value of 0.8, while others do not. If all cycles exceed a correlation of at least 0.8, the PCHC value will be 100%.
We observe that up to 3 km from the coast, all CORALv2-retracked datasets show that all cycles are highly correlated, i.e., with correlations of $\geq 0.8$ (apart from pass 44, from which we assume that the wave model is inaccurate). Approaching the coast yields a decrease in correlation, which corresponds to a decrease in the PCHC. FF-SAR shows, across all passes, higher PCHC values in the 1-3 km dist-to-coast band than UFSAR-20 (100% vs 76%), which is due to pass 213 whose footprints are highly affected by strongly reflective targets such as sandbanks. The PCHCs of the 0-1 km dist-to-coast band vary strongly between the individual passes, which is caused by the varying correlations of each pass. As for the correlations, the FF-SAR variants show the highest PCHC scores and, thus, the highest degree of similarity with the SWAN-Kuststrook wave model.

4.1.2. Quantity and Precision

The quantity and precision of the altimetry data are analysed by the number of valid records and the L2 noise, as described in Section 3.2. Both the number of valid records and precision are intrinsic metrics that do not require any external data and serve as complementary metrics for the statistical analysis vs the SWAN-Kuststrook wave model. Both measures have a substantial impact on the uncertainty of the estimates. A higher number of valid records yields more independent measurements to reduce the overall uncertainty and allows us to resolve features, such as spatial gradients in SWH when approaching the coastline, at smaller scales. Lower L2 noise values are a direct measure of the variability of the along-track estimates and likewise correspond to a lower uncertainty for each of the estimates.

**Number of Valid Records**  For up to 3 km from the coast, 95–100% are seen as good estimates for all CORALv2-retracked products across all passes. For a dist-to-coast closer than 3 km, FF-SAR exhibits more valid estimates than UF-SAR (1-3 km band: FFSAR-140: 79%, UFSAR-20: 49%). That is, FF-SAR better resolves spatial gradients in SWH and exhibits lower uncertainties, which is shown in the coastal SWH variations, as presented in Section 4.3.

The dependency on individual passes can also be seen in the number of valid records. They are coupled with the correlation of the passes, i.e., passes that show a deteriorated correlation likewise exhibit a decreased number of valid records in the corresponding dist-to-coast bands (e.g., pass 18, 0-1 km; pass 44, 1-3 km; pass 213, 1-3 km).

The number of valid records strongly depends on the passes and thus on the angle of approach of the satellite towards the coastline. The more the footprints in front of the coastline are affected by land intrusion, the fewer records are indicated as good estimates, and at the same time, show a deteriorated correlation with the wave model. For instance, this can be observed for pass 120, whose footprints are least affected by land (see Figure 1 (d)) and which shows the highest number of valid records with the highest correlation. In contrast, pass 213, whose footprints are strongly affected by sandbanks and land (see Figure 1 (f)), shows reduced numbers of estimates (FFSAR-140: 41–66%) and decreased correlations (FFSAR-140: 0.69/0.84 for the 0–1/1–3 bands).

**L2 Noise**  The rightmost column panels of Figure 2 show the estimated L2 noise of the datasets, as described in Section 3.2. Moreover, Figure 3 shows, in addition, the furthest offshore dist-to-coast band of 10–30 km and the gain in precision from FFSAR-140 to UFSAR-20.

The gain in precision between FF-SAR and UF-SAR is remarkable. Between FFSAR-140 and UFSAR-20, it amounts to 11-15 cm throughout the dist-to-coast bands, corresponding to a relative gain of 29–43%. The differences between the two FF-SAR variants are not significant.

When approaching the coastline from offshore to the coastline, the L2 noise gradually increases from $\sim 20$ cm at 10-30 km to $\sim 30$ cm at 1-3 km from the coast, which is attributed to individual estimates that are affected by coastal interference.
With respect to the individual passes, we find that the L2 noise level slightly varies: Pass 120, with the least intrusion of land, shows no significant increase in noise up to the coastline. Other passes that are more affected by land and strongly reflective targets, such as 196 and 213, show an increased noise level for a dist-to-coast of less than 3 km.

The noise level estimates that we find here are in line with the ones that were estimated for the UF-SAR retracking algorithms and S3 in Schlembach et al. (2020). Although they were estimated for a very large dataset and on the basis of the standard deviation of twenty 20 Hz measurements along a 1 Hz along-track distance, they likewise range for average sea states from 30–35 cm and >40 cm for the open ocean and the coastal zone, respectively.

![Figure 3: L2 noise for the different dist-to-coast bands, as shown in Figure 2 (e), but ranging from offshore at 10–30 km down to 0–1 km. In addition, the gain in precision of FFSAR-140 over UFSAR-20 is shown.](image)

In the rest of this work, we proceed with the analysis of the FFSAR-140 and UFSAR-20 datasets for the sake of simplicity.

### 4.2. Dissimilarities between Altimetry and the SWAN-Kuststrook Wave Model

In this section, we investigate the dissimilarities between the altimetry datasets and the SWAN-Kuststrook wave model. We first analyse systematic offsets between both and then look at a specific case where we observe an increase in SWH in the last 1–2 km from the coast.

#### 4.2.1. Systematic Offsets

In the statistical analysis in Section 4.1.1, we find offsets between the altimetry data and the SWAN-Kuststrook wave model that are mostly positive, i.e. the altimetry datasets systematically overestimate SWHs with respect to the wave model. As described in Section 2.2, the validation of the SWAN-Kuststrook wave model was performed in a hindcast-based analysis of four extreme events against over 50 in-situ sites, which showed only a small relative bias of -1%.

The sea-state-dependent overestimation of SAR-derived SWHs with respect to in-situ and conventional LRM-processed altimetry data has been shown by Moreau et al. (2017, 2018), and Abdalla et al. (2018) for CS2 and in Moreau et al. (2017) and Raynal et al. (2018) for S3. Since then, it has been shown that the effect is less apparent for longer-period (swell) waves and mainly comes from wave motions (Amarouche et al., 2019; Egido and Ray, 2019; Buchhaupt, 2019). According to the S6-MF mission performance working group, the bias between the PDAP-HR and the PDAP-LR products of the EUMETSAT baseline F06 are linked to vertical wave
velocities, which shows ∼10 cm higher SWHs for SWH = 1 m, and ∼20 cm higher SWHs for SWH = 2 m (EUMETSAT, 2022a; Martin-Puig et al., 2022). In Section 4.1.1, an additional offset between FF-SAR and UF-SAR found to amount to 13–14 cm. Parts of this mismatch are believed to be linked to different sensitivity of FF-SAR and UF-SAR to vertical wave motion (Buchhaupt et al., 2021). To account for the effect of vertical wave motions and the induced SWH bias, a LUT was proposed by Egido et al. (2022) that applies a sea-state-dependent SWH correction, which is planned to become operational for S6-MF baseline F09 in Q3 2023 (Scharroo et al., 2022). More recently, Buchhaupt et al. (2022) found that the HR-LR inconsistencies also originate from horizontal surface velocities that are caused by current, wind-induced movement, and swells and propose a 2D retracking scheme, which is capable of estimating both vertical wave-particle and along-track surface velocities along with the other three geophysical estimates. Based on simulations shown in Buchhaupt et al. (2022, Slide 27), the SWH bias due to horizontal surface velocities amounts to up to 4.5 cm, depending on the wind speed.

The effect of vertical wave velocities are similarly represented in our analysis: The offsets of the altimeter datasets, including the PDAP-LR product to SWAN-Kuststrook, are shown as a function of SWAN-Kuststrook SWH in Figure 4 (a), which exhibit a dependency on the sea state. SWAN-Kuststrook underestimates the SWH with respect to the PDAP-LR product by about 5–10 cm in the range of SWH values, which is relatively constant for an SWH of up to 2 m (in between most of the SWAN-Kuststrook estimates range). The magnitude of the offset between the PDAP-HR and PDAP-LR datasets is within the range that is shown in EUMETSAT (2022a, Figure 3). The stronger variations of the offsets for SWHs larger than 2 m likely arise due to the fewer estimates in this sea state region, which yields a poorer statistical representation.

Figure 4 (b) shows the probability density function (PDF) of the SWAN-Kuststrook SWHs in the offshore part of the considered area (dist-to-coast ≥ 20 km), showing a median SWH of 1.03 m. Figure 4 (c) depicts the median offset of the 5–10 km, 10–20 km, and 20–30 km dist-to-coast bands. The median offsets of the 20–30 km band amount to 42 cm and agree with the ones that can be seen from the differences between SWAN-Kuststrook and the individual datasets in Figure 4 (a), considering a median SWH of ∼1.0. The quality of the PDAP-LR estimates is too poor to analyse the nearshore offsets closer than 10 km from the coast.
4.2.2. Increase in Significant Wave Height Estimates

We find that a significant number of the individual overpasses show increasing SWH estimates in the last 1–2 km from the coast, as depicted exemplarily in Figure 5 (b) for the overpass of cycle 40 and pass 120. The increase is apparent for both the FFSAR-140 and UFSAR-20 datasets, while it is more significant for UFSAR-20 in both the intensity (SWH increase from below 0.5 m to almost 1.5 m) and the dist-to-coast of ~2 km. For FFSAR-140, the increase in SWH is up to ~0.9 m, and it stretches to ~1.5 km off the coast. The reason for the increase is explained by an extraordinarily strong reflective target, which is the straight sandbank at the defined coastline of pass 120 and the absence of any other land intrusions within the footprint, as shown in Figure 5 (a). This is visualised by the multilooked echo power radargram in Figure 5 (c) and (d) for FF-SAR and UF-SAR (with a posting rate of 140 Hz), respectively. The grating lobes of the S6-MF along-track PTR (Ehlers et al., 2022, Figure 6, Panel F), which are induced by the strong signal components of the sandbank interferer, can be well identified at distances of multiples of ~300 m off the coastline. The bow-tie-like pattern can also be recognised as the power is increasingly smeared over more range gates for waveforms that are further away from the sandbank. The power of the closely located grating lobes is concentrated more in the LE of the waveforms at range gates around bin ~100. This strongly deteriorates the SWH estimates in the first 1–2 km off the coast.

To determine how many overpasses are affected by an increase in SWH in the last three kilometres from the coast, we apply the following empirical constraint:

\[
\max(SWH_{0-3}) > \max(SWH_{3-5} + n_{L2})
\]  

where \(SWH_{0-3/3-5}\) are the estimated SWHs for the 0–3/3–5 km dist-to-coast bands and \(n_{L2}\) the estimated L2 noise, being set to 0.2 m and 0.3 m for FF-SAR and UF-SAR and 0 for SWAN-Kuststrook, respectively.

We apply Equation (3) to the 138 overpasses (excluding pass 44) for the FFSAR-140 and UFSAR-20 datasets and compute the (sample) mean probability of occurrence of an SWH increase for each of the individual passes, which is shown in Figure 6. FFSAR-140 tends to be less
affected by the SWH increase. However, the margin of error, corresponding to a 95% confidence interval, is quite large, with up to 17.5%, and hence no safe conclusion can be drawn for passes 18, 196, and 213. Pass 120, though, represents an exception, as FFSAR-140 shows a strongly reduced mean probability for an SWH increase of 9.7%±10.4%, as compared to UF-SAR with 52.8%±17.2%. The SWAN-Kuststrook wave model shows an increase of (only) up to 8 cm for one overpass of passes 18 and 120, none for pass 196, and in 19.4%±6.2% of the overpasses for pass 213.

A check for an increasing SWH in SWAN-Kuststrook (max(SWH_{0–3}) > max(SWH_{3–5})) reveals an increase of up to 8 cm for 10 out of the 138 cycles (6.5%±4.1%), whereas pass 213 is affected most (8), and passes 18 and 120 only once.

![Figure 6: Mean probabilities of occurrence for an SWH increase from 3–5 km to 0–3 km from the coast by applying Equation (3). The error bars indicate a 95% confidence interval.](image)

4.3. Coastal SWH Variation

The computed mean coastal SWH variations $\Delta_{6–30}$ and $\Delta_{2–30}$ of the FFSAR-140 and UFSAR-20 datasets for the passes 18, 120, and 196 are shown in Figure 7 (a) and (b), respectively. We exclude overpasses that exhibit low sea states of less than 0.5 m (according to SWAN-Kuststrook) since the altimetry data is dominated by L2 noise in this sea state region.

All coastal SWH variations are positive, i.e. the SWHs decay towards the coastline. We observe that both FF-SAR and UF-SAR estimate the decays with respect to the 5-7 km band with no significant differences. In the 5-7 km band, both FFSAR-140 and UFSAR-20 datasets are close to the decays that are estimated by SWAN-Kuststrook (FFSAR-140: 17.4%±2.5%, SWAN-Kuststrook: 15.9%±2.2%).

However, there are more significant differences between FF-SAR and UF-SAR for the 1-3 km band: UFSAR-20 strongly underestimates the mean decay for pass 18 and also shows a large standard errors that imply a large uncertainty of the estimated variations. FFSAR-140 is, in contrast, very close to the decays of the wave model and shows a decay of 26.4%±3.1%.

We argue that the difference between FF-SAR and UF-SAR is explained by the differences in their 2D-PTRs. For UF-SAR, it is a sinc$^2$ with a 3-dB width of ~300 m, which causes the reflected power of a single point scatterer to be smeared in this distance in both the along- and across-track direction in a bow-tie-like pattern (Ehlers et al., 2022, Figure 3, Panel B). The 2D-PTR of FF-SAR is instead much peakier, with a width of ~1 m in the along-track direction, i.e. the main reflected power is integrated over a much smaller distance in the along-track direction at the actual location of the point scatterer (the minor grating lobes yield only ~1% of the total,
reflected power) (Ehlers et al., 2022, Figure 6, Panel F). We thus argue that FF-SAR is more capable of resolving (static) small-scale interferers and estimating SWHs more accurately for a dist-to-coast of less than 3 km.

![Figure 7: Mean coastal SWH variations between the SWH between the 29–31 km dist-to-coast band and the 5–7 km or the 1–3 km dist-to-coast bands in (a) and (b), respectively, for the datasets FFSAR-140 and UFSAR-20. The error bars correspond to the 95% confidence interval.](image)

Passaro et al. (2021) found that the global mean coastal SWH variation at >3 km from the coastline, corresponding to our 5–7 km dist-to-coast band, is 22% with respect to the offshore SWH at 30 km. However, strong variations have been assessed for 14 different regions of the global coastal ocean (Reguero et al., 2015), which show a mean value of 17.2%±3.4%. For the Northern and Western Europe region, a decay of 22.41% was evaluated, with an average offshore sea state of SWH = 2.23 m and most of the areas being exposed to an open ocean with a higher ratio of swells of higher wavelengths. That is, considering a lower median SWH value of 1.03 m (from Figure 4) and the exposure of the milder North Sea, the overall variation we have estimated with the FFSAR-140 dataset is for the 5–7 km dist-to-coast band within an expected range of 17.4%±2.5%.

5. Conclusion and Future Work

In this work, we have conducted an extensive coastal case study to assess the applicability of FF-SAR-processed S6-MF coastal altimetry data to obtain SWHs. The data included 161 overpasses from five passes, covering the Dutch coast and the German coast along the East Frisian Islands in the North Sea, and 38 cycles, corresponding to the year 2021. Two FF-SAR-processing configurations with the 60/140 Hz L1b posting rates and one UF-SAR-processing configuration, UFSAR-20, with a 20 Hz L1b posting rate were used to process L1a data from EUMETSAT to acquire SWH estimates after the retracking process with the coastal retracking algorithm CORALv2.

The processed altimetry datasets, and the baseline PDAP-HR product from EUMETSAT, were compared with the coastal, high-resolution SWAN-Kuststrook wave model from the operational RWsOS operational forecasting system to assess the performance of the altimetry datasets. The FFSAR-140 dataset exhibits the highest similarity to the model, showing a correlation coefficient of ~0.8 at 45% of valid records for the 0–1 km band and 80% of valid records for the 1–3 km band. All passes, except pass 44, where the model might give inaccurate estimates, show PCHC scores of 100% from 1 km off the coast, i.e. for all cycles, a correlation coefficient of greater than or equal to 0.8 is estimated. The baseline PDAP-HR product shows strongly deteriorated correlations and a smaller number of valid records for a dist-to-coast of less than 10 km, e.g.
a correlation of $\sim$0.45 at $\sim$50% of valid records for the 1–3 km band for all passes. We have observed that the correlation and number of valid records can be further improved if the L1b posting rate is increased for the FF-SAR-variants from 60 to 140 Hz without any sacrifice in precision.

The FF-SAR datasets show an L2 noise of $\sim$20 cm in the open ocean segments and $\sim$31 cm for closer than 3 km from the coast, whereas UFSAR-20 exhibits L2 noise levels of $\sim$31 cm and $\sim$43 cm, respectively. That is, FF-SAR achieves a gain in precision of $\sim$37% and up to $\sim$29% in the open ocean and closer than 3 km off the coast. The PDAP-HR product shows similar L2 noise values as UFSAR-20 for more than 5 km from the coast, and increasingly higher values towards the coast of more than 82% for closer than 3 km off the coast, respectively.

We have also identified dissimilarities between estimates of the altimetry datasets and the SWAN-Kuststrook, which are mainly a consequence of known issues related to SAR altimetry parameter estimation; see references in Section 4.2. Accordingly, we observed that all FF-SAR- and UF-SAR-processed datasets exhibit a positive offset with respect to the wave model with a median offset of 34 cm (5%-percentile: 17 cm; 95%-percentile: 66 cm). Major parts of the offset are known and are likely caused by the influence of vertical wave velocities that are specific to SAR altimetry processing (FF-SAR more than UF-SAR) (Buchhaupt et al., 2021). This has been shown by including the PDAP-LR from the baseline L2 product in the offset analysis. A much smaller offset of less than 10 cm was observed between the PDAP-LR dataset and the SWAN-Kuststrook wave model for low and average sea states of up to 2.0 m in SWH. The median offset to the model gradually decreases from $\sim$42 cm for 20–30 km from the coast to $\sim$26 cm for less than 1 km off the coast (for FF-SAR-140).

In order to exploit the nearshore SWH estimates of the altimetry dataset, we have investigated the coastal SWH variations, which quantify the change in SWH from offshore at 30 km to the two coastal dist-to-coast bands 5–7 km and 1–3 km. With the FFSAR-140 dataset, we observed a mean decay in SWH of 17.4%\(\pm\)2.5% and 26.4%\(\pm\)3.1% with respect to the 5–7 km and the 1–3 km dist-to-coast bands for the three S6-MF passes 18, 120, and 196. The decays for the 5–7 km band are within the expected range of the ones globally and regionally found in Passaro et al. (2021). We thus demonstrated that the FFSAR-140 processing-configuration is also capable of giving accurate estimates for the coastal SWH variation in regard to the 1–3 km band.

To summarise the results of the individual objectives of this study, we can draw the following conclusions:

**FF-SAR vs UF-SAR** FF-SAR SWH estimates were found to exhibit lower noise, resulting in increased correlation with the numerical wave model, and provide a higher number of valid records and highly correlated cycles, as compared to the UF-SAR estimates.

**High-quality SWH estimates from 1 km from the coast** This case study demonstrates that one can acquire robust high-frequency SWH estimates up to 1 km off the coast by the combination of FF-SAR altimetry, the coastal CORALv2 retracker, and the subsequent removal of residual outliers.

**Estimation of nearshore, coastal SWH variations** With the aforementioned FF-SAR-configuration, we are able to give accurate estimates with respect to a numerical wave model for the coastal SWH variation of up to 1 km from the coast.

The FFSAR-140 represents the processing configuration with the best performance but, at the same time, exhibits the highest amount of computational complexity. However, it must also be noted that the used FF-SAR back-projection processing methodology is not the most efficient one. Guccione et al. (2018) have proposed the omega-kappa FF-SAR processing methodology, which strongly reduces the computational efforts with negligible costs in performance.

As part of future work, we suggest the development of more advanced interference mitigation techniques. The suppressing of signals from static interfering targets might give an additional
gain for FF-SAR processing. The improvement of the quality flagging after multilooking at the higher posting rates provides additional gains in the robustness of the L2 estimates. We also suggest studying the difference between the FF-SAR- and UF-SAR-processed datasets in more detail to be able to characterise small-scale features such as breaking waves or shoaling effects that FF-SAR might be able to resolve.

Author Contributions


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A. Autocorrelation Analysis

Dinardo et al. (2015) and Egido et al. (2020) suggest increasing posting rates to more than 20 Hz as commonly used by the EUMETSAT baseline products. In this work, the authors assume that the decorrelation length of the radar echoes is much smaller in the along-track direction than the inherent unfocused synthetic aperture radar (UF-SAR) along-track resolution of ∼300 m. Hence, depending on the sea state, a precision gain of 20–30% can be achieved for the geophysical estimates if the posting rates are increased to 40 or 60 Hz and then averaged to form 20 Hz estimates.

We have analysed the autocorrelation function (ACF) of different processing options by considering open ocean segments with a distance-to-coast (dist-to-coast) between 20 km and 30 km. We exclude those that show a larger standard deviation than 20 cm, 30 cm, and 50 cm for fully focused synthetic aperture radar (FF-SAR)-, UF-SAR- and low resolution mode (LRM)-processed datasets, respectively. We have added the two datasets, UFSAR-20 and Payload Data Acquisition and Processing Low Resolution (PDAP-LR), to assess their autocorrelations. The datasets with posting rates of more than 20 Hz are arithmetically averaged to yield the targeted 20 Hz posting rate. The ACFs of the first three lags for the different datasets are shown in Figure 8. Apart from UFSAR-60, all datasets exhibit no correlation between their adjacent records, as the ACF stays within the confidence interval of the standard error of white noise (Brockwell
and Davis, 1987). UFSAR-60 shows a correlation of ∼0.2 for lag $k = 1$. The resulting Level-2 (L2) noise, or precision, and the gain in precision over UFSAR-20 are shown in Figure 9 (a) and (b), respectively. No correlation is observed for the FF-SAR-processed datasets, not even for FFSAR-60 and FFSAR-140. UFSAR-20 shows a gain in precision of 25.3% over PDAP-HR. This is noticeable and in line with the numbers being reported by Egido et al. (2020), who estimated precision gains of 22% and 25% for posting rates of 40 Hz and 60 Hz. Nevertheless, we find that the increased precision of the geophysical estimates is, per se, not an actual gain but comes together with an added correlation between the reduced 20 Hz estimates. The subsampling of the 20 Hz estimates thus acts as a smoothing or low-pass filter, which smears the effective signal over the subsequent estimate. Consequently, we decided not to include any UF-SAR datasets with posting rates of larger than 20 Hz in this study to allow for a fair comparison of the individual analysed dataset.

Figure 8: Autocorrelation of the datasets FFSAR-60, FFSAR-140, UFSAR-20, UFSAR-60, PDAP-HR, and PDAP-LR in a-f, respectively. The light blue area for $k \neq 0$ indicates the standard error of white noise, which is approximated as $\sigma_n = \sqrt{N^{-1}}$, with $N$ being the number of estimates.

References


Figure 9: The L2 noise of the datasets FFSAR-60, FFSAR-140, UFSAR-20, UFSAR-60, PDAP-HR, and PDAP-LR is shown in (a). The gain in precision is shown relative to UFSAR-20 in (b).


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