Application of Aerial InSAR to Measure Glacier Elevations

Bryce Glenn¹, Andrew G. Fountain¹, and Delwyn Moller²

¹Portland State University ²University of Auckland

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Abstract

Glaciers and perennial snowfields are important to alpine ecosystems and regional hydrology. Quantifying volume change of a population of glaciers widely distributed over a region is difficult and expensive. We employed NASA's novel Airborne Glacier and Ice Surface Topography Interferometer (GLISTIN) to rapidly map surface topography of alpine glaciers across the western USA. In five flight days 3289 glaciers and perennial snowfields were surveyed. Comparison with lidar over control sites showed a mean difference of $+0.17 \pm 1.78$ m at a spatial scale of 3 m. Data coverage increased and elevation uncertainty decreased with the mosaicking of multiple passes due to the complex terrain. Elevation change since the National Elevation Dataset shows a thinning (and volume loss) over the last ~56 years, averaging -0.3 ± 0.2 m and accelerating since 1980. GLISTIN can be a valuable tool for rapidly mapping ice surfaces in the alpine environment.

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3 4 5	Bryce Glenn ¹ , Andrew G. Fountain ¹ , Delwyn Moller ²
6	¹ Department of Geology, Portland State University, Portland, Oregon, USA 97207
7	² Department of Electrical, Computer & Software Engineering, University of Auckland,
8	Auckland, New Zealand
9 10 11 12	Corresponding author: Andrew G. Fountain, andrew@pdx.edu
13	Key Points:
14	• Aerial InSAR can rapidly map the topography of alpine glaciers over a broad
15	region.
16	• Elevations compare favorably to lidar, $+0.17 \pm 1.78$ m at spatial scale of 3 m.
17	• The mean rate of glacier elevation change (specific volume) is -0.3 ± 0.2 m yr ⁻¹
18	for the past 56 years with rates increasing since 1980.
19 20	

21 Abstract

22

23 Glaciers and perennial snowfields are important to alpine ecosystems and regional 24 hydrology. Quantifying volume change of a population of glaciers widely distributed 25 over a region is difficult and expensive. We employed NASA's novel Airborne Glacier 26 and Ice Surface Topography Interferometer (GLISTIN) to rapidly map surface 27 topography of alpine glaciers across the western USA. In five flight days 3289 glaciers 28 and perennial snowfields were surveyed. Comparison with lidar over control sites showed 29 a mean difference of $+0.17 \pm 1.78$ m at a spatial scale of 3 m. Data coverage increased 30 and elevation uncertainty decreased with the mosaicking of multiple passes due to the 31 complex terrain. Elevation change since the National Elevation Dataset shows a thinning 32 (and volume loss) over the last ~56 years, averaging -0.3 ± 0.2 m and accelerating since 33 1980. GLISTIN can be a valuable tool for rapidly mapping ice surfaces in the alpine 34 environment.

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37

36 Plain Language Summary

38 Glaciers and perennial snowfields are important water sources to alpine ecosystems and 39 regional hydrology. To quantify their contribution their volume change is measured by mapping elevation changes of the ice surface. However, quantifying volume change for a 40 41 population of glaciers widely distributed over a region is difficult and expensive. We 42 employed NASA's airborne radar (GLISTIN) to rapidly map surface topography of 43 alpine glaciers across the western USA. In only five flight days 3289 glaciers and 44 perennial snowfields were surveyed. GLISTIN data over control-regions were compared 45 to lidar, an independent elevation measure using lasers, and showed small differences 46 indicating this method can be a valuable and cost-effective tool to track glacier change in 47 the future. Comparing the new elevations against historic elevations from USGS maps a 48 dramatic thinning (and volume loss) over the last ~60 years.

49

50 1. Introduction

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52 Glacier melt is important to runoff in high alpine landscapes. At a local scale, melting

53 glaciers maintain streamflow during the dry, late summer months after the seasonal snow

has melted (Fountain & Tangborn, 1985; Moore et al., 2009). Shrinking glaciers lose ice
volume and supply more water to streams and rivers than anticipated from precipitation.
Although this may be a temporary benefit, particularly in dry regions, their ability to
buffer seasonal runoff in future is reduced, making watersheds more vulnerable to
drought (Hall & Fagre, 2003; Moore et al., 2009). At a global scale, mass transfer of
water from storage as ice to water runoff increases global sea-levels (Meier, 1984; Pfeffer
et al., 2014; Zemp et al., 2019).

61

62 Traditionally, tracking glacier mass change was a field effort based on measuring the gain 63 and loss of snow and ice at points on the glacier (Kaser et al., 2003; Ostrem & Brugman, 64 1991). Although these efforts produce high-quality results showing spatial variations in 65 mass change across a glacier only a few glaciers can be so monitored by any agency (Andreassen et al., 2005; O'Neel et al., 2019). Remote-sensing methods can be used to 66 67 cover broad regions using an alternative approach that estimates mass change from 68 volume change. Differential interferometric synthetic aperture radar (InSAR) can map 69 surface elevation changes and offers the advantage of an all-weather, day/night 70 capability, a particularly valuable tool in often cloudy alpine environments (Rosen et al., 71 2000). Satellite-borne applications have revolutionized our understanding of Antarctica 72 and Greenland (Mouginot et al., 2019; Shepherd et al., 2018), and more recently, the 73 larger alpine glaciers (Millan et al., 2022). Challenges using InSAR include shadowing, 74 decorrelation due to layover, phase unwrapping, and temporal landscape changes 75 (Eineder & Holzner, 2000; Rees, 2000).

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Here, we test a novel approach for determining surface elevations on alpine glaciers using
an airborne single-pass InSAR, NASA's Glacier, and Ice Surface Topography
Interferometer (GLISTIN; Moller et al., 2017). Unlike differential/repeat-pass InSAR,
GLISTIN collects two radar images simultaneously, allowing elevations to be derived
from a single flight pass and are thus not sensitive to temporal decorrelation between
observations. Mounted on a jet aircraft, GLISTIN can image large areas in a short time
and has been used to map the relatively gentle topography of large glaciers and ice sheets

84	(Hensley et al., 2016; Moller et al., 2019). We evaluate its performance to map small
85	alpine glaciers in complex terrain across a broad region. In addition, the updated glacier
86	elevations are differenced from the National Elevation Data (Gesch, 2002) to calculate
87	glacier elevation change across the western US.
88 89 90	2. Data and Methods
91 02	2.1 Study Area
92 93	The study region is the American West, defined as the continental United States west of
94	the 100th meridian enclosing about $2x10^6$ km ² and home to about 5036 glaciers and
95	perennial snowfields ($\geq 0.01 \text{ km}^2$) as of the late 20 th century (Figure 1; Fountain et al.,
96	2017). The region is made up of three large mountain ranges, the Rocky Mountains, the
97	Cascade Range, and the Sierra Nevada. Many peaks exceed 4000 m in. The largest
98	concentration of glaciers, and lowest elevation (2000 m - 3000 m asl) is in the maritime
99	climate of the Pacific Northwest (Oregon, Washington, north-west Montana,). The
100	remaining glaciers are in continental climates elsewhere at high elevations, > 3000m.
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Figure 1. Map of glaciers and perennial snowfields (black dots) in the Western U.S. The
boxes show regions surveyed by GLISTIN.

106 Regional studies have shown drastic decreases in glacier area exceeding 50% over the

107 last century (DeVisser & Fountain, 2015; Fagre et al., 2017; O'Neel et al., 2019). The

- 108 rate of change has not been constant or spatially uniform (Basagic & Fountain, 2011;
- 109 Hoffman et al., 2007; O'Neal et al., 2015). Glacier volume changes, estimated by
- 110 differencing topography over time, show a loss on Mount Rainier, WA, of -0.65 km³,

- 111 average specific mass loss rate of -0.16 m w.e yr⁻¹ (1970 2007/2008; Sisson et al.,
- 112 2011). Menounos et al. (2018) estimated a volume loss of -127.65 ± 45.17 km³, $-0.42 \pm$
- 0.15 m w.e. between 2000 and 2018 for most of the glaciated terrain in Western NorthAmerica.

116 2.2 GLISTIN

117

118 GLISTIN is a Ka-band radar (8.4 mm, 35.66 GHz) system that utilizes two horizontally 119 polarized antennas, 0.25 m apart in elevation, both of which are capable of transmitting 120 and receiving (Moller et al., 2019). Unlike repeat-pass InSAR, GLISTIN's dual antennas, 121 collect data simultaneously. The Ka-band center frequency enables high accuracy with a 122 compact architecture and reduces snow penetration compared to lower frequencies. This 123 cross-track InSAR system is capable of providing not only the position of each image 124 point in along-track and slant range as with traditional SAR but also the height of that 125 point via the interferometric phase. Because the phase repeats after 2π , it must be 126 "unwrapped" to determine its unique location and height relative to a reference surface 127 (Moller et al., 2011; Rosen et al., 2000). The system is contained in an external pod 128 beneath NASA's Gulfstream-III aircraft with left looking view angles of 15-50° from 129 nadir. The system is coupled to inertial navigation and global position that provide pitch 130 and roll of the aircraft as well as its precise position in space. Nominal flight altitudes are 131 about 12,500 m above sea-level with a ground swath width of about 12 km and its typical air speed is 720 km hr⁻¹. 132

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134 To guide the aerial survey, the locations of the glaciers were retrieved from Fountain et 135 al. (2017). Flight passes were typically flown in pairs, each in an opposite direction, to 136 reduce gaps in backscatter from radar shadow or layover in the mountainous terrain. In a 137 few regions additional perpendicular flight passes were also flown. The georectified 138 height-maps from each pass were mosaicked into a 3-meter pixel-size digital elevation 139 model (DEM; Hensley et al., 2016) and projected into the Universal Transverse Mercator 140 (UTM) coordinate system. Self-reported elevation accuracy is 'height-precision', a 141 statistical estimate based on the interferometric correlation of each individual radar pixel

making up the 3 m mosaicked pixel (Moller et al., 2011). In the final mosaicked DEM, the elevation of each pixel is the weighted sum of elevations from individual passes and the weights are inversely proportional to the height-precision (Hensley et al., 2016). The vertical absolute uncertainty of GLISTIN-derived topography was found to be about \pm 0.30 m over bare non-snow-covered terrain (Schumann et al., 2016). Data collection and processing were provided by the Jet Propulsion Laboratory at California Institute of Technology, Pasadena, CA.

149

150 2.3 Accuracy 151

152 The accuracy of GLISTIN elevations was ground-truthed by differencing lidar DEMs 153 from GLISTIN DEMs (Table SOM2). All lidar data were converted from its native 154 coordinate system to WGS84 to UTM using Vdatum (Version 3.8, 2017, National 155 Oceanic and Atmospheric Administration, Washington, DC), inducing an error of about 0.076 m (self-reported by Vdatum during conversion) and resampled to 3 m to match the 156 157 GLISTIN DEMs spatial posting, using bilinear interpolation. To calculate elevation 158 change the ¹/₃ arc-second NED was converted to UTM (WGS84) using Vdatum and 159 resampled to 10 m using bilinear interpolation. GLISTIN and lidar elevations were also 160 resampled to 10 m using bilinear interpolation to match the NED. The relative accuracy 161 of GLISTIN, lidar, and the NED were inter-compared at four barren earth snow-free 162 control zones in the Cascade Range of Oregon and Washington where all three estimates 163 of elevation were available. Each control zone is a patchwork of co-located but isolated 164 terrains. Barren earth terrains were derived from the 'barren' class of the 2016 National 165 Land Cover Database (https://www.mrlc.gov/data/nlcd-2016-land-cover-conus). 166 GLISTIN's performance imaging ice/snow surfaces was examined by comparing 167 elevations to lidar data acquired on Mount Adams, Washington, which was flown 28 168 days prior to the GLISTIN flights. We expect GLISTIN to yield somewhat lower 169 elevations due to melting of the snow and ice.

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171

173 2.4 Area and Volume Change

- 174 The reference area and elevation of the glaciers and perennial snowfields are derived 175 176 from (Fountain et al., 2017) and a 'historic' version of the NED (Gesch et al., 2002), 177 respectively. Both are based on the original U.S. Geological Survey 1:24000 topographic 178 maps from which the glacier outlines and elevations were derived. The maps in the 179 western US were drawn over a period of years (1940s-1980s. Resolution of the NED is $\frac{1}{3}$ 180 arc-second (~10 m), and the horizontal and vertical coordinate systems are North 181 American Datum of 1983, North American Vertical Datum of 1988, respectively. The 182 NED is continually being updated and it was necessary to retrieve the original 'historic' 183 version from multiple sources (Table SOM1).
- 184

185 Volume change was estimated by differencing the GLISTIN elevations from the NED 186 elevations within the original perimeter and for only those glaciers with $\geq 80\%$ GLISTIN 187 coverage. Le Bris and Paul (2015) showed that good estimates of volume change can be achieved with the elevation postings cover at least 80% of the glacier area. Reasonable 188 189 estimates of volume change can be obtained for coverages as low as 40%, however 190 results depend on interpolation method (McNabb et al., 2019), so we adopted the more 191 conservative threshold of 80% used by Le Bris and Paul (2015). In order to compare 192 volume loss between large and small glaciers and because the historic mapping occurred 193 over a time-span of decades across the western US, results are expressed as the rate of specific volume (volume/area) change (m⁻³ m⁻² yr⁻¹ or m yr⁻¹). 194 195

196 Uncertainty of volume change, $\sigma_{\Delta V}$, is calculated for each individual glacier or perennial 197 snowfield, using the vertical and area uncertainties (Menounos et al., 2018),

198
$$\sigma_{\Delta V} = \sqrt{\left(\sigma_{\Delta z} A_g\right)^2 + \left(\sigma_A \Delta z\right)^2}, \qquad (1)$$

199

where $\sigma_{\Delta Z}$ is the RMSE of elevation differences between GLISTIN and the NED for all barren earth control zones, for the region in which the glacier or perennial snowfield is located, A_g is the original (historic) area of the glacier or perennial snowfield, Δz is the







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fraction of area mapped by GLISTIN. Initial area refers to the area from the U.S.

222 Geological Survey's 1:24000 map series. The x-axis value is the maximum for each bin.

224 225 As expected, increasing the number of flight passes over the same area increased the 226 backscatter coverage. For one flight pass backscatter was received from 17% of the entire 227 illuminated area, for two flights 66%, four flights, 86%, and for eight flights 94% (Table 228 SOM3). No significant difference was observed in backscatter coverage of snow/ice 229 surfaces compared to ice-free surfaces, and within glaciers no significant differences 230 between snow-covered regions and ice-exposed regions. Backscatter reception was only 231 significantly correlated with terrain slope with greater loss on steeper slopes. 232

233 3.2 Accuracy

234 235 The GLISTIN DEMs for three of the four barren earth control zones were compiled from 236 multiple passes. The fourth control zone (Mount Adams, WA) was comprised of single 237 pass data and was examined separately. For the three multi-pass barren earth control 238 zones the GLISTIN – lidar (3 m posting) mean difference was $+0.17 \pm 1.78$ m (Table 239 SOM4). Comparing GLISTIN and the NED over the same regions (10 m posting), the 240 mean difference and standard deviation was much larger, $\pm 1.05 \pm 6.38$ m. This is due to 241 the much larger uncertainty in the NED elevations of 3.74 m, which is based mostly on 242 control points located in lower elevation and less complex terrain (Gesch, 2007). The 243 mean lidar-NED difference -0.89 ± 5.83 , supports this inference. For the control zones on 244 Mount Adams, the mean elevations difference of single-pass GLISTIN - lidar (3 m 245 posting) was -0.00 ± 3.20 m, whereas for the snow/ice surfaces it was -0.86 ± 3.76 m. 246 The negative difference for the snow/ice surfaces is to be expected given the melting that 247 occurred over the 28-day period between the initial lidar survey followed by the 248 GLISTIN survey. Given that the snow is wet during this time of year and interferometric 249 penetration is negligible (Hensley et al., 2016).

With respect to interferometric radar errors it is important to note that the height precision is dominated by the instrument random noise. This relative error is high frequency and will scale with spatial averaging of uncorrelated pixels or independent samples. The same is not true for the height accuracy or systematic (mean) offset which does not 254 improve with averaging as they are correlated. Therefore, if we calculate the RMSE for 255 more coarse spatial postings this metric will reduce significantly (with the random 256 /precision inversely proportional to the square-root of the effective number of 257 independent looks (Hensley et. al. 2016). For this paper we analyze GLISTIN data at a spatial posting of 3m due to the small footprint of many of these glaciers. However, one 258 259 can expect significantly improved height precision, and thereby RMSE for large glaciers 260 via spatial averaging. The low mean difference (i.e. accuracy) observed for the barren 261 areas indicates that extremely low height errors are achievable with sufficient spatial 262 averaging to reduce the random component (Schumann et. al. 2016; Moller et.al. 2019)

263 Although no correlation was observed between mean elevation difference (GLISTIN -

lidar) and surface slope, the standard deviation increased from about 1.7 m for slopes

between 20° and 30° to 3.8 m for slopes between 50° and 60°. The RMSE (GLISTIN-

NED) increased from 6.1 m for slopes 20° to 30° to 10.2 m for slopes between 50° and

 $267 \quad 60^{\circ}$. The rate of phase change is a function of the interferometric measurement geometry

and is directly proportional to the local slope. Phase unwrapping becomes more difficult

as the slope increases so an increased RMSE in extreme topography is to be expected.

270 The orientation of single-pass GLISTIN relative to the terrain surface affects the

271 elevation difference. The mean elevation difference (GLISTIN-lidar) was smaller for

surfaces facing towards GLISTIN, $+0.01 \pm 2.07$ m, than surfaces facing away, $+0.07 \pm$

273 4.03 m.

274 3.3 Volume change

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Volume change was estimated for 1770 glaciers and perennial snowfields (54% of total) consisting of 351 glaciers and 1419 snowfields. Overall mean uncertainty, based on barren earth control zones across the west (Table SOM5), was -0.37 ± 7.31 m. Rejecting those specific volume changes that were smaller than uncertainty yielded 231 glaciers totaling 198.84 km² and 551 perennial snowfields (21.31 km²). Comparing our volume change to a prior estimate for Mt. Rainier, Washington (Sisson et al., 2011), showed that the prior estimate, based on a lidar-NED difference, of -8.6 m (1970-2007) is within the

- 283 uncertainty of our value, -9.7 ± 4.8 m (1970-2016). That our estimate showed a greater 284 mass loss is consistent with the longer time period of comparison.
- 285

Most glaciers and perennial snowfields lost mass (Figure 3). The median rate of change 286

- for glaciers, -0.3 ± 0.2 m yr⁻¹, and for snowfields, -0.2 ± 0.2 m yr⁻¹. Four glaciers (2%) 287
- 288 and 56 (10%) perennial snowfields increased in volume; their locations are not region
- specific. These features are characterized by small area, median 0.02 km^2 (all but one < 289
- 290 0.2 km^2), steeper slopes, and higher elevations. The features that gained volume were at
- 291 significantly higher elevations and steeper slopes (median 3100 m, 28°) compared to
- those that lost volume, (median 2335 m 25° ; p < 0.05, Mann-Whitney U). The time series 292
- 293 of ice mass loss in the Cascade Range, Washington is relatively complete compared to
- 294 other regions and show increasing mass loss with time (Figure 4). The rate of change
- 295 increased significantly since 1980.
- 296
- 297



298

299 Figure 3. Specific volume change of glaciers and perennial snowfields (G&PS). Light 300 grey circles represent perennial snowfields, and dark grey circles represent glaciers. The 301 'whiskers' represent uncertainty. Initial area refers to the area from the U.S. Geological 302 Survey's 1:24000 map series.

303





Figure 4. Volume change glaciers (dark grey boxes) and perennial snowfields (light grey boxes for each region with more than ten features, grouped by initial mapping date (all ending in 2016), 1960 (1956 to 1960) (A), 1970 (1966 to 1970) (B), 1975 (1971 to 1975) (C), 1980 (1976 to 1980) (D), and 1985 (1981 to 1985) (E). The 'whiskers' represent the smallest and largest values not considered outliers. The values that exceed 1.5 times the interquartile range (IQR) below the first quartile or above the third quartile are considered outliers (open circles 'Bear/Abs' refers to Beartooth-Absaroka, MT.

318

317 4. Discussion and Conclusions

319 GLISTIN was developed for measuring the relatively flat surfaces of large glaciers and 320 ice sheets, and its application to the complex topography alpine terrain presents a stress-321 case for the instrument. GLISTIN elevation mosaics compared favorably to lidar 322 measurements over barren earth $+0.17 \pm 1.78$ m (3 m posting). Similar comparisons over 323 bedrock in Greenland showed, $+0.32 \pm 0.95$ m (30 m posting) for single pass elevations 324 (Moller et al., 2019). Over snow and ice surfaces on Mount Adams the mean difference 325 of GLISTIN and lidar was -0.87 ± 3.8 m (3 m posting). We regard much of the difference 326 due to snow and ice melt over the 28-day interval between the initial lidar and later 327 GLISTIN surveys. Similar mean GLISTIN – lidar differences, were observed on two 328 gently sloping glacier surfaces in Alaska, $+0.8 \pm 1.7$ m and $+1.2 \pm 3.7$ m (3 m posting, 329 Moller et al., 2019). There was a similarly substantial time interval between the GLISTIN 330 and subsequent lidar surveys of 1.5 month and 1 month, respectively. Differencing 331 GLISTIN from the NED for estimating historic glacier change showed the RMSE at 332 control zones to be 7.35 m and largely driven by uncertainty in the NED. 333

334 The standard deviations for all elevation comparisons increased with surface slope and 335 most likely due to small offsets in aligning the DEMs. This result is also common to 336 other studies using matching DEMs. The mean elevation difference (Shuttle Radar 337 Topography Mission 1 Arc-Second Global DEM) over non-glaciated terrain near the 338 Akshiirak glaciers (Tien Shan, Central Asia) was -4.5 ± 10.9 m for slopes between 25° 339 and 30°, increasing to -7.6 ± 25.6 m for slopes between 40° and 78° (Paul, 2008; 340 Surazakov & Aizen, 2006). For North & Middle Sisters, Oregon the RMSE (lidar-NED) 341 was 5.7 m and 12.3 m for slopes between 20° to 30° and 50° to 60° , respectively 342 (Ohlschlager, 2015), and similar to the GLISTIN-NED RMSE of 6.4 m and 10.2 m for 343 the same slope bins. 344

345 Elevations were acquired for 85% of the surveyed glaciers and perennial snowfields, of

346 which 12% were completely mapped and 60% had \geq 80% coverage. Increased number of flight passes increased data coverage. This is one clear advantage over satellite InSAR
that look direction can be easily changed. Most of the missing backscatter was caused by
radar shadow and some from layover due to the steep terrain.

350

351 Rates of glacier specific mass loss across the western US are consistent with rates 352 estimated by other studies in our region. Overall, our rates over the last period of our 353 study 1985 - 2016 are consistent with the western US average (2000-2020) of about -0.4 m yr⁻¹ (Hugonnet et al., 2021). For the Cascade Range in Washington, Menounos et al. 354 355 (2018) estimated -0. 29 ± 0.10 m yr⁻¹ (2000-2018) from DEMs derived from optical satellite imagery, which is half of our estimate of -0.63 ± 0.26 m yr⁻¹ over the longer time 356 357 period of 1985-2016. Furthermore, our historic (pre-2000) rates of change is similar to 358 rates elsewhere globally (Andreassen et al., 2020; Carturan et al., 2013; DeBEER & 359 Sharp, 2007; Lambrecht & Kuhn, 2007). We also note an acceleration in mass loss since

360 361 1980.

GLISTIN makes an important contribution in tracking glacier change because data can be
 rapidly collected unimpeded by weather providing a near instantaneous elevation survey

364 of glaciers across broad regions. It performed well in complex terrain exceeding its

365 design requirement and future improvements in flight planning will reduce the

366 uncertainty. Significantly improved uncertainty for larger glaciers is expected due to

367 spatial averaging that reduces the random error component.

368

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373 Data Availability Statement

Analyzed data are included as Supporting Information S1. The single radar swaths of

375 elevation can be obtained from NASA, <u>https://uavsar.jpl.nasa.gov/cgi-bin/data.pl</u>, select

- 376 TopSAR (Ka-band). The mosaicked radar swaths used in this study can be found at,
- 377 <u>https://pdxscholar.library.pdx.edu/geology_data/5/</u>. The reference glacier outlines and
- 378 elevations derived from the historic 1:24,000 USGS topographic maps and historic
- 379 National Elevation Dataset (NED), respectively are located at,
- 380 <u>https://pdxscholar.library.pdx.edu/geology_data/4/</u>.
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523 Supplementary Online Material

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525 To identify the date of each glacier DEM, the glacier outlines were combined with a 526 shapefile of the NED metadata (https://viewer.nationalmap.gov/basic) in ArcGIS (ESRI, 527 Inc.). The NED from non-USGS sources (Table SOM1) did not include metadata for the 528 imagery date. In those cases, we used the dates listed on the map collars of the USGS 529 1:24000 topographic maps. Often the same aerial photographs used to create the 530 topographic maps were also used to derive the NED. Photography used to create the 531 portion of the NED overlapping the GLISTIN surveys were flown between 1950-1993, 532 with only two glaciers surveyed in 1950 (Wind River Range, WY) and nine after 1990 533 (Sierra Nevada, CA). There were 108 glacier outlines where the NED was derived from 534 imagery spanning multiple years, of which 23 had USGS metadata, clearly identifying 535 which portion of the outline corresponds with which year. The DEMs covering the 536 remaining 85 glaciers were from non-USGS sources, and it is unclear what portion of the 537 glacier were covered by imagery from which year. For G&PS, where multiple images 538 were used to create the NED, if >80% of the G&PS area was imaged within a single year 539 (21 G&PS), that year defined the date. For the remaining 64 G&PS, the date is defined as 540 the average of all years listed. The reported RMSE of the NED (1999 version) is 3.74 m, 541 but that RMSE under samples high elevation and slopes, fewer than ten samples for slope 542 $> 30^{\circ}$, and ~ 20 samples for elevations > 3000 m (Gesch, 2007). Therefore, the error over 543 glaciers and the surrounding alpine environment is probably much higher.

544

545 The NED was split into regions corresponding to the mountain ranges covered by 546 GLISTIN. In some cases, regions were split into smaller sub-regions to reduce processing 547 time. Each was converted to the same vertical reference system as GLISTIN (WGS84) 548 using V datum then projected into the UTM coordinate system and resampled to 10 m 549 using bilinear interpolation. The pixel resolution was resampled to 10 m so that it was 550 standard across all regions. Before resampling, the pixel resolution of the NED differed 551 by region, ranging from 8.5 m (northern Cascades, WA) to 9.4 m (Sierra Nevada, CA). GLISTIN was also resampled to 10 m and co-registered to the NED using the methods of 552

Berthier et al. (2007). The co-registration process reduces the horizontal and vertical offsets between the DEMs by first minimizing the standard deviation of differences over control zones and then applying that shift to the whole DEM. Offsets between DEMs can significantly influence estimates of elevation change, particularly on steep slopes (Berthier et al., 2007).



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Figure SOM1. Acquisition dates for imagery used to create the U.S. Geological Survey 1:24000 topographic maps for areas with glaciers and perennial snowfields (G&PS). The date on the x-axis represents the full decade (e.g., 1960 = 1960 to 1969). The y-axis is the fraction of the total. The solid grey bars are the fraction of area, and the dashed outline is the fraction of the number of G&PS. The top left depicts the imagery for all G&PS in the western U.S. The other graphs show the acquisition date for each state. Reprinted from Fountain et al. (2017).





579 Figure SOM2. Root mean square error (RMSE) between GLISTIN elevations and the

580 National Elevation Dataset for control zones binned by 10° slopes. The slope label

581 represents the maximum of that bin. The 10° slope bin includes slopes of 0° .

Table SOM1. List of sources compiled for the historical elevation data. The three

sources used were the National Map, maintained by the U.S. Geological Survey (USGS),

the Oregon office of the Bureau of Land Management (BLM), and the Geomorphological

596 Research Group at the University of Washington (UW).

State/Range	Source	Website
California		
Sierra Nevada	USGS	https://viewer.nationalmap.gov/basic
Colorado		
Front	USGS	https://viewer.nationalmap.gov/basic
Gore	USGS	https://viewer.nationalmap.gov/basic
Montana		
Beartooth-Absaroka	USGS	https://viewer.nationalmap.gov/basic
Lewis	USGS	https://viewer.nationalmap.gov/basic
Oregon		
Cascade	BLM	http://earthexplorer.usgs.gov
Washington		
northern Cascades	UW	http://gis.ess.washington.edu/data/
northern Cascades	USGS	https://viewer.nationalmap.gov/basic
southern Cascades	BLM	http://earthexplorer.usgs.gov
Wyoming		
Teton	USGS	https://viewer.nationalmap.gov/basic
Wind River	USGS	https://viewer.nationalmap.gov/basic

- 608 **Table SOM2**. List of lidar datasets used for the absolute error assessment. The datasets
- 609 came from three sources, the National Map, maintained by the U.S. Geological Survey
- 610 (USGS; https://viewer.nationalmap.gov/basic/), Washington Department of Natural
- 611 Resources (WA DNR; https://lidarportal.dnr.wa.gov/), and Oregon Department of
- 612 Geology and Mineral Industries (DOGAMI;
- 613 https://gis.dogami.oregon.gov/maps/lidarviewer/). 'Uncertainty' refers to the reported
- 614 absolute vertical uncertainty of the lidar.

	Region	Year	Source	Uncertainty			
	Mount Adams, WA	2016	USGS	0.07			
	northern Cascade Range, WA	2009	WA DNR	0.04			
	Mount Rainier, WA	2007/2008	WA DNR	0.04			
	Three Sisters, OR	2010	DOGAMI	0.04			
615 616 617 618							
619 620	Table SOM3. Amount of missing data in	n GLISTIN n	nosaic based or	n the number of flight			
621	passes. 'Missing Area' is the total area of pixels for the listed category in the GLISTIN						
622	mosaic that had no elevation data. 'Total	Area' is the	total area of al	l pixels for the			
623	category in the GLISTIN mosaic. '% Missing' is the ratio of the missing area divided by						
624	the total area within that category.						
625	Missing	Total					
	WIISSING	I ULAI					

	Missing	Total	
Flight	Area	Area	%
Passes	(km ²)	(km ²)	Missing
1	8575.94	10259.58	83.59
2	5368.17	15877.95	33.81
3	1167.58	7344.92	15.90
4	912.02	6511.64	14.01
5	154.29	813.70	18.96
6	51.56	379.55	13.59
7	8.67	147.40	5.88
8	4.00	64.31	6.23

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631 **Table SOM4.** Elevation uncertainty for control zones estimated from comparing

632 GLISTIN, lidar, and National Elevation Dataset (NED). The sources and accuracy of the

633 lidar data are listed in the supplementary online material. 'Region' refers to the region of

the mosaicked GLISTIN digital elevation models, 'Area' is the area of the control zone,

635 'Swath Count' is a range of the number of GLISTIN flights covering the control zones,

and standard deviation, 'RMSE' is the root mean square error. The 'All' column

637 combines data from the three regions (columns to the left) with multiple GLISTIN

638 passes.

	northern	Mount	Three	All	Mount Adams,
	Cascades,	Rainier, WA	Sisters, OR		WA
	WA				
Lidar Year	2009	2007/08	2010		2016
Area (km ²)	1.61	3.10	1.95	6.66	12.74
Swath Count	3-6	3-4	2	2-6	1
GLISTIN minus	s lidar				
RMSE (m)	+1.79	+1.87	+1.64	+1.78	+3.20
Mean \pm std (m)	$\textbf{-0.14} \pm 1.78$	$+0.38\pm1.83$	$+0.10\pm1.63$	$+0.17\pm1.78$	0.00 ± 3.20
Median (m)	-0.08	+0.17	+0.15	+0.11	0.00
GLISTIN minus	s NED				
RMSE (m)	+8.84	+3.36	+7.14	+6.46	+6.22
Mean \pm std (m)	$+4.49\pm7.61$	$+0.57\pm3.31$	-2.05 ± 6.84	$+1.05\pm6.38$	$+0.49\pm6.20$
Median (m)	+4.83	+035	-0.49	+0.80	+0.52
Lidar minus NED					
RMSE (m)	+7.21	+2.27	+8.37	+5.89	+5.60
Mean \pm std (m)	$+0.13\pm7.21$	-0.21 ± 2.27	-2.87 ± 7.86	$\textbf{-0.89} \pm 5.83$	-0.18 ± 5.60
Median (m)	+0.54	-0.15	-0.62	-0.19	-0.03

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647 **Table SOM5.** Root mean square error (RMSE), and mean elevation difference between

648 the National Elevation Dataset and GLISTIN derived elevations of barren earth control

control zones, and total area (Area) of the barren earth control zones in each region sampled.

		RMSE	Mean ± std	Area
	Region	(m)	(m)	(km ²)
	northern Cascades, WA	7.74	$+0.33\pm7.73$	107.34
	southern Cascades, WA	5.81	$+0.62\pm5.83$	27.06
	Mount Hood, OR	8.26	-2.42 ± 8.25	10.21
	Three Sisters, OR	6.07	$+0.64\pm6.03$	23.19
	Sierra Nevada, CA	6.64	-1.72 ± 6.42	191.16
	Lewis, MT	8.89	$+1.72\pm8.80$	22.16
	Beartooth-Absaroka, MT	10.57	-0.26 ± 10.57	7.83
	Teton, WY	3.53	-0.32 ± 3.52	0.93
	Wind River, WY	6.55	$\textbf{-0.96} \pm 6.48$	7.81
	Front, CO	8.31	$+1.40\pm8.19$	36.54
	Gore, CO	8.15	$+1.68\pm7.98$	27.43
	Total	7.32	-0.37 ± 7.31	461.67
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Table SOM6. Volume change estimates for glaciers and perennial snowfields in select666regions and periods. Volume change was estimated between the initial NED year and the667GLISTIN year of 2016 for glaciers and perennial snowfields with \geq 80% GLISTIN. The668change was grouped by region and year. The year listed is the last in the 5-year interval669(e.g., 1955 = 1951 to 1955). 'Num' is the number of G&PS for that category.670

			** 1			Specific Vol
D: /X/ /T	NT	Area	Volum	106)	Specific Vol	Change Rate
Region/Year/Type	Num	(Km²)	Change (m	^o x 10°)	Change (m)	$(m yr^{-1})$
WA Cascades	75	10.70	226.01	117 40	17.10 . 5.00	0.21 ± 0.11
1960 Classica	15	19.70	$-330.81 \pm$	11/.49	-17.10 ± 5.96	-0.31 ± 0.11
Glacier	29	17.75	$-312.42 \pm$	100.50	-17.60 ± 6.00	-0.31 ± 0.11
Snowfield	46	1.95	$-24.40 \pm$	10.93	-12.48 ± 5.59	-0.22 ± 0.10
1970	53	53.36	-507.94 ±	255.44	-9.52 ± 4.79	-0.21 ± 0.10
Glacier	23	52.40	-501.59 ±	250.65	-9.57 ± 4.78	-0.21 ± 0.10
Snowfield	30	0.96	-6.35 ±	4.79	-6.62 ± 5.00	-0.14 ± 0.11
1975	82	15.88	$-290.34 \pm$	124.61	-18.29 ± 7.85	-0.45 ± 0.19
Glacier	24	13.14	-249.19 ±	102.35	-18.96 ± 7.79	-0.46 ± 0.19
Snowfield	58	2.73	-41.16 ±	22.26	-15.05 ± 8.14	-0.37 ± 0.20
1980	20	21.40	$-320.08 \pm$	180.75	-14.95 ± 8.44	-0.42 ± 0.23
Glacier	8	20.81	-309.81 \pm	175.82	-14.89 ± 8.45	-0.41 ± 0.23
Snowfield	12	0.59	-10.27 \pm	4.94	-17.32 ± 8.33	-0.48 ± 0.23
1985	101	34.14	-662.12 \pm	275.94	-19.39 ± 8.08	-0.63 ± 0.26
Glacier	40	31.54	-628.40 \pm	257.10	-19.92 ± 8.15	-0.64 ± 0.26
Snowfield	61	2.60	-33.71 ±	18.83	-12.97 ± 7.25	-0.42 ± 0.23
OR Cascades						
1960	44	14.47	$-215.07 \pm$	90.29	-14.86 ± 6.24	-0.27 ± 0.11
Glacier	13	12.19	$-188.44 \pm$	76.15	-15.46 ± 6.25	-0.28 ± 0.11
Snowfield	31	2.28	$-26.63 \pm$	14.14	-11.67 ± 6.19	-0.21 ± 0.11
1975	25	8.09	-143.32 ±	50.91	-17.71 ± 6.29	-0.43 ± 0.15
Glacier	9	7.44	-137.50 ±	46.93	-18.48 ± 6.31	-0.45 ± 0.15
Snowfield	16	0.65	-5.83 ±	3.98	-8.97 ± 6.13	-0.22 ± 0.15
Sierra Nevada						
1975	16	0.39	-4.19 ±	2.38	-10.74 ± 6.09	-0.26 ± 0.15
Glacier	2	0.13	-1.85 +	0.73	-14.57 + 5.73	-0.36 ± 0.14
Snowfield	14	0.15	-2.35 +	1 65	-8.90 + 6.26	-0.22 ± 0.15
1980	35	2.61	-42.98 +	18 44	-1644 + 705	-0.46 ± 0.20
Glacier	12	1.95	-34 69 +	13 74	-17.76 ± 7.03	-0.49 ± 0.20
Snowfield	23	0.66	-8 30 +	4 70	-1255 ± 710	-0.35 ± 0.20
1985	109	3.87	-40 62 ±	18 78	-10.50 ± 4.86	-0.34 ± 0.16
Glacier	9	1 40	-19 27 +	8.63	-13.79 ± 6.18	-0.44 ± 0.10
Snowfield	100	2.40	$-17.27 \pm 21.35 \pm$	10.15	-13.77 ± 0.10 8 64 + 4 11	-0.44 ± 0.20 0.28 ± 0.13
Wind River	100	2.47	-21.35 ±	10.15	-0.04 ± 4.11	-0.20 ± 0.13
1970	6/	23.05	-365 80 +	115 /3	-1528 + 482	-0.33 ± 0.10
Glacier	10	25.95 21.17	$-305.00 \pm$	102 55	-15.20 ± 4.02 16 31 ± 1.91	-0.33 ± 0.10 0.35 ± 0.11
Snowfield	17	21.1/ 277	$-3+3.41 \pm$	102.33	-10.31 ± 4.64	-0.33 ± 0.11
Snowneid	43	2.11	$-20.40 \pm$	12.89	-1.33 ± 4.04	-0.10 ± 0.10

	1975	24	0.60	-3.61 ±	2.82	-6.01 ± 4.70	-0.15 ± 0.11
	Glacier	1	0.05	-1.12 ±	0.27	-20.90 ± 4.96	-0.51 ± 0.12
	Snowfield	23	0.55	$-2.49 \pm$	2.56	-4.55 ± 4.68	-0.11 ± 0.11
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1 2	Application of Aerial InSAR to Measure Glacier Elevations
3 4 5	Bryce Glenn ¹ , Andrew G. Fountain ¹ , Delwyn Moller ²
6	¹ Department of Geology, Portland State University, Portland, Oregon, USA 97207
7	² Department of Electrical, Computer & Software Engineering, University of Auckland,
8	Auckland, New Zealand
9 10 11 12	Corresponding author: Andrew G. Fountain, andrew@pdx.edu
13	Key Points:
14	• Aerial InSAR can rapidly map the topography of alpine glaciers over a broad
15	region.
16	• Elevations compare favorably to lidar, $+0.17 \pm 1.78$ m at spatial scale of 3 m.
17	• The mean rate of glacier elevation change (specific volume) is -0.3 ± 0.2 m yr ⁻¹
18	for the past 56 years with rates increasing since 1980.
19 20	

21 Abstract

22

23 Glaciers and perennial snowfields are important to alpine ecosystems and regional 24 hydrology. Quantifying volume change of a population of glaciers widely distributed 25 over a region is difficult and expensive. We employed NASA's novel Airborne Glacier 26 and Ice Surface Topography Interferometer (GLISTIN) to rapidly map surface 27 topography of alpine glaciers across the western USA. In five flight days 3289 glaciers 28 and perennial snowfields were surveyed. Comparison with lidar over control sites showed 29 a mean difference of $+0.17 \pm 1.78$ m at a spatial scale of 3 m. Data coverage increased 30 and elevation uncertainty decreased with the mosaicking of multiple passes due to the 31 complex terrain. Elevation change since the National Elevation Dataset shows a thinning 32 (and volume loss) over the last ~56 years, averaging -0.3 ± 0.2 m and accelerating since 33 1980. GLISTIN can be a valuable tool for rapidly mapping ice surfaces in the alpine 34 environment.

35

37

36 Plain Language Summary

38 Glaciers and perennial snowfields are important water sources to alpine ecosystems and 39 regional hydrology. To quantify their contribution their volume change is measured by mapping elevation changes of the ice surface. However, quantifying volume change for a 40 41 population of glaciers widely distributed over a region is difficult and expensive. We 42 employed NASA's airborne radar (GLISTIN) to rapidly map surface topography of 43 alpine glaciers across the western USA. In only five flight days 3289 glaciers and 44 perennial snowfields were surveyed. GLISTIN data over control-regions were compared 45 to lidar, an independent elevation measure using lasers, and showed small differences 46 indicating this method can be a valuable and cost-effective tool to track glacier change in 47 the future. Comparing the new elevations against historic elevations from USGS maps a 48 dramatic thinning (and volume loss) over the last ~60 years.

49

50 1. Introduction

51

52 Glacier melt is important to runoff in high alpine landscapes. At a local scale, melting

53 glaciers maintain streamflow during the dry, late summer months after the seasonal snow

has melted (Fountain & Tangborn, 1985; Moore et al., 2009). Shrinking glaciers lose ice
volume and supply more water to streams and rivers than anticipated from precipitation.
Although this may be a temporary benefit, particularly in dry regions, their ability to
buffer seasonal runoff in future is reduced, making watersheds more vulnerable to
drought (Hall & Fagre, 2003; Moore et al., 2009). At a global scale, mass transfer of
water from storage as ice to water runoff increases global sea-levels (Meier, 1984; Pfeffer
et al., 2014; Zemp et al., 2019).

61

62 Traditionally, tracking glacier mass change was a field effort based on measuring the gain 63 and loss of snow and ice at points on the glacier (Kaser et al., 2003; Ostrem & Brugman, 64 1991). Although these efforts produce high-quality results showing spatial variations in 65 mass change across a glacier only a few glaciers can be so monitored by any agency (Andreassen et al., 2005; O'Neel et al., 2019). Remote-sensing methods can be used to 66 67 cover broad regions using an alternative approach that estimates mass change from 68 volume change. Differential interferometric synthetic aperture radar (InSAR) can map 69 surface elevation changes and offers the advantage of an all-weather, day/night 70 capability, a particularly valuable tool in often cloudy alpine environments (Rosen et al., 71 2000). Satellite-borne applications have revolutionized our understanding of Antarctica 72 and Greenland (Mouginot et al., 2019; Shepherd et al., 2018), and more recently, the 73 larger alpine glaciers (Millan et al., 2022). Challenges using InSAR include shadowing, 74 decorrelation due to layover, phase unwrapping, and temporal landscape changes 75 (Eineder & Holzner, 2000; Rees, 2000).

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Here, we test a novel approach for determining surface elevations on alpine glaciers using
an airborne single-pass InSAR, NASA's Glacier, and Ice Surface Topography
Interferometer (GLISTIN; Moller et al., 2017). Unlike differential/repeat-pass InSAR,
GLISTIN collects two radar images simultaneously, allowing elevations to be derived
from a single flight pass and are thus not sensitive to temporal decorrelation between
observations. Mounted on a jet aircraft, GLISTIN can image large areas in a short time
and has been used to map the relatively gentle topography of large glaciers and ice sheets

84	(Hensley et al., 2016; Moller et al., 2019). We evaluate its performance to map small
85	alpine glaciers in complex terrain across a broad region. In addition, the updated glacier
86	elevations are differenced from the National Elevation Data (Gesch, 2002) to calculate
87	glacier elevation change across the western US.
88 89 90	2. Data and Methods
91 02	2.1 Study Area
92 93	The study region is the American West, defined as the continental United States west of
94	the 100th meridian enclosing about $2x10^6$ km ² and home to about 5036 glaciers and
95	perennial snowfields ($\geq 0.01 \text{ km}^2$) as of the late 20 th century (Figure 1; Fountain et al.,
96	2017). The region is made up of three large mountain ranges, the Rocky Mountains, the
97	Cascade Range, and the Sierra Nevada. Many peaks exceed 4000 m in. The largest
98	concentration of glaciers, and lowest elevation (2000 m - 3000 m asl) is in the maritime
99	climate of the Pacific Northwest (Oregon, Washington, north-west Montana,). The
100	remaining glaciers are in continental climates elsewhere at high elevations, > 3000m.
101	



102

Figure 1. Map of glaciers and perennial snowfields (black dots) in the Western U.S. The
boxes show regions surveyed by GLISTIN.

106 Regional studies have shown drastic decreases in glacier area exceeding 50% over the

107 last century (DeVisser & Fountain, 2015; Fagre et al., 2017; O'Neel et al., 2019). The

- 108 rate of change has not been constant or spatially uniform (Basagic & Fountain, 2011;
- 109 Hoffman et al., 2007; O'Neal et al., 2015). Glacier volume changes, estimated by
- 110 differencing topography over time, show a loss on Mount Rainier, WA, of -0.65 km³,

- 111 average specific mass loss rate of -0.16 m w.e yr⁻¹ (1970 2007/2008; Sisson et al.,
- 112 2011). Menounos et al. (2018) estimated a volume loss of -127.65 ± 45.17 km³, $-0.42 \pm$
- 0.15 m w.e. between 2000 and 2018 for most of the glaciated terrain in Western NorthAmerica.

116 2.2 GLISTIN

117

118 GLISTIN is a Ka-band radar (8.4 mm, 35.66 GHz) system that utilizes two horizontally 119 polarized antennas, 0.25 m apart in elevation, both of which are capable of transmitting 120 and receiving (Moller et al., 2019). Unlike repeat-pass InSAR, GLISTIN's dual antennas, 121 collect data simultaneously. The Ka-band center frequency enables high accuracy with a 122 compact architecture and reduces snow penetration compared to lower frequencies. This 123 cross-track InSAR system is capable of providing not only the position of each image 124 point in along-track and slant range as with traditional SAR but also the height of that 125 point via the interferometric phase. Because the phase repeats after 2π , it must be 126 "unwrapped" to determine its unique location and height relative to a reference surface 127 (Moller et al., 2011; Rosen et al., 2000). The system is contained in an external pod 128 beneath NASA's Gulfstream-III aircraft with left looking view angles of 15-50° from 129 nadir. The system is coupled to inertial navigation and global position that provide pitch 130 and roll of the aircraft as well as its precise position in space. Nominal flight altitudes are 131 about 12,500 m above sea-level with a ground swath width of about 12 km and its typical air speed is 720 km hr⁻¹. 132

133

134 To guide the aerial survey, the locations of the glaciers were retrieved from Fountain et 135 al. (2017). Flight passes were typically flown in pairs, each in an opposite direction, to 136 reduce gaps in backscatter from radar shadow or layover in the mountainous terrain. In a 137 few regions additional perpendicular flight passes were also flown. The georectified 138 height-maps from each pass were mosaicked into a 3-meter pixel-size digital elevation 139 model (DEM; Hensley et al., 2016) and projected into the Universal Transverse Mercator 140 (UTM) coordinate system. Self-reported elevation accuracy is 'height-precision', a 141 statistical estimate based on the interferometric correlation of each individual radar pixel

making up the 3 m mosaicked pixel (Moller et al., 2011). In the final mosaicked DEM, the elevation of each pixel is the weighted sum of elevations from individual passes and the weights are inversely proportional to the height-precision (Hensley et al., 2016). The vertical absolute uncertainty of GLISTIN-derived topography was found to be about \pm 0.30 m over bare non-snow-covered terrain (Schumann et al., 2016). Data collection and processing were provided by the Jet Propulsion Laboratory at California Institute of Technology, Pasadena, CA.

149

150 2.3 Accuracy 151

152 The accuracy of GLISTIN elevations was ground-truthed by differencing lidar DEMs 153 from GLISTIN DEMs (Table SOM2). All lidar data were converted from its native 154 coordinate system to WGS84 to UTM using Vdatum (Version 3.8, 2017, National 155 Oceanic and Atmospheric Administration, Washington, DC), inducing an error of about 0.076 m (self-reported by Vdatum during conversion) and resampled to 3 m to match the 156 157 GLISTIN DEMs spatial posting, using bilinear interpolation. To calculate elevation 158 change the ¹/₃ arc-second NED was converted to UTM (WGS84) using Vdatum and 159 resampled to 10 m using bilinear interpolation. GLISTIN and lidar elevations were also 160 resampled to 10 m using bilinear interpolation to match the NED. The relative accuracy 161 of GLISTIN, lidar, and the NED were inter-compared at four barren earth snow-free 162 control zones in the Cascade Range of Oregon and Washington where all three estimates 163 of elevation were available. Each control zone is a patchwork of co-located but isolated 164 terrains. Barren earth terrains were derived from the 'barren' class of the 2016 National 165 Land Cover Database (https://www.mrlc.gov/data/nlcd-2016-land-cover-conus). 166 GLISTIN's performance imaging ice/snow surfaces was examined by comparing 167 elevations to lidar data acquired on Mount Adams, Washington, which was flown 28 168 days prior to the GLISTIN flights. We expect GLISTIN to yield somewhat lower 169 elevations due to melting of the snow and ice.

170

171

173 2.4 Area and Volume Change

- 174 The reference area and elevation of the glaciers and perennial snowfields are derived 175 176 from (Fountain et al., 2017) and a 'historic' version of the NED (Gesch et al., 2002), 177 respectively. Both are based on the original U.S. Geological Survey 1:24000 topographic 178 maps from which the glacier outlines and elevations were derived. The maps in the 179 western US were drawn over a period of years (1940s-1980s. Resolution of the NED is $\frac{1}{3}$ 180 arc-second (~10 m), and the horizontal and vertical coordinate systems are North 181 American Datum of 1983, North American Vertical Datum of 1988, respectively. The 182 NED is continually being updated and it was necessary to retrieve the original 'historic' 183 version from multiple sources (Table SOM1).
- 184

185 Volume change was estimated by differencing the GLISTIN elevations from the NED 186 elevations within the original perimeter and for only those glaciers with $\geq 80\%$ GLISTIN 187 coverage. Le Bris and Paul (2015) showed that good estimates of volume change can be achieved with the elevation postings cover at least 80% of the glacier area. Reasonable 188 189 estimates of volume change can be obtained for coverages as low as 40%, however 190 results depend on interpolation method (McNabb et al., 2019), so we adopted the more 191 conservative threshold of 80% used by Le Bris and Paul (2015). In order to compare 192 volume loss between large and small glaciers and because the historic mapping occurred 193 over a time-span of decades across the western US, results are expressed as the rate of specific volume (volume/area) change (m⁻³ m⁻² yr⁻¹ or m yr⁻¹). 194 195

196 Uncertainty of volume change, $\sigma_{\Delta V}$, is calculated for each individual glacier or perennial 197 snowfield, using the vertical and area uncertainties (Menounos et al., 2018),

198
$$\sigma_{\Delta V} = \sqrt{\left(\sigma_{\Delta z} A_g\right)^2 + \left(\sigma_A \Delta z\right)^2}, \qquad (1)$$

199

where $\sigma_{\Delta Z}$ is the RMSE of elevation differences between GLISTIN and the NED for all barren earth control zones, for the region in which the glacier or perennial snowfield is located, A_g is the original (historic) area of the glacier or perennial snowfield, Δz is the







219



fraction of area mapped by GLISTIN. Initial area refers to the area from the U.S.

222 Geological Survey's 1:24000 map series. The x-axis value is the maximum for each bin.

224 225 As expected, increasing the number of flight passes over the same area increased the 226 backscatter coverage. For one flight pass backscatter was received from 17% of the entire 227 illuminated area, for two flights 66%, four flights, 86%, and for eight flights 94% (Table 228 SOM3). No significant difference was observed in backscatter coverage of snow/ice 229 surfaces compared to ice-free surfaces, and within glaciers no significant differences 230 between snow-covered regions and ice-exposed regions. Backscatter reception was only 231 significantly correlated with terrain slope with greater loss on steeper slopes. 232

233 3.2 Accuracy

234 235 The GLISTIN DEMs for three of the four barren earth control zones were compiled from 236 multiple passes. The fourth control zone (Mount Adams, WA) was comprised of single 237 pass data and was examined separately. For the three multi-pass barren earth control 238 zones the GLISTIN – lidar (3 m posting) mean difference was $+0.17 \pm 1.78$ m (Table 239 SOM4). Comparing GLISTIN and the NED over the same regions (10 m posting), the 240 mean difference and standard deviation was much larger, $\pm 1.05 \pm 6.38$ m. This is due to 241 the much larger uncertainty in the NED elevations of 3.74 m, which is based mostly on 242 control points located in lower elevation and less complex terrain (Gesch, 2007). The 243 mean lidar-NED difference -0.89 ± 5.83 , supports this inference. For the control zones on 244 Mount Adams, the mean elevations difference of single-pass GLISTIN - lidar (3 m 245 posting) was -0.00 ± 3.20 m, whereas for the snow/ice surfaces it was -0.86 ± 3.76 m. 246 The negative difference for the snow/ice surfaces is to be expected given the melting that 247 occurred over the 28-day period between the initial lidar survey followed by the 248 GLISTIN survey. Given that the snow is wet during this time of year and interferometric 249 penetration is negligible (Hensley et al., 2016).

With respect to interferometric radar errors it is important to note that the height precision is dominated by the instrument random noise. This relative error is high frequency and will scale with spatial averaging of uncorrelated pixels or independent samples. The same is not true for the height accuracy or systematic (mean) offset which does not 254 improve with averaging as they are correlated. Therefore, if we calculate the RMSE for 255 more coarse spatial postings this metric will reduce significantly (with the random 256 /precision inversely proportional to the square-root of the effective number of 257 independent looks (Hensley et. al. 2016). For this paper we analyze GLISTIN data at a spatial posting of 3m due to the small footprint of many of these glaciers. However, one 258 259 can expect significantly improved height precision, and thereby RMSE for large glaciers 260 via spatial averaging. The low mean difference (i.e. accuracy) observed for the barren 261 areas indicates that extremely low height errors are achievable with sufficient spatial 262 averaging to reduce the random component (Schumann et. al. 2016; Moller et.al. 2019)

263 Although no correlation was observed between mean elevation difference (GLISTIN -

lidar) and surface slope, the standard deviation increased from about 1.7 m for slopes

between 20° and 30° to 3.8 m for slopes between 50° and 60°. The RMSE (GLISTIN-

NED) increased from 6.1 m for slopes 20° to 30° to 10.2 m for slopes between 50° and

 $267 \quad 60^{\circ}$. The rate of phase change is a function of the interferometric measurement geometry

and is directly proportional to the local slope. Phase unwrapping becomes more difficult

as the slope increases so an increased RMSE in extreme topography is to be expected.

270 The orientation of single-pass GLISTIN relative to the terrain surface affects the

271 elevation difference. The mean elevation difference (GLISTIN-lidar) was smaller for

surfaces facing towards GLISTIN, $+0.01 \pm 2.07$ m, than surfaces facing away, $+0.07 \pm$

273 4.03 m.

274 3.3 Volume change

275

Volume change was estimated for 1770 glaciers and perennial snowfields (54% of total) consisting of 351 glaciers and 1419 snowfields. Overall mean uncertainty, based on barren earth control zones across the west (Table SOM5), was -0.37 ± 7.31 m. Rejecting those specific volume changes that were smaller than uncertainty yielded 231 glaciers totaling 198.84 km² and 551 perennial snowfields (21.31 km²). Comparing our volume change to a prior estimate for Mt. Rainier, Washington (Sisson et al., 2011), showed that the prior estimate, based on a lidar-NED difference, of -8.6 m (1970-2007) is within the

- 283 uncertainty of our value, -9.7 ± 4.8 m (1970-2016). That our estimate showed a greater 284 mass loss is consistent with the longer time period of comparison.
- 285

Most glaciers and perennial snowfields lost mass (Figure 3). The median rate of change 286

- for glaciers, -0.3 ± 0.2 m yr⁻¹, and for snowfields, -0.2 ± 0.2 m yr⁻¹. Four glaciers (2%) 287
- 288 and 56 (10%) perennial snowfields increased in volume; their locations are not region
- specific. These features are characterized by small area, median 0.02 km^2 (all but one < 289
- 290 0.2 km^2), steeper slopes, and higher elevations. The features that gained volume were at
- 291 significantly higher elevations and steeper slopes (median 3100 m, 28°) compared to
- those that lost volume, (median 2335 m 25° ; p < 0.05, Mann-Whitney U). The time series 292
- 293 of ice mass loss in the Cascade Range, Washington is relatively complete compared to
- 294 other regions and show increasing mass loss with time (Figure 4). The rate of change
- 295 increased significantly since 1980.
- 296
- 297



298

299 Figure 3. Specific volume change of glaciers and perennial snowfields (G&PS). Light 300 grey circles represent perennial snowfields, and dark grey circles represent glaciers. The 301 'whiskers' represent uncertainty. Initial area refers to the area from the U.S. Geological 302 Survey's 1:24000 map series.

303





Figure 4. Volume change glaciers (dark grey boxes) and perennial snowfields (light grey boxes for each region with more than ten features, grouped by initial mapping date (all ending in 2016), 1960 (1956 to 1960) (A), 1970 (1966 to 1970) (B), 1975 (1971 to 1975) (C), 1980 (1976 to 1980) (D), and 1985 (1981 to 1985) (E). The 'whiskers' represent the smallest and largest values not considered outliers. The values that exceed 1.5 times the interquartile range (IQR) below the first quartile or above the third quartile are considered outliers (open circles 'Bear/Abs' refers to Beartooth-Absaroka, MT.

318

317 4. Discussion and Conclusions

319 GLISTIN was developed for measuring the relatively flat surfaces of large glaciers and 320 ice sheets, and its application to the complex topography alpine terrain presents a stress-321 case for the instrument. GLISTIN elevation mosaics compared favorably to lidar 322 measurements over barren earth $+0.17 \pm 1.78$ m (3 m posting). Similar comparisons over 323 bedrock in Greenland showed, $+0.32 \pm 0.95$ m (30 m posting) for single pass elevations 324 (Moller et al., 2019). Over snow and ice surfaces on Mount Adams the mean difference 325 of GLISTIN and lidar was -0.87 ± 3.8 m (3 m posting). We regard much of the difference 326 due to snow and ice melt over the 28-day interval between the initial lidar and later 327 GLISTIN surveys. Similar mean GLISTIN – lidar differences, were observed on two 328 gently sloping glacier surfaces in Alaska, $+0.8 \pm 1.7$ m and $+1.2 \pm 3.7$ m (3 m posting, 329 Moller et al., 2019). There was a similarly substantial time interval between the GLISTIN 330 and subsequent lidar surveys of 1.5 month and 1 month, respectively. Differencing 331 GLISTIN from the NED for estimating historic glacier change showed the RMSE at 332 control zones to be 7.35 m and largely driven by uncertainty in the NED. 333

334 The standard deviations for all elevation comparisons increased with surface slope and 335 most likely due to small offsets in aligning the DEMs. This result is also common to 336 other studies using matching DEMs. The mean elevation difference (Shuttle Radar 337 Topography Mission 1 Arc-Second Global DEM) over non-glaciated terrain near the 338 Akshiirak glaciers (Tien Shan, Central Asia) was -4.5 ± 10.9 m for slopes between 25° 339 and 30°, increasing to -7.6 ± 25.6 m for slopes between 40° and 78° (Paul, 2008; 340 Surazakov & Aizen, 2006). For North & Middle Sisters, Oregon the RMSE (lidar-NED) 341 was 5.7 m and 12.3 m for slopes between 20° to 30° and 50° to 60° , respectively 342 (Ohlschlager, 2015), and similar to the GLISTIN-NED RMSE of 6.4 m and 10.2 m for 343 the same slope bins. 344

345 Elevations were acquired for 85% of the surveyed glaciers and perennial snowfields, of

346 which 12% were completely mapped and 60% had \geq 80% coverage. Increased number of flight passes increased data coverage. This is one clear advantage over satellite InSAR
that look direction can be easily changed. Most of the missing backscatter was caused by
radar shadow and some from layover due to the steep terrain.

350

351 Rates of glacier specific mass loss across the western US are consistent with rates 352 estimated by other studies in our region. Overall, our rates over the last period of our 353 study 1985 - 2016 are consistent with the western US average (2000-2020) of about -0.4 m yr⁻¹ (Hugonnet et al., 2021). For the Cascade Range in Washington, Menounos et al. 354 355 (2018) estimated -0. 29 ± 0.10 m yr⁻¹ (2000-2018) from DEMs derived from optical satellite imagery, which is half of our estimate of -0.63 ± 0.26 m yr⁻¹ over the longer time 356 357 period of 1985-2016. Furthermore, our historic (pre-2000) rates of change is similar to 358 rates elsewhere globally (Andreassen et al., 2020; Carturan et al., 2013; DeBEER & 359 Sharp, 2007; Lambrecht & Kuhn, 2007). We also note an acceleration in mass loss since

360 361 1980.

GLISTIN makes an important contribution in tracking glacier change because data can be
 rapidly collected unimpeded by weather providing a near instantaneous elevation survey

364 of glaciers across broad regions. It performed well in complex terrain exceeding its

365 design requirement and future improvements in flight planning will reduce the

366 uncertainty. Significantly improved uncertainty for larger glaciers is expected due to

367 spatial averaging that reduces the random error component.

368

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373 Data Availability Statement

Analyzed data are included as Supporting Information S1. The single radar swaths of

375 elevation can be obtained from NASA, <u>https://uavsar.jpl.nasa.gov/cgi-bin/data.pl</u>, select

- 376 TopSAR (Ka-band). The mosaicked radar swaths used in this study can be found at,
- 377 <u>https://pdxscholar.library.pdx.edu/geology_data/5/</u>. The reference glacier outlines and
- 378 elevations derived from the historic 1:24,000 USGS topographic maps and historic
- 379 National Elevation Dataset (NED), respectively are located at,
- 380 <u>https://pdxscholar.library.pdx.edu/geology_data/4/</u>.
- 381

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523 Supplementary Online Material

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525 To identify the date of each glacier DEM, the glacier outlines were combined with a 526 shapefile of the NED metadata (https://viewer.nationalmap.gov/basic) in ArcGIS (ESRI, 527 Inc.). The NED from non-USGS sources (Table SOM1) did not include metadata for the 528 imagery date. In those cases, we used the dates listed on the map collars of the USGS 529 1:24000 topographic maps. Often the same aerial photographs used to create the 530 topographic maps were also used to derive the NED. Photography used to create the 531 portion of the NED overlapping the GLISTIN surveys were flown between 1950-1993, 532 with only two glaciers surveyed in 1950 (Wind River Range, WY) and nine after 1990 533 (Sierra Nevada, CA). There were 108 glacier outlines where the NED was derived from 534 imagery spanning multiple years, of which 23 had USGS metadata, clearly identifying 535 which portion of the outline corresponds with which year. The DEMs covering the 536 remaining 85 glaciers were from non-USGS sources, and it is unclear what portion of the 537 glacier were covered by imagery from which year. For G&PS, where multiple images 538 were used to create the NED, if >80% of the G&PS area was imaged within a single year 539 (21 G&PS), that year defined the date. For the remaining 64 G&PS, the date is defined as 540 the average of all years listed. The reported RMSE of the NED (1999 version) is 3.74 m, 541 but that RMSE under samples high elevation and slopes, fewer than ten samples for slope 542 $> 30^{\circ}$, and ~ 20 samples for elevations > 3000 m (Gesch, 2007). Therefore, the error over 543 glaciers and the surrounding alpine environment is probably much higher.

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545 The NED was split into regions corresponding to the mountain ranges covered by 546 GLISTIN. In some cases, regions were split into smaller sub-regions to reduce processing 547 time. Each was converted to the same vertical reference system as GLISTIN (WGS84) 548 using V datum then projected into the UTM coordinate system and resampled to 10 m 549 using bilinear interpolation. The pixel resolution was resampled to 10 m so that it was 550 standard across all regions. Before resampling, the pixel resolution of the NED differed 551 by region, ranging from 8.5 m (northern Cascades, WA) to 9.4 m (Sierra Nevada, CA). GLISTIN was also resampled to 10 m and co-registered to the NED using the methods of 552

Berthier et al. (2007). The co-registration process reduces the horizontal and vertical offsets between the DEMs by first minimizing the standard deviation of differences over control zones and then applying that shift to the whole DEM. Offsets between DEMs can significantly influence estimates of elevation change, particularly on steep slopes (Berthier et al., 2007).



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Figure SOM1. Acquisition dates for imagery used to create the U.S. Geological Survey 1:24000 topographic maps for areas with glaciers and perennial snowfields (G&PS). The date on the x-axis represents the full decade (e.g., 1960 = 1960 to 1969). The y-axis is the fraction of the total. The solid grey bars are the fraction of area, and the dashed outline is the fraction of the number of G&PS. The top left depicts the imagery for all G&PS in the western U.S. The other graphs show the acquisition date for each state. Reprinted from Fountain et al. (2017).





579 Figure SOM2. Root mean square error (RMSE) between GLISTIN elevations and the

580 National Elevation Dataset for control zones binned by 10° slopes. The slope label

581 represents the maximum of that bin. The 10° slope bin includes slopes of 0° .

Table SOM1. List of sources compiled for the historical elevation data. The three

sources used were the National Map, maintained by the U.S. Geological Survey (USGS),

the Oregon office of the Bureau of Land Management (BLM), and the Geomorphological

596 Research Group at the University of Washington (UW).

State/Range	Source	Website
California		
Sierra Nevada	USGS	https://viewer.nationalmap.gov/basic
Colorado		
Front	USGS	https://viewer.nationalmap.gov/basic
Gore	USGS	https://viewer.nationalmap.gov/basic
Montana		
Beartooth-Absaroka	USGS	https://viewer.nationalmap.gov/basic
Lewis	USGS	https://viewer.nationalmap.gov/basic
Oregon		
Cascade	BLM	http://earthexplorer.usgs.gov
Washington		
northern Cascades	UW	http://gis.ess.washington.edu/data/
northern Cascades	USGS	https://viewer.nationalmap.gov/basic
southern Cascades	BLM	http://earthexplorer.usgs.gov
Wyoming		
Teton	USGS	https://viewer.nationalmap.gov/basic
Wind River	USGS	https://viewer.nationalmap.gov/basic

- 608 **Table SOM2**. List of lidar datasets used for the absolute error assessment. The datasets
- 609 came from three sources, the National Map, maintained by the U.S. Geological Survey
- 610 (USGS; https://viewer.nationalmap.gov/basic/), Washington Department of Natural
- 611 Resources (WA DNR; https://lidarportal.dnr.wa.gov/), and Oregon Department of
- 612 Geology and Mineral Industries (DOGAMI;
- 613 https://gis.dogami.oregon.gov/maps/lidarviewer/). 'Uncertainty' refers to the reported
- 614 absolute vertical uncertainty of the lidar.

	Region	Year	Source	Uncertainty
	Mount Adams, WA	2016	USGS	0.07
	northern Cascade Range, WA	2009	WA DNR	0.04
	Mount Rainier, WA	2007/2008	WA DNR	0.04
	Three Sisters, OR	2010	DOGAMI	0.04
615 616 617 618				
619 620	Table SOM3. Amount of missing data in	n GLISTIN n	nosaic based or	n the number of flight
621	passes. 'Missing Area' is the total area o	f pixels for th	e listed catego	ry in the GLISTIN
622	mosaic that had no elevation data. 'Total	Area' is the	total area of al	l pixels for the
623	category in the GLISTIN mosaic. '% Mi	ssing' is the r	atio of the mis	sing area divided by
624	the total area within that category.			
625	Missing	Total		
	VIISSI112	I ULAI		

	Missing	Total	
Flight	Area	Area	%
Passes	(km ²)	(km ²)	Missing
1	8575.94	10259.58	83.59
2	5368.17	15877.95	33.81
3	1167.58	7344.92	15.90
4	912.02	6511.64	14.01
5	154.29	813.70	18.96
6	51.56	379.55	13.59
7	8.67	147.40	5.88
8	4.00	64.31	6.23

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631 **Table SOM4.** Elevation uncertainty for control zones estimated from comparing

632 GLISTIN, lidar, and National Elevation Dataset (NED). The sources and accuracy of the

633 lidar data are listed in the supplementary online material. 'Region' refers to the region of

the mosaicked GLISTIN digital elevation models, 'Area' is the area of the control zone,

635 'Swath Count' is a range of the number of GLISTIN flights covering the control zones,

and standard deviation, 'RMSE' is the root mean square error. The 'All' column

637 combines data from the three regions (columns to the left) with multiple GLISTIN

638 passes.

	northern	Mount	Three	All	Mount Adams,
	Cascades,	Rainier, WA	Sisters, OR		WA
	WA				
Lidar Year	2009	2007/08	2010		2016
Area (km ²)	1.61	3.10	1.95	6.66	12.74
Swath Count	3-6	3-4	2	2-6	1
GLISTIN minus	s lidar				
RMSE (m)	+1.79	+1.87	+1.64	+1.78	+3.20
Mean \pm std (m)	$\textbf{-0.14} \pm 1.78$	$+0.38\pm1.83$	$+0.10\pm1.63$	$+0.17\pm1.78$	0.00 ± 3.20
Median (m)	-0.08	+0.17	+0.15	+0.11	0.00
GLISTIN minus	s NED				
RMSE (m)	+8.84	+3.36	+7.14	+6.46	+6.22
Mean \pm std (m)	$+4.49\pm7.61$	$+0.57\pm3.31$	-2.05 ± 6.84	$+1.05\pm6.38$	$+0.49\pm6.20$
Median (m)	+4.83	+035	-0.49	+0.80	+0.52
Lidar minus NED					
RMSE (m)	+7.21	+2.27	+8.37	+5.89	+5.60
Mean \pm std (m)	$+0.13\pm7.21$	-0.21 ± 2.27	-2.87 ± 7.86	$\textbf{-0.89} \pm 5.83$	-0.18 ± 5.60
Median (m)	+0.54	-0.15	-0.62	-0.19	-0.03

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647 **Table SOM5.** Root mean square error (RMSE), and mean elevation difference between

648 the National Elevation Dataset and GLISTIN derived elevations of barren earth control

control zones, and total area (Area) of the barren earth control zones in each region sampled.

		RMSE	Mean ± std	Area
	Region	(m)	(m)	(km ²)
	northern Cascades, WA	7.74	$+0.33\pm7.73$	107.34
	southern Cascades, WA	5.81	$+0.62\pm5.83$	27.06
	Mount Hood, OR	8.26	-2.42 ± 8.25	10.21
	Three Sisters, OR	6.07	$+0.64\pm6.03$	23.19
	Sierra Nevada, CA	6.64	-1.72 ± 6.42	191.16
	Lewis, MT	8.89	$+1.72\pm8.80$	22.16
	Beartooth-Absaroka, MT	10.57	-0.26 ± 10.57	7.83
	Teton, WY	3.53	-0.32 ± 3.52	0.93
	Wind River, WY	6.55	$\textbf{-0.96} \pm 6.48$	7.81
	Front, CO	8.31	$+1.40\pm8.19$	36.54
	Gore, CO	8.15	$+1.68\pm7.98$	27.43
	Total	7.32	-0.37 ± 7.31	461.67
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Table SOM6. Volume change estimates for glaciers and perennial snowfields in select666regions and periods. Volume change was estimated between the initial NED year and the667GLISTIN year of 2016 for glaciers and perennial snowfields with \geq 80% GLISTIN. The668change was grouped by region and year. The year listed is the last in the 5-year interval669(e.g., 1955 = 1951 to 1955). 'Num' is the number of G&PS for that category.670

			** 1			Specific Vol
D: /X/ /T	Area	Volum		Specific Vol	Change Rate	
Region/Year/Type	Num	(Km²)	Change (m	^o x 10°)	Change (m)	$(m yr^{-1})$
WA Cascades	75	10.70	226.01	117 40	17.10 . 5.00	0.21 ± 0.11
1960 Classica	15	19.70	$-330.81 \pm$	11/.49	-17.10 ± 5.96	-0.31 ± 0.11
Glacier	29	17.75	$-312.42 \pm$	100.50	-17.60 ± 6.00	-0.31 ± 0.11
Snowfield	46	1.95	$-24.40 \pm$	10.93	-12.48 ± 5.59	-0.22 ± 0.10
1970	53	53.36	-507.94 ±	255.44	-9.52 ± 4.79	-0.21 ± 0.10
Glacier	23	52.40	-501.59 ±	250.65	-9.57 ± 4.78	-0.21 ± 0.10
Snowfield	30	0.96	-6.35 ±	4.79	-6.62 ± 5.00	-0.14 ± 0.11
1975	82	15.88	$-290.34 \pm$	124.61	-18.29 ± 7.85	-0.45 ± 0.19
Glacier	24	13.14	$-249.19 \pm$	102.35	-18.96 ± 7.79	-0.46 ± 0.19
Snowfield	58	2.73	-41.16 ±	22.26	-15.05 ± 8.14	-0.37 ± 0.20
1980	20	21.40	-320.08 \pm	180.75	-14.95 ± 8.44	-0.42 ± 0.23
Glacier	8	20.81	-309.81 \pm	175.82	-14.89 ± 8.45	-0.41 ± 0.23
Snowfield	12	0.59	-10.27 \pm	4.94	-17.32 ± 8.33	-0.48 ± 0.23
1985	101	34.14	-662.12 \pm	275.94	-19.39 ± 8.08	-0.63 ± 0.26
Glacier	40	31.54	-628.40 \pm	257.10	-19.92 ± 8.15	-0.64 ± 0.26
Snowfield	61	2.60	-33.71 ±	18.83	-12.97 ± 7.25	-0.42 ± 0.23
OR Cascades						
1960	44	14.47	$-215.07 \pm$	90.29	-14.86 ± 6.24	-0.27 ± 0.11
Glacier	13	12.19	$-188.44 \pm$	76.15	-15.46 ± 6.25	-0.28 ± 0.11
Snowfield	31	2.28	$-26.63 \pm$	14.14	-11.67 ± 6.19	-0.21 ± 0.11
1975	25	8.09	-143.32 ±	50.91	-17.71 ± 6.29	-0.43 ± 0.15
Glacier	9	7.44	-137.50 ±	46.93	-18.48 ± 6.31	-0.45 ± 0.15
Snowfield	16	0.65	-5.83 ±	3.98	-8.97 ± 6.13	-0.22 ± 0.15
Sierra Nevada						
1975	16	0.39	-4.19 ±	2.38	-10.74 ± 6.09	-0.26 ± 0.15
Glacier	2	0.13	-1.85 ±	0.73	-14.57 ± 5.73	-0.36 ± 0.14
Snowfield	14	0.26	-2.35 ±	1.65	-8.90 ± 6.26	-0.22 ± 0.15
1980	35	2.61	-42.98 +	18.44	-16.44 + 7.05	-0.46 ± 0.20
Glacier	12	1.95	-34.69 +	13.74	-17.76 + 7.04	-0.49 ± 0.20
Snowfield	23	0.66	-8 30 +	4 70	-12.55 + 7.10	-0.35 ± 0.20
1985	109	3.87	-40.62 +	18 78	-1050 ± 4.86	-0.34 ± 0.16
Glacier	9	1 40	-19 27 +	8.63	-13.79 ± 6.18	-0.44 ± 0.10
Snowfield	100	2.40	-21 35 +	10.15	-8.64 ± 4.11	-0.28 ± 0.13
Wind River	100	2.77	-21.33 ±	10.15	-0.04 ± 4.11	-0.20 ± 0.13
1970	64	23.95	-365 80 +	115 43	-1528 + 482	-0.33 + 0.10
Glacier	10	23.75	-345 41 +	102 55	-1631 ± 4.84	-0.35 ± 0.10
Snowfield	19	21.17	$-3+3.41 \pm$ 20.40 ±	12.55	-10.31 ± 4.04 7 35 ± 1.61	-0.55 ± 0.11 0.16 ± 0.10
SHOWHEIU	40	2.11	-20.40 ±	12.09	-7.55 ± 4.04	-0.10 ± 0.10

	1975	24	0.60	-3.61 ±	2.82	-6.01 ± 4.70	-0.15 ± 0.11
	Glacier	1	0.05	-1.12 ±	0.27	-20.90 ± 4.96	-0.51 ± 0.12
	Snowfield	23	0.55	$-2.49 \pm$	2.56	-4.55 ± 4.68	-0.11 ± 0.11
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