Electron Heating in Magnetosheath Turbulence: Dominant Role of the Parallel Electric Field within Coherent Structures

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Abstract

How are particles being energized by turbulent electromagnetic fields is an outstanding question in plasma physics and astrophysics. This paper investigates the electron acceleration mechanism in strong turbulence ($\delta B/B_0 \sim 1$) in the Earth’s magnetosheath based on the novel observations of the Magnetospheric Multiscale (MMS) mission. We find that electrons are magnetized in turbulent fields for the majority of the time. By directly calculating the electron acceleration rate from Fermi, betatron mechanism, and parallel electric field, it is found that electrons are primarily accelerated by the parallel electric field within coherent structures. Moreover, the acceleration rate by parallel electric fields increases as the spatial scale reduces, with the most intense acceleration occurring over about one ion inertial length. This study is an important step towards fully understanding the turbulent energy dissipation in weakly collisional plasmas.
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Key points:
1. Electrons are primarily accelerated by the parallel electric field in the magnetosheath turbulence.
2. The $E_{||}$ acceleration mostly occurs within the coherent structures through Joule-type dissipation.
3. The average $E_{||}$ acceleration rate increases with the decreasing local spatial scale.

Abstract
How are particles being energized by turbulent electromagnetic fields is an outstanding question in plasma physics and astrophysics. This paper investigates the electron acceleration mechanism in strong turbulence ($\delta B/B_0 \sim 1$) in the Earth’s magnetosheath based on the novel observations of the Magnetospheric Multiscale (MMS) mission. We find that electrons are magnetized in turbulent fields for the majority of the time. By directly calculating the electron acceleration rate from Fermi, betatron mechanism, and parallel electric field, it is found that electrons are primarily accelerated by the parallel electric field within coherent structures. Moreover, the acceleration rate by parallel electric fields increases as the spatial scale reduces, with
the most intense acceleration occurring over about one ion inertial length. This study is an important step towards fully understanding the turbulent energy dissipation in weakly collisional plasmas.

Plain language summary

The magnetosheath is one of the most turbulent environments in near-Earth space, which is very beneficial to the study of collisionless turbulent plasma. The mechanism of turbulent energy dissipation and the consequent plasma heating is not fully understood. The Magnetosphere Multiscale mission provides high-time cadence data and simultaneous multi-spacecraft measurements at very small inter-spacecraft separations. That can measure important quantities related to dissipation and heating at kinetic scales. This paper investigates how electrons are being accelerated through the dissipation of magnetic energy in nonlinear turbulence in the Earth's magnetosheath. We classify the acceleration mechanisms into three types: Fermi mechanism, betatron mechanism, and E∥ acceleration. By directly calculating and comparing these mechanisms, we find electrons are predominantly accelerated by parallel electric fields within coherent structures. The E∥ acceleration is the most effective around the ion inertial length.

1. Introduction

Energy cascade is one of the most prominent features of turbulence. Energy is injected at large scales, like fluid scales, then cascades to small scales through non-linear interactions, and finally dissipated at kinetic scales, leading to plasma heating and particle acceleration and the formation of suprathermal tails in the particle energy spectrum (Kiyani et al., 2015). Space plasma is typical of weak collisionality; hence collisionless mechanisms play a critical role in turbulent energy dissipation in space plasmas (Matthaeus et al., 2015; Chen 2016; Howes 2017). How the particles are heated/accelerated by turbulence is one of the most outstanding questions in plasma turbulence; however, the mechanism of turbulent energy dissipation and the consequent plasma heating is not fully understood after decades of intensive study.

Different types of acceleration mechanisms have been proposed to explain plasma
heating by the turbulent cascade in collisionless plasma. These mechanisms can be
generally classified into two categories: resonant acceleration and non-resonant
acceleration. The dissipation of waves is usually due to the energy transfer to energizing
particles caused by field and particle resonance, which can work over a long distance
and a long time. It includes Landau damping, cyclotron damping, and transit-time
damping (Chandran et al., 2010; Dmitruk et al., 2004a; Sahraoui et al., 2009; Isenberg
& Hollweg 1983; Gary et al., 2000; Isenberg 2001; Marsch & Tu 2001; Klein et al.,
2017). Previous studies have found clues of this resonant acceleration in space plasma
turbulence. He et al. (2015a, 2015b) suggested that solar wind ions are heated by
Landau damping and cyclotron damping by identifying characteristic signatures of
these resonances in the ion velocity distribution functions. Recently, in situ signature of
cyclotron resonant heating in the solar wind turbulence is observed by Parker Solar
Probe observations (Bowen et al., 2022). Chen et al. (2019) presented direct evidence
for Landau damping in magnetosheath turbulence by using the novel field-particle
correlation technique. The Landau damping mechanism for electron heating is further
confirmed by examining more events in the magnetosheath using the same field-particle
correlation method (Afshari et al., 2021).

One typical non-resonant acceleration is stochastic heating, which heats plasma
when the motion of particles becomes chaotic as the amplitude of electromagnetic field
fluctuations, at scales comparable to the gyro-scale, exceeds a critical value (Chandran
et al., 2010; Vech et al., 2017). It is found that acceleration and dissipation also occur
in coherent structures, such as current sheets (Retinò et al., 2007; Dmitruk et al., 2004b;
Osman et al., 2012), magnetic islands (Huang et al., 2016), small-scale vortices
(Alexandrova & Saur 2008), and magnetic holes (Huang et al., 2017a, 2017b; Zhong et
al., 2019), etc. It is suggested that magnetic reconnection occurring within the current
sheets in turbulence provides an important pathway for energy dissipation (Osman et
al., 2014; Zhou et al., 2021). The correlation between energy dissipation and localized
coherent structures indicates that energy dissipation may occur non-uniformly.

The motivation of this study is to investigate the acceleration and heating of electrons
in plasma turbulence. Different from Chen et al. (2019) and Afshari et al. (2021), the
turbulent interval we examine in this paper has large fluctuations with \( \delta B/B_0 \sim 1 \). In addition, we not only quantify the electron acceleration rate by the parallel electric field, as has been done by Chen et al. (2019) and Afshari et al. (2021), but also quantify the acceleration by the perpendicular electric field. The electron acceleration rates are evaluated under the guiding center approximation. We have used the data from the Magnetospheric Multiscale (MMS) mission, which provides high-time cadence data and simultaneous multi-spacecraft measurements at very small inter-spacecraft separations. This combination enables the study of the nature of dissipation at kinetic scales with an unprecedented level of accuracy and resolution. The FGM magnetic field instruments (Russell et al., 2016), EDP electric field instruments (Ergun et al., 2016; Lindqvist et al., 2016), and FPI ion and electron detectors (Pollock et al., 2016) provide the high-resolution data required to characterize signatures of dissipation and heating.

2. Methodology

Here we employ the method that has been used to calculate the acceleration rate in reconnection. This method considers the particle energy gain under guiding center approximation (Dahlin et al., 2014; Zhou et al., 2018; Zhong et al., 2020; Ma et al., 2020, 2022). The integrated energy gain of electrons in a unit volume per unit time for betatron acceleration is given by:

\[
W_b = P_{e\perp} v_{E\times B} \cdot \nabla B + \frac{P_{e\perp}}{B} \frac{\partial B}{\partial t} \tag{1}
\]

where \( P_{e\perp} \) is the perpendicular electron pressure, \( v_{E\times B} \) is the \( E\times B \) drift speed, \( \nabla B \) is the gradient of the total magnetic field. We refer to \( W_b \) as the betatron acceleration rate hereafter. Betatron acceleration might be efficient in magnetosheath turbulence, which usually involves large-amplitude \( |B| \) fluctuations, such as magnetic holes and magnetic peaks (e.g., Huang et al., 2017a, 2017b; Yao et al., 2018).

The Fermi acceleration rate is calculated by

\[
W_f = \left( P_{e\parallel} + n_e m_e v_{e\parallel}^2 \right) v_{E\times B} \cdot (b \cdot \nabla b) \tag{2}
\]

where \( P_{e\parallel} \) is the electron parallel pressure, \( v_{e\parallel} \) is the electron parallel bulk velocity and \( b \) is the unit vector of the magnetic field. Fermi acceleration is essentially caused by the
curvature drift in motional curved field lines. In situ observations in the magnetosheath suggest that curvature drift acceleration may be important for particle energization in magnetized turbulence (Bandyopadhyay et al., 2020; Huang et al., 2020).

The $E_\parallel$ acceleration rate, which is caused by the parallel electric field, is given by

$$W_{E\parallel} = J_{e\parallel}E_\parallel + \frac{\beta_{e\perp}}{2} J_\parallel E_\parallel$$

where $\beta_{e\perp}$ is the ratio between the perpendicular electron pressure and the magnetic pressure, $J_\parallel$ is the total parallel current density and $J_{e\parallel}$ is the parallel current carried by electrons. The presence of $\frac{\beta_{e\perp}}{2} J_\parallel E_\parallel$ is to eliminate the work caused by the parallel magnetization drift.

Betatron and Fermi mechanisms cause the heating of plasmas while $E_\parallel$ leads to not only plasma heating but also plasma bulk acceleration. The heating of plasma by $E_\parallel$ can be understood by examining the electron momentum equation:

$$E_\parallel = -\frac{1}{en} (\nabla \cdot P_e)_\parallel - \frac{m_e}{e} \left( \frac{d\nu_e}{dt} \right)_\parallel$$

where $e$ is the unit charge, $n$ is the number density, $\nu_e$ is the electron bulk velocity and $P_e$ is the electron pressure tensor. The relationship between the parallel electric field and the electron energy gain can be obtained by multiplying Eq. (4) by $-ne\nu_{e\parallel}$:

$$-ne\nu_e E_\parallel = v_{e\parallel} (\nabla \cdot P_e)_\parallel + nm_e \nu_{e\parallel} \left( \frac{d\nu_e}{dt} \right)_\parallel$$

The first term on the RHS of Eq. (5) contributes to the thermal energy increase of electrons, i.e., electron heating, while the second term on the RHS of Eq. (5) is related to the electron bulk velocity variation.

Equations (1) – (3) can be used to evaluate the acceleration rates for the three different types of mechanisms when the electrons satisfy the guiding center approximation, i.e., they are magnetized, or say, the 1st adiabatic invariant is conserved. To test this criterion, we calculate $\kappa$ (Büchner & Zelenyi 1989):

$$\kappa_{\text{curv}} = \sqrt{\frac{R_c}{\rho_e}}$$

where $R_c$ is the curvature radius of the magnetic field, and $\rho_e$ is the electron gyration radius, which is calculated by using four times the electron temperature, higher than the energy of most electrons in the magnetosheath. When $\kappa > 3$, electrons of the specific
energy are considered to satisfy the guiding center approximation. In the following study, we calculate the acceleration rates only at times when $\kappa$ is greater than 3.

3. Results

Figure 1 shows the overview of the MMS observations in a turbulent magnetosheath from 07:08:14 to 07:18:34 UT on 2016 December 18. The location of the MMS spacecraft in the geocentric solar ecliptic (GSE) coordinate system is $[11.4, 0.8, 0.2] \, \text{R}_E$ ($\text{R}_E$ is earth radii), downstream of the quasi-perpendicular bow shock. The average spacing of the MMS tetrahedron is $\sim 8.5 \, \text{km} \sim 9.5 \, d_e$ given the average plasma density of $\sim 35 \, \text{cm}^3$, where $d_e$ is the electron inertial length. The tetrahedron quality factor (TQF) is $\sim 0.99$, indicating that the four satellites constitute a nearly perfect tetrahedron in space. One can see from Figures 1a-1c that the electromagnetic fields and plasma flows are highly turbulent. The electron flow speed is similar to that of the ion flow, except that electron bulk velocity has some high-frequency fluctuations, which leads to filamentary currents with peak density larger than 500 nA m$^{-2}$ (Figure 1f). The electron temperature exhibits an anisotropy with $T_{e||} > T_{e\perp}$ in this interval (Figure 1g). The average ion bulk velocity is about $120 \, \text{km} \, \text{s}^{-1}$ and the average electron temperature is about 50 eV.

Figure 1g shows that $\kappa$ is larger than 3 (the black dotted line) for most of the time. This can be also clearly seen in the probability distribution function (PDF) of the $\kappa$ values displayed in Figure 2a. About 99% of $\kappa$ are greater than 3, which means that electrons are magnetized almost during the entire interval. The PDF of $\kappa$ increases from nearly 0 and reaches the peak at around $\kappa=18$, then it monotonically descends as the increment of $\kappa$. Figures 1h-1j display the electron acceleration rates for the three different acceleration mechanisms. They have both positive and negative values, suggesting bi-directional energy exchange between the electromagnetic fields and electrons rather than unidirectional energy conversion. The largest acceleration rate is up to $2 \times 10^4 \, \text{eV} \, \text{s}^{-1} \, \text{cm}^3 \sim 3.2 \, \text{nW} \, \text{m}^3$. There are many spikes in accelerated rates, which is the manifestation of intermittency. Note that the above three acceleration rates are
calculated in the frame co-moving with the magnetosheath flow, that is, \( \mathbf{E}' = \mathbf{E} + <\mathbf{V}> \times \mathbf{B} \), where \(<\mathbf{V}>\) is the average ion bulk velocity in the whole interval.

To determine the main acceleration mechanism, we plot the PDF of the three acceleration rates in Figure 2b. The total number of data points is about 20,000. We see that the highest value of the PDF is around \( W=0 \). The PDFs are sign-indefinite, which implies that the energy exchange between electromagnetic fields and plasmas goes both ways. The PDF of \( W_{E||} \) is the broadest among the three, indicating that \( E|| \) acceleration is generally greater than the other two mechanisms. The PDF of \( W_{E||} \) is asymmetric with respect to \( W=0 \), with a higher positive tail, while the PDF of \( W_b \) shows a subtle heavier negative tail and the PDF of \( W_f \) is nearly symmetric to \( W=0 \). The average acceleration rate of \( E|| \), betatron, and Fermi acceleration is \( 278 \, \text{eV s}^{-1} \, \text{cm}^{-3} \), \(-77 \, \text{eV s}^{-1} \, \text{cm}^{-3}\), and \(-4 \, \text{eV s}^{-1} \, \text{cm}^{-3} \), respectively. Therefore, on average, electrons were accelerated by \( E|| \), whereas betatron and Fermi mechanisms decelerated the electrons. The average energization rate of electrons by \( E|| \) is at least one order of magnitude larger than the results reported in previous literature (Afshari et al., 2021; Bandyopadhyay et al., 2020).

The PDF of \( W_{E||} \) is non-Gaussian with a heavier tail (Figure 2c), suggesting the intermittent nature of the acceleration process (Matthaeus et al., 2015). The intermittency is further proved by the large kurtosis of the \( E|| \), betatron, and Fermi acceleration rate, which is 374, 196, and 72, respectively.

Since the acceleration of electrons is dominated by parallel electric fields, we mainly focus on \( E|| \) acceleration in the following. To understand at which scale the acceleration occurs, we estimate the spatial scale of the magnetic field \( L_{dB} = \frac{B}{|\nabla B|} \) using the multi-spacecraft measurements under the assumption that the spatial variation is linear inside the MMS tetrahedron (Chanteur et al. 1998). Here, \( |\nabla B| \) is the norm of the Jacobian matrix of the magnetic field, i.e., \( |\nabla B| = \sqrt{\sum_i (\frac{\partial B_i}{\partial x_j})^2} \) (Kress et al. 2007). Figure 3a shows the joint PDF of the \( E|| \) acceleration rate \( W_{E||} \) and the \( L_{dB} \). We see that most of the data points are near \( W_{E||}=0 \), which is consistent with Figure 2b. \( L_{dB} \) is typically larger than \(~0.3 \, d\) and smaller than \(~30 \, d\). Figure 3b points out that the average acceleration rate descends with the increment of the spatial scale, from larger than \( 1000 \, \text{eV s}^{-1} \, \text{cm}^{-3} \)
when $L_{dB} < 10^{-0.5}$ d, to less than 200 eV s$^{-1}$ cm$^{-3}$ when $L_{dB} > 10$ d. Figures 3c displays that the average $L_{dB}$ is the largest near $W_{E//}$=0 and descends toward larger $W_{E//}$ in both the positive and negative directions. The average $L_{dB}$ reduces to about 1 d when $W_{E//}$ is 6 times larger than its RMS.

The Partial Variance of Increments (PVI) method has been widely used to identify the coherent structures in turbulent plasma (Matthaeus et al., 2015; Greco et al., 2009, 2018; Chasapis et al., 2015). The PVI index can be calculated using magnetic fields observed by multi-spacecraft:

$$PVI_{ij}(t) = \sqrt{\frac{|B_i(t) - B_j(t)|^2}{\langle |B_i(t) - B_j(t)|^2 \rangle}}$$

(7)

where the subscript $i, j=1,2,3,4$ indicates the different spacecraft. Figure 4a shows the $E//_{||}$ acceleration rate conditioned on the PVI index. We see that the average $W_{E//}$ monotonically increases with the increment of PVI index, which means that the most intense $E//_{||}$ acceleration corresponds to the largest PVI index. The average $W_{E//}$ with PVI index >3 is about 40 times the $W_{E//}$ averaged over all the data points. We also examine the local increase of the electron temperature conditioned on the PVI index (Figure 4b). The local increase of the electron temperature is represented by the electron temperature normalized by its regional average. It shows that similar to the profile of $W_{E//}$, the average $T_e$ also increases nearly monotonically with the increase of the PVI index. Notice that the monotonic trend is clearer in $T_{e//}$ than in $T_{e\perp}$. This is consistent with previous observations that strong electron heating, measured by the local increase of the electron temperature, occurs within current sheets with large PVI index, while no apparent heating within current sheets with small PVI index (Chasapis et al., 2015; Huang et al., 2022). Here we go one step further by confirming that structures with larger PVI index contribute to greater energy dissipation and electron acceleration.

Moreover, we investigate where the most intense $E//_{||}$ acceleration occurs. We define the intense $E//_{||}$ acceleration event as the interval in which the peak $W_{E//}$ is greater than 5,100 eV s$^{-1}$ cm$^{-3}$. This value is the intersection of the PDF of $W_{E//}$ and the Gaussian curve in Figure 2c. The boundary of each event is set as $5100/e \approx 1,900$, where $e$ is the
natural exponential. We identify the coherent structures when the PVI index is larger than the threshold $⟨PVI⟩+\sigma(PVI) \sim 1.3$, where $⟨PVI⟩$ and $\sigma(PVI)$ are the average and standard deviation of PVI index in the entire interval (Greco et al., 2009). Finally, 68 intense $E_∥$ acceleration events were selected, with 60 events having a PVI index greater than the threshold, i.e., they are within the coherent structures. One can see from Figure 3a that data points with $W_{E_∥}$ larger than 5,100 eV s$^{-1}$ cm$^{-3}$ are mostly in the range $L_{dB} \sim [1, 10]$ d.

Figure 5 shows one example of intense $E_∥$ acceleration events. It is shown that the intense $E_∥$ acceleration was coincident with a large PVI index, which corresponds to a coherent structure with a sharp change of the magnetic field and an intense current. A unipolar $E_∥ \sim 3$ mV m$^{-1}$ was responsible for $\sim 8 \times 10^4$ eV s$^{-1}$ cm$^{-3}$ acceleration rate in the parallel direction. Moreover, we transfer the magnetic field, electron bulk flow, and electric current to the local LMN coordinates (Figure 5g-5i) to see whether this event was associated with a local reconnection. We employ the same procedure as Man et al. (2022) to identify local reconnection, such as the electron outflowing jets and the out-of-plane current supporting the magnetic field reversal. We see a clear electron bulk flow reversal corresponding well to the current sheet crossing, implying that MMS encountered an active reconnection in this coherent structure. We have further examined all the intense $E_∥$ acceleration events. Overall, 30 ($\sim 44\%$) intense $E_∥$ acceleration events are associated with local reconnection. Therefore, we conclude that reconnection plays a significant role in accelerating electrons in this event.

4. Discussion and Conclusion

We have analyzed 31 other intervals in the turbulent magnetosheath observed by MMS from the year 2015 to 2019 (Wang et al., 2021). Twenty-two of these intervals are downstream of the quasi-parallel bow shock, and the other 9 events are downstream of the quasi-perpendicular bow shock. These events have a broader range of plasma β. We analyze these events by the same method described in this paper and find qualitatively similar results, that is, electrons are predominantly accelerated by $E_∥$ no
matter whether the interval is downstream of the quasi-parallel or quasi-perpendicular bow shock.

A further question that needs to be addressed is whether the $E_{||}$ acceleration in the coherent structures is due to Landau damping, stochastic heating, or Joule-type dissipation. Since the electrons are magnetized most of the time, they could not be energized through stochastic heating, which requires that the electron magnetic moment is not conserved (e.g., Vech et al., 2017). This event is different from the events reported by Afshari et al. (2021) and Chen et al. (2019), which demonstrate that electrons were accelerated through Landau resonance with the kinetic Alfvén waves. One major difference is that the magnetic field is relatively stable and has few coherent structures in the events studied by Afshari et al. (2021). This is also manifested by the non-Gaussian PDF of the $E_{||}$ acceleration rate in our event, whereas the PDF is near Gaussian in turbulence dominated by Landau damping (not shown). Importantly, we find that the large $E_{||}$ acceleration studied in this paper is usually associated with unipolar $E_{||}$ rather than wave-like $E_{||}$. Thus, the $E_{||}$ acceleration observed in our event is unlikely caused by Landau damping. More detailed analysis using the field-particle correlation technique for each intense $E_{||}$ acceleration event can be performed to further understand $E_{||}$ acceleration in these coherent structures.

In summary, we have investigated how electrons are being accelerated through the dissipation of magnetic energy in nonlinear turbulence in the Earth’s magnetosheath. Since electrons are mostly magnetized, we classify the acceleration mechanisms into three types: Fermi process, betatron mechanism, and $E_{||}$ acceleration. We find that the PDF of $E_{||}$ acceleration is significantly broader than the PDF of the other two acceleration rates, which implies that electrons are predominantly accelerated by parallel electric fields. $W_{E_{||}}$ increases with the reduction of the spatial scale and the increment of the PVI index, suggesting that the $E_{||}$ acceleration is the most effective around the ion inertial length and coherent structures play a vital role in energizing electrons through $E_{||}$. We demonstrate that electrons are accelerated through Joule-type dissipation/heating in strong turbulence containing many coherent structures, which is another important building block of the particle energization physical scenario besides
the mechanism proposed by Chen et al. (2019) and Afshari et al. (2021).

The acceleration and heating of ions by turbulence may be quite different to the electrons because ions are expected to be demagnetized due to their much larger gyro-radius. Hence one cannot use the guiding center approximation to describe the ion motion and may resort to other methods to quantify the ion acceleration, which is underway for further report.

Acknowledgments

Thanks to the MMS team for providing the high-quality data to complete this work. This work is supported by the National Natural Science Foundation of China (NSFC) under grant Nos. 42074197, 42130211, and 41774154.

Data Availability Statement

The data used in this study was obtained from the MMS Science Data Center (https://lasp.colorado.edu/mms/sdc/public/about/browse-wrapper/).
Figure 1. Overview of the turbulence in the magnetosheath observed by MMS from 07:08:14 to 07:18:34 UT on 18 December 2016. From the top to bottom are: (a) three components of the magnetic field and (b) the electric field; (c) electron number density; (d) ion bulk velocity; (e) electron parallel and perpendicular temperatures; (f) electric current density; (g) κ value; (h) – (j) the acceleration rate from $E_{||}$, Fermi process and betatron mechanism, respectively. The vectors are displayed in the GSE coordinate system.
Figure 2. (a) probability distribution function (PDF) of $\kappa$. The pink line marks $\kappa=3$; (b) PDF of betatron acceleration rate (blue), Fermi acceleration rate (red) and the $E_{||}$ acceleration rate (green). The green dashed line is the mirror image of the negative $E_{||}$ acceleration rate; (c) comparison of the PDF of the $E_{||}$ acceleration rate and the Gaussian curve (black).

Figure 3. (a) Joint PDFs of $E_{||}$ acceleration rate and the local magnetic field scale $L_{dB}$; (b) the average $W_{E_{||}}$ as a function of $L_{dB}$; (c) the average $L_{dB}$ as a function of $W_{E_{||}}/(W_{E_{||}})_{rms}$, here $(W_{E_{||}})_{rms}$ is the root mean square of $W_{E_{||}}$; The vertical bars in panels (b) and (c) represent the standard errors of the mean.

Figure 4. Average $E_{||}$ acceleration rate (a) and electron temperature (b) conditioned on the binned PVI index. The average $W_{E_{||}}$ is normalized by the averaged value in the entire
interval. The electron temperature is normalized by $<T_e>$ in a moving window with\n\nduration of 4 s, equivalent to approximately 10 $d_i$. The vertical bars represent the\nstandard error of the mean.

**Figure 5.** An example of the intense $E_\parallel$ accelerate event. From the top to bottom are:\n(a) three components of the magnetic field; (b) parallel electric field; (c) electric current\ndensity; (d) $E_\parallel$ acceleration rate; (e) PVI Index. The shaded area highlights a significant
electron accelerate by $E_\|$, within a coherent structure. The expanded view displays the
(f) magnetic field; (g) electron bulk velocity and (h) current density in the LMN
coordinate system around the coherent structure.

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Perpendicular ion heating by low-frequency Alfvén-wave turbulence in the solar wind.


Figure 1.
Figure 2.
Figure 3.
(a) $W_{||}(eV \cdot s^{-1} \cdot cm^{-3}) \times 10^4$

(b) $\langle W_{||} \rangle (eV \cdot s^{-1} \cdot cm^{-3})$

(c) $\langle L_{||} \rangle / (W_{||})_{rms}$
Figure 5.
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the most intense acceleration occurring over about one ion inertial length. This study is an important step towards fully understanding the turbulent energy dissipation in weakly collisional plasmas.

Plain language summary

The magnetosheath is one of the most turbulent environments in near-Earth space, which is very beneficial to the study of collisionless turbulent plasma. The mechanism of turbulent energy dissipation and the consequent plasma heating is not fully understood. The Magnetosphere Multiscale mission provides high-time cadence data and simultaneous multi-spacecraft measurements at very small inter-spacecraft separations. That can measure important quantities related to dissipation and heating at kinetic scales. This paper investigates how electrons are being accelerated through the dissipation of magnetic energy in nonlinear turbulence in the Earth’s magnetosheath. We classify the acceleration mechanisms into three types: Fermi mechanism, betatron mechanism, and $E_{||}$ acceleration. By directly calculating and comparing these mechanisms, we find electrons are predominantly accelerated by parallel electric fields within coherent structures. The $E_{||}$ acceleration is the most effective around the ion inertial length.

1. Introduction

Energy cascade is one of the most prominent features of turbulence. Energy is injected at large scales, like fluid scales, then cascades to small scales through nonlinear interactions, and finally dissipated at kinetic scales, leading to plasma heating and particle acceleration and the formation of suprathermal tails in the particle energy spectrum (Kiyani et al., 2015). Space plasma is typical of weak collisionality; hence collisionless mechanisms play a critical role in turbulent energy dissipation in space plasmas (Matthaeus et al., 2015; Chen 2016; Howes 2017). How the particles are heated/accelerated by turbulence is one of the most outstanding questions in plasma turbulence; however, the mechanism of turbulent energy dissipation and the consequent plasma heating is not fully understood after decades of intensive study.

Different types of acceleration mechanisms have been proposed to explain plasma
heating by the turbulent cascade in collisionless plasma. These mechanisms can be generally classified into two categories: resonant acceleration and non-resonant acceleration. The dissipation of waves is usually due to the energy transfer to energizing particles caused by field and particle resonance, which can work over a long distance and a long time. It includes Landau damping, cyclotron damping, and transit-time damping (Chandran et al., 2010; Dmitruk et al., 2004a; Sahraoui et al., 2009; Isenberg & Hollweg 1983; Gary et al., 2000; Isenberg 2001; Marsch & Tu 2001; Klein et al., 2017). Previous studies have found clues of this resonant acceleration in space plasma turbulence. He et al. (2015a, 2015b) suggested that solar wind ions are heated by Landau damping and cyclotron damping by identifying characteristic signatures of these resonances in the ion velocity distribution functions. Recently, in situ signature of cyclotron resonant heating in the solar wind turbulence is observed by Parker Solar Probe observations (Bowen et al., 2022). Chen et al. (2019) presented direct evidence for Landau damping in magnetosheath turbulence by using the novel field-particle correlation technique. The Landau damping mechanism for electron heating is further confirmed by examining more events in the magnetosheath using the same field-particle correlation method (Afshari et al., 2021).

One typical non-resonant acceleration is stochastic heating, which heats plasma when the motion of particles becomes chaotic as the amplitude of electromagnetic field fluctuations, at scales comparable to the gyro-scale, exceeds a critical value (Chandran et al., 2010; Vech et al., 2017). It is found that acceleration and dissipation also occur in coherent structures, such as current sheets (Retinò et al., 2007; Dmitruk et al., 2004b; Osman et al., 2012), magnetic islands (Huang et al., 2016), small-scale vortices (Alexandrova & Saur 2008), and magnetic holes (Huang et al., 2017a, 2017b; Zhong et al., 2019), etc. It is suggested that magnetic reconnection occurring within the current sheets in turbulence provides an important pathway for energy dissipation (Osman et al., 2014; Zhou et al., 2021). The correlation between energy dissipation and localized coherent structures indicates that energy dissipation may occur non-uniformly.

The motivation of this study is to investigate the acceleration and heating of electrons in plasma turbulence. Different from Chen et al. (2019) and Afshari et al. (2021), the
turbulent interval we examine in this paper has large fluctuations with $\delta B/B_0 \sim 1$. In addition, we not only quantify the electron acceleration rate by the parallel electric field, as has been done by Chen et al. (2019) and Afshari et al. (2021), but also quantify the acceleration by the perpendicular electric field. The electron acceleration rates are evaluated under the guiding center approximation. We have used the data from the Magnetospheric Multiscale (MMS) mission, which provides high-time cadence data and simultaneous multi-spacecraft measurements at very small inter-spacecraft separations. This combination enables the study of the nature of dissipation at kinetic scales with an unprecedented level of accuracy and resolution. The FGM magnetic field instruments (Russell et al., 2016), EDP electric field instruments (Ergun et al., 2016; Lindqvist et al., 2016), and FPI ion and electron detectors (Pollock et al., 2016) provide the high-resolution data required to characterize signatures of dissipation and heating.

2. Methodology

Here we employ the method that has been used to calculate the acceleration rate in reconnection. This method considers the particle energy gain under guiding center approximation (Dahlin et al., 2014; Zhou et al., 2018; Zhong et al., 2020; Ma et al., 2020, 2022). The integrated energy gain of electrons in a unit volume per unit time for betatron acceleration is given by:

$$ W_b = P_{e \perp} v_{E \times B} \cdot \nabla B + \frac{P_{e \perp} \delta B}{B} \frac{\partial}{\partial t} $$

where $P_{e \perp}$ is the perpendicular electron pressure, $v_{E \times B}$ is the $E \times B$ drift speed, $\nabla B$ is the gradient of the total magnetic field. We refer to $W_b$ as the betatron acceleration rate hereafter. Betatron acceleration might be efficient in magnetosheath turbulence, which usually involves large-amplitude $|B|$ fluctuations, such as magnetic holes and magnetic peaks (e.g., Huang et al., 2017a, 2017b; Yao et al., 2018).

The Fermi acceleration rate is calculated by

$$ W_f = \left( P_{e \parallel} + n_e m_e v_{e \parallel}^2 \right) v_{E \times B} \cdot (b \cdot \nabla b) $$

where $P_{e \parallel}$ is the electron parallel pressure, $v_{e \parallel}$ is the electron parallel bulk velocity and $b$ is the unit vector of the magnetic field. Fermi acceleration is essentially caused by the
curvature drift in motional curved field lines. In situ observations in the magnetosheath suggest that curvature drift acceleration may be important for particle energization in magnetized turbulence (Bandyopadhyay et al., 2020; Huang et al., 2020).

The $E_\parallel$ acceleration rate, which is caused by the parallel electric field, is given by

$$W_{E\parallel} = J_{\parallel} E_{\parallel} + \frac{\beta_{e\perp}}{2} J_{\parallel} E_{\parallel}$$

where $\beta_{e\perp}$ is the ratio between the perpendicular electron pressure and the magnetic pressure, $J_\parallel$ is the total parallel current density and $J_{e\parallel}$ is the parallel current carried by electrons. The presence of $\frac{\beta_{e\perp}}{2} J_{\parallel} E_{\parallel}$ is to eliminate the work caused by the parallel magnetization drift.

Betatron and Fermi mechanisms cause the heating of plasmas while $E_{\parallel}$ leads to not only plasma heating but also plasma bulk acceleration. The heating of plasma by $E_{\parallel}$ can be understood by examining the electron momentum equation:

$$E_{\parallel} = -\frac{1}{en} (\nabla \cdot P_e)_{\parallel} - \frac{m_e}{e} \left( \frac{d v_e}{dt} \right)_{\parallel}$$

where $e$ is the unit charge, $n$ is the number density, $v_e$ is the electron bulk velocity and $P_e$ is the electron pressure tensor. The relationship between the parallel electric field and the electron energy gain can be obtained by multiplying Eq. (4) by $-ne v_e$:

$$-ne v_e E_{\parallel} = (\nabla \cdot P_e)_{\parallel} + n m_e v_e \left( \frac{d v_e}{dt} \right)_{\parallel}$$

The first term on the RHS of Eq. (5) contributes to the thermal energy increase of electrons, i.e., electron heating, while the second term on the RHS of Eq. (5) is related to the electron bulk velocity variation.

Equations (1) – (3) can be used to evaluate the acceleration rates for the three different types of mechanisms when the electrons satisfy the guiding center approximation, i.e., they are magnetized, or say, the 1st adiabatic invariant is conserved. To test this criterion, we calculate $\kappa$ (Büchner & Zelenyi 1989):

$$\kappa_{\text{curv}} = \sqrt{R_c/\rho_e}$$

where $R_c$ is the curvature radius of the magnetic field, and $\rho_e$ is the electron gyration radius, which is calculated by using four times the electron temperature, higher than the energy of most electrons in the magnetosheath. When $\kappa > 3$, electrons of the specific
energy are considered to satisfy the guiding center approximation. In the following
study, we calculate the acceleration rates only at times when $\kappa$ is greater than 3.

3. Results

Figure 1 shows the overview of the MMS observations in a turbulent magnetosheath
from 07:08:14 to 07:18:34 UT on 2016 December 18. The location of the MMS
spacecraft in the geocentric solar ecliptic (GSE) coordinate system is [11.4, 0.8, 0.2] $R_E$
($R_E$ is earth radii), downstream of the quasi-perpendicular bow shock. The average
spacing of the MMS tetrahedron is ~ 8.5 km ~ 9.5 $d_e$ given the average plasma density
of ~ 35 cm$^3$, where $d_e$ is the electron inertial length. The tetrahedron quality factor (TQF)
is ~ 0.99, indicating that the four satellites constitute a nearly perfect tetrahedron in
space. One can see from Figures 1a-1c that the electromagnetic fields and plasma flows
are highly turbulent. The electron flow speed is similar to that of the ion flow, except
that electron bulk velocity has some high-frequency fluctuations, which leads to
filamentary currents with peak density larger than 500 nA m$^{-2}$ (Figure 1f). The electron
temperature exhibits an anisotropy with $T_{e||}$ > $T_{e\perp}$ in this interval (Figure 1g). The average
ion bulk velocity is about 120 km s$^{-1}$ and the average electron temperature is about 50
eV.

Figure 1g shows that $\kappa$ is larger than 3 (the black dotted line) for most of the time.
This can be also clearly seen in the probability distribution function (PDF) of the $\kappa$
values displayed in Figure 2a. About 99% of $\kappa$ are greater than 3, which means that
electrons are magnetized almost during the entire interval. The PDF of $\kappa$ increases from
nearly 0 and reaches the peak at around $\kappa$=18, then it monotonically descends as the
increment of $\kappa$. Figures 1h-1j display the electron acceleration rates for the three
different acceleration mechanisms. They have both positive and negative values,
suggesting bi-directional energy exchange between the electromagnetic fields and
electrons rather than unidirectional energy conversion. The largest acceleration rate is
up to $2 \times 10^4$ eV s$^{-1}$ cm$^{-3}$ ~ 3.2 nW m$^{-3}$. There are many spikes in accelerated rates, which
is the manifestation of intermittency. Note that the above three acceleration rates are
calculated in the frame co-moving with the magnetosheath flow, that is, $E' = E + \langle V \rangle \times B$, where $\langle V \rangle$ is the average ion bulk velocity in the whole interval.

To determine the main acceleration mechanism, we plot the PDF of the three acceleration rates in Figure 2b. The total number of data points is about 20,000. We see that the highest value of the PDF is around $W=0$. The PDFs are sign-indefinite, which implies that the energy exchange between electromagnetic fields and plasmas goes both ways. The PDF of $W_{E||}$ is the broadest among the three, indicating that $E_{||}$ acceleration is generally greater than the other two mechanisms. The PDF of $W_{E||}$ is asymmetric with respect to $W=0$, with a higher positive tail, while the PDF of $W_b$ shows a subtle heavier negative tail and the PDF of $W_f$ is nearly symmetric to $W=0$. The average acceleration rate of $E_{||}$, betatron, and Fermi acceleration is 278 eV s$^{-1}$ cm$^{-3}$, -77 eV s$^{-1}$ cm$^{-3}$, and -4 eV s$^{-1}$ cm$^{-3}$, respectively. Therefore, on average, electrons were accelerated by $E_{||}$, whereas betatron and Fermi mechanisms decelerated the electrons. The average energization rate of electrons by $E_{||}$ is at least one order of magnitude larger than the results reported in previous literature (Afshari et al., 2021; Bandyopadhyay et al., 2020). The PDF of $W_{E||}$ is non-Gaussian with a heavier tail (Figure 2c), suggesting the intermittent nature of the acceleration process (Matthaeus et al., 2015). The intermittency is further proved by the large kurtosis of the $E_{||}$, betatron, and Fermi acceleration rate, which is 374, 196, and 72, respectively.

Since the acceleration of electrons is dominated by parallel electric fields, we mainly focus on $E_{||}$ acceleration in the following. To understand at which scale the acceleration occurs, we estimate the spatial scale of the magnetic field $L_{dB} = B/|\nabla B|$ using the multi-spacecraft measurements under the assumption that the spatial variation is linear inside the MMS tetrahedron (Chanteur 1998). Here, $|\nabla B|$ is the norm of the Jacobian matrix of the magnetic field, i.e., $|\nabla B| = \sqrt{\sum_{ij} \left(\frac{\partial B_i}{\partial x_j}\right)^2}$ (Kress et al. 2007). Figure 3a shows the joint PDF of the $E_{||}$ acceleration rate $W_{E||}$ and the $L_{dB}$. We see that most of the data points are near $W_{E||}=0$, which is consistent with Figure 2b. $L_{dB}$ is typically larger than ~ 0.3 d, and smaller than 30 d. Figure 3b points out that the average acceleration rate descends with the increment of the spatial scale, from larger than 1000 eV s$^{-1}$ cm$^{-3}$
when $L_{dB} < 10^{-0.5}$ d, to less than 200 eV s$^{-1}$ cm$^{-3}$ when $L_{dB} > 10$ d. Figures 3c displays that the average $L_{dB}$ is the largest near $W_{E||}=0$ and descends toward larger $W_{E||}$ in both the positive and negative directions. The average $L_{dB}$ reduces to about 1 d, when $W_{E||}$ is 6 times larger than its RMS.

The Partial Variance of Increments (PVI) method has been widely used to identify the coherent structures in turbulent plasma (Matthaeus et al., 2015; Greco et al., 2009, 2018; Chasapis et al., 2015). The PVI index can be calculated using magnetic fields observed by multi-spacecraft:

$$PVI_{ij}(t) = \sqrt{\frac{|B_{i}(t) - B_{j}(t)|^2}{\langle |B_{i}(t) - B_{j}(t)|^2 \rangle}}$$

where the subscript $i, j=1,2,3,4$ indicates the different spacecraft. Figure 4a shows the $E_{||}$ acceleration rate conditioned on the PVI index. We see that the average $W_{E||}$ monotonically increases with the increment of PVI index, which means that the most intense $E_{||}$ acceleration corresponds to the largest PVI index. The average $W_{E||}$ with PVI index >3 is about 40 times the $W_{E||}$ averaged over all the data points. We also examine the local increase of the electron temperature conditioned on the PVI index (Figure 4b). The local increase of the electron temperature is represented by the electron temperature normalized by its regional average. It shows that similar to the profile of $W_{E||}$, the average $T_{e}$ also increases nearly monotonically with the increase of the PVI index. Notice that the monotonic trend is clearer in $T_{e||}$ than in $T_{e\perp}$. This is consistent with previous observations that strong electron heating, measured by the local increase of the electron temperature, occurs within current sheets with large PVI index, while no apparent heating within current sheets with small PVI index (Chasapis et al., 2015; Huang et al., 2022). Here we go one step further by confirming that structures with larger PVI index contribute to greater energy dissipation and electron acceleration.

Moreover, we investigate where the most intense $E_{||}$ acceleration occurs. We define the intense $E_{||}$ acceleration event as the interval in which the peak $W_{E||}$ is greater than 5,100 eV s$^{-1}$ cm$^{-3}$. This value is the intersection of the PDF of $W_{E||}$ and the Gaussian curve in Figure 2c. The boundary of each event is set as $5100/e \approx 1,900$, where e is the
natural exponential. We identify the coherent structures when the PVI index is larger than the threshold \((PVI)+\sigma(PVI)\sim 1.3\), where \(<PVI>\) and \(\sigma(PVI)\) are the average and standard deviation of PVI index in the entire interval (Greco et al., 2009). Finally, 68 intense \(E_{||}\) acceleration events were selected, with 60 events having a PVI index greater than the threshold, i.e., they are within the coherent structures. One can see from Figure 3a that data points with \(W_{E||}\) larger than 5,100 eV s\(^{-1}\) cm\(^{-3}\) are mostly in the range \(L_{dB}\sim [1, 10]\) d. 

Figure 5 shows one example of intense \(E_{||}\) acceleration events. It is shown that the intense \(E_{||}\) acceleration was coincident with a large PVI index, which corresponds to a coherent structure with a sharp change of the magnetic field and an intense current. A unipolar \(E_{||} \sim 3\) mV m\(^{-1}\) was responsible for \(~8\times10^{4}\) eV s\(^{-1}\) cm\(^{-3}\) acceleration rate in the parallel direction. Moreover, we transfer the magnetic field, electron bulk flow, and electric current to the local \(\text{LMN}\) coordinates (Figure 5g-5i) to see whether this event was associated with a local reconnection. We employ the same procedure as Man et al. (2022) to identify local reconnection, such as the electron outflowing jets and the out-of-plane current supporting the magnetic field reversal. We see a clear electron bulk flow reversal corresponding well to the current sheet crossing, implying that MMS encountered an active reconnection in this coherent structure. We have further examined all the intense \(E_{||}\) acceleration events. Overall, 30 (~ 44\%) intense \(E_{||}\) acceleration events are associated with local reconnection. Therefore, we conclude that reconnection plays a significant role in accelerating electrons in this event.

4. Discussion and Conclusion

We have analyzed 31 other intervals in the turbulent magnetosheath observed by MMS from the year 2015 to 2019 (Wang et al., 2021). Twenty-two of these intervals are downstream of the quasi-parallel bow shock, and the other 9 events are downstream of the quasi-perpendicular bow shock. These events have a broader range of plasma \(\beta\). We analyze these events by the same method described in this paper and find qualitatively similar results, that is, electrons are predominantly accelerated by \(E_{||}\) no
matter whether the interval is downstream of the quasi-parallel or quasi-perpendicular bow shock.

A further question that needs to be addressed is whether the \( E_{||} \) acceleration in the coherent structures is due to Landau damping, stochastic heating, or Joule-type dissipation. Since the electrons are magnetized most of the time, they could not be energized through stochastic heating, which requires that the electron magnetic moment is not conserved (e.g., Vech et al., 2017). This event is different from the events reported by Afshari et al. (2021) and Chen et al. (2019), which demonstrate that electrons were accelerated through Landau resonance with the kinetic Alfvén waves. One major difference is that the magnetic field is relatively stable and has few coherent structures in the events studied by Afshari et al. (2021). This is also manifested by the non-Gaussian PDF of the \( E_{||} \) acceleration rate in our event, whereas the PDF is near Gaussian in turbulence dominated by Landau damping (not shown). Importantly, we find that the large \( E_{||} \) acceleration studied in this paper is usually associated with unipolar \( E_{||} \) rather than wave-like \( E_{||} \). Thus, the \( E_{||} \) acceleration observed in our event is unlikely caused by Landau damping. More detailed analysis using the field-particle correlation technique for each intense \( E_{||} \) acceleration event can be performed to further understand \( E_{||} \) acceleration in these coherent structures.

In summary, we have investigated how electrons are being accelerated through the dissipation of magnetic energy in nonlinear turbulence in the Earth’s magnetosheath. Since electrons are mostly magnetized, we classify the acceleration mechanisms into three types: Fermi process, betatron mechanism, and \( E_{||} \) acceleration. We find that the PDF of \( E_{||} \) acceleration is significantly broader than the PDF of the other two acceleration rates, which implies that electrons are predominantly accelerated by parallel electric fields. \( W_{E_{||}} \) increases with the reduction of the spatial scale and the increment of the PVI index, suggesting that the \( E_{||} \) acceleration is the most effective around the ion inertial length and coherent structures play a vital role in energizing electrons through \( E_{||} \). We demonstrate that electrons are accelerated through Joule-type dissipation/heating in strong turbulence containing many coherent structures, which is another important building block of the particle energization physical scenario besides
the mechanism proposed by Chen et al. (2019) and Afshari et al. (2021).

The acceleration and heating of ions by turbulence may be quite different to the electrons because ions are expected to be demagnetized due to their much larger gyroradius. Hence one cannot use the guiding center approximation to describe the ion motion and may resort to other methods to quantify the ion acceleration, which is underway for further report.

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Data Availability Statement
The data used in this study was obtained from the MMS Science Data Center (https://lasp.colorado.edu/mms/sdc/public/about/browse-wrapper/).
Figure 1. Overview of the turbulence in the magnetosheath observed by MMS from 07:08:14 to 07:18:34 UT on 18 December 2016. From the top to bottom are: (a) three components of the magnetic field and (b) the electric field; (c) electron number density; (d) ion bulk velocity; (e) electron parallel and perpendicular temperatures; (f) electric current density; (g) $\kappa$ value; (h) – (j) the acceleration rate from $E_||$, Fermi process and betatron mechanism, respectively. The vectors are displayed in the GSE coordinate system.
Figure 2. (a) probability distribution function (PDF) of $\kappa$. The pink line marks $\kappa=3$; (b) PDF of betatron acceleration rate (blue), Fermi acceleration rate (red) and the $E_||$ acceleration rate (green). The green dashed line is the mirror image of the negative $E_||$ acceleration rate; (c) comparison of the PDF of the $E_||$ acceleration rate and the Gaussian curve (black).

Figure 3. (a) Joint PDFs of $E_||$ acceleration rate and the local magnetic field scale $L_{dB}$; (b) the average $W_{E||}$ as a function of $L_{dB}$; (c) the average $L_{dB}$ as a function of $W_{E||}/(W_{E||})_{rms}$, here $(W_{E||})_{rms}$ is the root mean square of $W_{E||}$; The vertical bars in panels (b) and (c) represent the standard errors of the mean.

Figure 4. Average $E_||$ acceleration rate (a) and electron temperature (b) conditioned on the binned PVI index. The average $W_{E||}$ is normalized by the averaged value in the entire
interval. The electron temperature is normalized by $\langle T_e \rangle$ in a moving window with duration of 4 s, equivalent to approximately 10 $d_i$. The vertical bars represent the standard error of the mean.

**Figure 5.** An example of the intense $E_\parallel$ accelerate event. From the top to bottom are: (a) three components of the magnetic field; (b) parallel electric field; (c) electric current density; (d) $E_\parallel$ acceleration rate; (e) PVI Index. The shaded area highlights a significant
electron accelerate by $E_\parallel$ within a coherent structure. The expanded view displays the (f) magnetic field; (g) electron bulk velocity and (h) current density in the LMN coordinate system around the coherent structure.

References


