Atmospherically Driven Seasonal and Interannual Variability in the Lagrangian Transport Time Scales of a Multiple-inlet Coastal System

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Abstract

Intense short-term wind events can flush multiple-inlet systems and even renew the water entirely. Nonetheless, little is known about the effect of wind variations at seasonal and interannual scales on the flushing of such systems. Here, we computed two Lagrangian transport time scales (LTTS), the residence and exposure times, for a multiple-inlet system (the Dutch Wadden Sea) over 36 years using a realistic numerical model simulation. Our results reveal pronounced seasonal and interannual variability in both system-wide LTTS. The seasonality of the LTTS is strongly anti-correlated to the wind energy from the prevailing directions, which are from the southwesterly quadrant and coincidently aligned with the geographical orientation of the system. This wind energy, which is stronger in autumn-winter than in spring-summer, triggers strong flushing (and hence low values of the LTTS) during autumn-winter. The North Atlantic Oscillation (NAO) and the Scandinavia Pattern (SCAN) are shown to be the main drivers of interannual variability in the local wind and, ultimately, in both LTTS. However, this coupling is much more efficient during autumn-winter when these patterns show larger values and variations. During these seasons, a positive NAO and a negative SCAN induce stronger winds in the prevailing directions, enhancing the flushing efficiency of the system. The opposite happens during positive SCAN and negative NAO, when weaker flushing during autumn-winter is observed. Thus, large-scale atmospheric patterns strongly affect the interannual variability in flushing and are potential drivers of the long-term ecology and functioning of multiple-inlet systems.
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Key Points:

• The Lagrangian transport time scales in the Dutch Wadden Sea are typically 1.8 times smaller in autumn-winter than in spring-summer.
• The seasonal and interannual variability of the Lagrangian transport time scales is attributed to the local wind.
• The winter interannual variations are well explained by North Atlantic large-scale atmospheric patterns.

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Abstract

Intense short-term wind events can flush multiple-inlet systems and even renew the water entirely. Nonetheless, little is known about the effect of wind variations at seasonal and interannual scales on the flushing of such systems. Here, we computed two Lagrangian transport time scales (LTTS), the residence and exposure times, for a multiple-inlet system (the Dutch Wadden Sea) over 36 years using a realistic numerical model simulation. Our results reveal pronounced seasonal and interannual variability in both system-wide LTTS. The seasonality of the LTTS is strongly anti-correlated to the wind energy from the prevailing directions, which are from the southwesterly quadrant and coincidentally aligned with the geographical orientation of the system. This wind energy, which is stronger in autumn-winter than in spring-summer, triggers strong flushing (and hence low values of the LTTS) during autumn-winter. The North Atlantic Oscillation (NAO) and the Scandinavia Pattern (SCAN) are shown to be the main drivers of interannual variability in the local wind and, ultimately, in both LTTS. However, this coupling is much more efficient during autumn-winter when these patterns show larger values and variations. During these seasons, a positive NAO and a negative SCAN induce stronger winds in the prevailing directions, enhancing the flushing efficiency of the system. The opposite happens during positive SCAN and negative NAO, when weaker flushing during autumn-winter is observed. Thus, large-scale atmospheric patterns strongly affect the interannual variability in flushing and are potential drivers of the long-term ecology and functioning of multiple-inlet systems.

Plain language summary

In multiple-inlet coastal systems, strong wind events efficiently renew the water in these systems. In this paper, we investigate if the flushing of such systems has also a marked response to wind variability at longer time scales. To quantify the flushing, we compute the time that particles, each representing a certain volume of water, spend in the system before leaving it (known as the residence time) and the total time they spend within it considering future returns (known as the exposure time). Our 36-year simulation of the hydrodynamics of the DWS shows that the wind induces seasonal and interannual variations in both spatially-averaged quantities. The seasonality is related to the wind energy from the dominant directions, which is much larger during autumn-winter than during spring-summer. This variation leads to a reduction of both time scales by, on average, a factor 1.8 from spring-summer to autumn-winter. Two well-known North Atlantic large-scale atmospheric patterns, primarily active during autumn-winter, induce interannual variations in the wind and consequently in both time scales. Thus, future changes in these patterns could strongly affect water transport and the ecology of the Dutch Wadden Sea. Similar situations are likely to occur in other multiple-inlet systems.

1 Introduction

Transport time scales (TTS), such as the residence, exposure, transit, age, and flushing times (Zimmerman, 1976; Monsen et al., 2002), are measures for the efficiency of transport and exchange of water or freshwater content within a water body system and with its surroundings (Cucco et al., 2009; Duran-Matute et al., 2014; Rayson et al., 2016; Xiong et al., 2021). They also serve to estimate the time that a substance, like dissolved nitrogen, takes to be transported off-shore from high-productivity coastal regions (Hailegeorgis et al., 2021); to understand the variability of the mineralization rates of organic matter in sediments (den Heyer & Kalff, 1998); to explain regional differences of nutrient and eutrophication levels (González et al., 2008; Schwichtenberg et al., 2017); and as a first-order estimation of the exposure of a region (e.g. a protected area) to pollutants (Soomere et al., 2011; Patgaonkar et al., 2012; Pawlowicz et al., 2019).
Depending on a coastal system’s particularities, the TTS’s variability can be highly affected by tides, freshwater discharge, gravitational circulation, winds, and other factors. The influence of some of these forcing mechanisms on the intra-annual and the seasonal variability of the TTS has been explored in bights (Zhang et al., 2010), bays (Dippner et al., 2019; Jiang et al., 2019) and lakes (Cimatoribus et al., 2019). However, these studies were based on just 1 to 2 years of data, and thus, a robust relationship of the seasonality with the local forcing cannot be expected if there is a marked interannual variability.

A realistic simulation covering 32 years was used by Du and Shen (2016) to study the residence time in the Chesapeake Bay. The seasonal, monthly and interannual variabilities of the system-wide Eulerian residence time were found to be mainly controlled by the freshwater discharge. To determine the role of the wind, they compared two simulations for a given year, one with the full forcing and the other without wind. They found that downstream and upstream winds reduce the residence time in the eastern side of the Bay, whereas only upstream winds increase the residence time on the opposite side. This means that in this single-inlet system winds from different directions can trigger complex patterns in the TTS but not necessarily induce net transport across the system.

Single-inlet systems contrast with multiple-inlet systems because, in the latter, winds from specific directions are very efficient in forcing net residual transport across the system (Li, 2013; Herrling & Winter, 2015; Duran-Matute et al., 2016). Due to this effect, the influence of other forcing mechanisms can become of secondary importance during strong wind conditions. Thus, winds in multiple-inlet systems can strongly modify the TTS at local, inter-basin, and system-wide scales. This effect has been observed in different multiple-inlet systems using numerical simulations. Cucco and Umgiesser (2006) showed that, in the Venice lagoon, strong northeasterly bora winds (of around 12 m/s) lead to a fully wind-driven dominated system, to a reduction of the system-averaged residence time by a factor of 3, and to a negligible return flow. In the Dutch Wadden Sea (DWS), strong winds exceeding 10 m/s, and aligned with the geographical orientation of the system, induce a wind-driven flow that reduces the system-wide flushing time of freshwater discharge by a factor of 10-15 (Duran-Matute et al., 2014; Donatelli et al., 2022a). Similar strong winds as in the previous cases, also reduced the monthly-average residence time by about a factor 2 in the Virginia Coast Reserve (Safak et al., 2015); and the daily-average Lagrangian residence time (for particles released every 1h during a particular day) in areas located between the inlets of the Barnegat Bay-Little Egg Harbor estuary by a factor between 2-4 (Defne & Ganju, 2015).

Until now, the previous studies linking TTS to wind in multiple-inlet systems focused on idealized fixed wind conditions (e.g. Cucco & Umgiesser, 2006), synoptic-scale events (e.g Duran-Matute et al., 2014; Safak et al., 2015) and annual statistics (e.g Donatelli et al., 2022a). In the latter case, Donatelli et al. (2022a) showed that sporadic strong high-frequency winds (with time scales in the order of days) could impact the annual TTS averages in the DWS, but also the long-term values (mean or median representative of their 11-year simulation). However, they did not isolate the effect of high- and low-frequency winds (with time scales of months or longer) on the TTS to unequivocally attribute the changes in the annual and long-term TTS to high-frequency wind events. The relevance of the low-frequency variability is further suggested by the fact that monthly and multi-decadal sea level variability in the North Sea region is modulated by large-scale atmospheric patterns, which are represented by the North Atlantic Oscillation (NAO), the East Atlantic Pattern (EAP) and the Scandinavia Pattern (SCAN) (Chadik et al., 2017; Frederikse & Gerkema, 2018). Therefore, we investigate if and how much these large-scale atmospheric patterns affect the TTS in the DWS.

Our goal is to determine the low-frequency variability (i.e., the seasonality and interannual variations) of the Lagrangian TTS (LTTS), particularly the residence and exposure times, in a multiple-inlet system. Moreover, we aim to correlate their system-wide
Figure 1. Map of the region of interest. The red contour surrounds most of the DWS and denotes the region where particles were deployed. The names of the five inlets are indicated in black. The Schiermonnikoog and the Terschelling watersheds are marked in green. The location and the names of the two main sluices are depicted in blue. The location of the stations employed for the validation with the sea-surface height (SSH) are shown in magenta. The color bar denotes the depth.

behavior with the wind and large-scale atmospheric patterns. The region of analysis covers most of the DWS (Figure 1): a UNESCO world heritage site and a complex multiple-inlet system. Due to the lack and the difficulty of acquiring observed Lagrangian data in shallow coastal regions, the results are based on a realistic 36-year simulation (1980-2015) of the DWS, combined with particle tracking. The simulation consists of an offline coupling of the General Estuarine Transport Model (GETM; Burchard & Bolding, 2002) with the Probably A Really Efficient Lagrangian Simulator (Parcels) v2.1.1 (Lange & van Sebille, 2017; Delandmeter & Van Sebille, 2019).

2 Data and methods

2.1 Numerical models

2.1.1 Eulerian model

The currents, sea level, salinity, temperature, and density are obtained through three-dimensional, baroclinic numerical simulations performed using GETM. The setup is based on four nested models, with the DWS numerical domain as the end-member. The domain is discretized using an equidistant grid of 200 m resolution using the Rijksdriehoek projection (the standard projection employed by the Dutch Government) in the horizontal and 25 layers in the vertical. The bathymetry was built based on the measurements closest in time to 2009-2010 (see Duran-Matute et al., 2014, for details), and the resulting map was kept fixed throughout the 36-year simulation. This was done intentionally to remove the effects of bathymetry variations on the hydrodynamics of the system and to focus on the role of the atmospheric forcing. The meteorological forcing was taken from
the dataset “Uncertainties in Ensembles of Regional Reanalyses” (UERRA; Ridal et al., 2017), which has a spatial resolution of 11 km and a temporal resolution of 1 h. The freshwater discharge through the Den Oever and Kornwerderzand sluices and 10 other smaller ones was reconstructed based on data from Rijkswaterstaat with a temporal resolution of 12 minutes (see Duran-Matute et al., 2014, for details). Our model configuration is almost identical to those employed by Donatelli et al. (2022a, 2022b), but the simulation here spans 36 years instead of 11 years.

We contrast our numerical results with sea-surface height (SSH) measured at 14 tidal stations located within and around the DWS (Figure 1). Our simulation performed similar as the one by Duran-Matute et al. (2014), and a full description of the validation can be found in Text S1 from Supporting Information S1.

2.1.2 Lagrangian model

Passive particle trajectories were obtained offline by feeding vertically-averaged velocities every 20 minutes from the GETM simulation to Parcels. We used a fourth-order Runge-Kutta method for the temporal integration and a bilinear interpolation in space, which showed to be accurate enough in idealized and realistic applications (Lange & van Sebille, 2017; Delandmeter & Van Sebille, 2019). We used a time step of 158 s to balance accuracy and computational time. It was also chosen to have the timestep as an integer fraction of the M2 tidal period (44714 s), which is the main tidal constituent in the DWS. In our setup, particles were released within the region of interest (denoted with the red contour in Figure 1) in the center of each of the 200 m × 200 m grid cells but skipping every other cell. Then they were advected with depth-averaged currents to capture the effects of the net horizontal currents on water transport. This procedure was repeated every M2 period from January-1980 to October-2015, with each release consisting of 12967 particles. The total amount of particles trajectories obtained is (12967 particles per deployment) × (25290 deployments) ≈ 328 million particle trajectories (≈ 1.1 TB of data). To avoid deploying particles when most of the tidal flats are dry, the first deployment was near the time of maximum water volume within the DWS so that the subsequent ones (every M2 period) were also close to maximum volume conditions. The particle positions were saved every M2 period to remove the back-and-forth due to this dominant semi-diurnal tidal constituent in the DWS (Zimmerman, 1976). We, thus, capture the net residual displacement of the particles. We note that individual tidal periods may deviate somewhat from the M2 period, but since M2 is the dominant constituent, the long-term mean tidal period equals the M2 period(Gerkema, 2019).

To avoid errors in the estimation of LTTS due to particles being stuck because of being released too close to the coast or to areas that seldom flood, we removed such particles from our original dataset (containing ≈ 328 million particles trajectories) using three steps. In the first step, we discarded beaching particles (defined as the ones located within 100 m of a land point at any time), which represents around 8.4% of the original data. In the second step, we removed particles that do not leave our domain of interest (red contour in Figure 1) through its open boundaries within their integration time (around 1.8%). This latter condition help to remove particles whose trajectories can be potentially affected by the poorly resolved flow near the coast, even though they are not beaching according to our definition. These particles can spend some days barely moving and meandering close to the coast due to the small currents present in these areas. In general, these first two steps remove most of the particle trajectories that suffer from numerical artifacts (e.g. error of the numerical solvers, the spatial resolution of the flow, and the temporal time step for the integration of trajectories; which are described by Delandmeter and Van Sebille (2019)). In the third and last step, all the particles released from positions in which the amount of discarded particles (from the previous two steps) represents more than 30% of the total deployments per point of release were also discarded. This step, removes an extra 3.4% of particles. These particles were mostly deployed in
the few regions that are above mean sea level, which are only flood during large storm surges. However, omitting this last step leads to almost the same results because most of the problematic particles were already removed using the first two steps. Finally, after applying all the previous steps, we end up with around 283 million particle trajectories for our analysis.

To check the sensitivity of our results when using non-uniform total integration times, trajectories of particles released at the beginning of every month of our 36-year simulation were integrated for 177 M2 periods (about 91 days). Then, we decreased this time linearly until 117 M2 periods (around 60 days) for the particles released at the end of every month. Particles were not tracked anymore if they crossed the boundaries of the numerical domain before their integration time was reached. We found that under a common integration time of 60 days, instead of the 60-91 days interval employed in our analysis, the results were almost the same since 98.5 % of the 283 million particles left our domain of interest (see red contour in Figure 1) through its open boundaries before 60 days.

### 2.2 Definitions of Lagrangian transport time scales (LTTS)

The Lagrangian residence time is a function of space and time and highlights the spatio-temporal heterogeneity of transport. It is defined as the time required for a particle to exit a domain for the first time (Zimmerman, 1976; Monsen et al., 2002). Nonetheless, this first-crossing definition has a drawback. When particles are close to an open boundary, they might exit the system during ebb and return during flood, possibly repeating this behavior during the following cycles, after which they can remain in the domain for several days. In this way, such a definition of the residence time might give a wrong idea of the actual time particles spend in the system, particularly close to the inlets. We largely avoid this problem by saving particle positions only every M2 period (i.e., using the net or residual displacement). With those generated tracks, we define the Lagrangian residence time as the number of M2 periods required for the particles to leave our domain of interest (red contour in Figure 1) through its open boundaries. Since the residence time varies with space and time, we define $T_{ij}^r$ as the residence time of a particle released during the $j$-th deployment (at time $t_j$) at position $(x_i, y_i)$, where $i$ is the spatial index of the particle released in the center of the 200 m × 200 m grid, and $t_j$ are the times of deployments (every M2 cycle during our 36-year simulation). A similar approach is employed for the Lagrangian exposure time $T_{ij}^e$, which is defined as the total amount of time a particle spends in our system (neglecting the time spent outside of it), and thus $T_{ij}^e \geq T_{ij}^r$ (Monsen et al., 2002; Huguet et al., 2019).

To describe the spatial variability between seasons, we further define the temporal average over $N_{i}^{d}$ deployments as

$$T_i^r = \frac{\sum_{j=1}^{N_i^{d}} T_{ij}^r H^{ij}}{\sum_{j=1}^{N_i^{d}} H^{ij}},$$

(1)

where $N_i^{d}$ is the total amount of deployments per point of release available during time period for averaging, and $H^{ij}$ is the height of the water column in which the particle is deployed. Specifically, we consider two temporal averages: one for all autumn-winter (September-February) and one for all spring-summer (March-August) seasons of our 36-year simulation. The weighted average using $H^{ij}$ is employed because particles are advected with depth-averaged currents, and thus, a particle released over a large water column represents more fluid with that value of $T_{ij}^r$ (Ridderinkhof & Zimmerman, 1990). To study the variability of the system-wide LTTS, we define the spatial average over all $N_{j}^{p}$ par-
particles released at the same time as

\[ T^i_j = \frac{\sum_{i=1}^{N^i_j} T^i_j H^i_j}{\sum_{i=1}^{N^i_j} H^i_j}. \]  

(2)

Similarly, we obtain \( T^i_j \) and \( T^j_i \) using equivalents to equation (1) and equation (2) for

2.3 Atmospheric forcing characterization

To understand the origin of the variability of the LTTS, we characterize the atmospheric forcing using a local and a large-scale approach.

2.3.1 Local approach

For the local approach, we employ the concept of sectorial wind energy, following Gerkema and Duran-Matute (2017). The wind direction is divided into eight sectors using the indices \( s = 1, \ldots, 8 \), corresponding to southerly (S), southeasterly (SE), easterly (E), northeasterly (NE), northerly (N), northwesterly (NW), westerly (W), and southwesterly (SW) winds (i.e., the direction from which the wind blows). Then, the kinetic energy of an air parcel (wind energy) with mass \( m \) crossing a unit area \( A \) during an interval \( \Delta t \) and from sector or direction \( s \) is given by

\[ E_{s,n} = \frac{1}{2} m W_{s,n}^2 = \frac{1}{2} \rho V W_{s,n}^2 = \frac{1}{2} \rho A \Delta t W_{s,n}^3, \]  

(3)

where \( V \) is the volume, which is equal to the area \( A \) times the length \( W_{s,n} \); \( W_{s,n} \) is the hourly wind speed (used in the GETM simulation) blowing from sector \( s \), with \( n \) as a temporal index running over our full 36-year simulation; \( \Delta t = 3600 \) s is the resolution of our wind data; and \( \rho = 1.225 \) kg m\(^{-3}\) is the density of the air at sea level with temperature of 15\(^\circ\)C.

In all our analysis, the wind energy from the grid point closest to the middle of the Texel inlet is employed. Due to the small spatial variations of the wind inside the DWS, we anticipate that using the wind energy from different locations does not change qualitatively our results, as was also the case for Duran-Matute et al. (2016) in their analysis of the residual volume transport in the DWS.

2.3.2 Large-scale approach

For the large-scale approach, we use the North Atlantic Oscillation (NAO), the East Atlantic Pattern (EAP), and the Scandinavian Pattern (SCAN). To derive them, we perform an empirical orthogonal function (EOF) analysis following Chafik et al. (2017) and Frederikse and Gerkema (2018). With this method, the atmospheric patterns have spatial structures represented by empirical orthogonal functions (EOFs), whereas their temporal variability are captured by principal components (PCs). To obtain the EOFs and PCs, we employ the monthly-mean sea level pressure (SLP) from the NCEP/NCAR Reanalysis 1 (Kalnay et al., 1996) spanning the period 1950-2015 in the North Atlantic/European sector (30°-80°N, 80W-50°E). For every grid cell, the monthly-mean SLP is detrended and deseasonalized, i.e., the linear trend, and the annual and semi-annual components are removed. Then, the data are weighted by the cosine of the latitude at every grid point before computing the EOF analysis. This is done to give less weight to grid cells located towards the poles as they represent less area (which decreases with the cosine of the latitude in spherical coordinates). Finally, the EOF analysis is performed only in the North Atlantic domain to avoid the influence of regions outside of it in the three main modes of variability obtained.
3 Results and Discussions

3.1 Seasonality and interannual variability of the LTTS

The mean autumn-winter and spring-summer spatial patterns for the residence time $T_i^e$ (from equation (1)) are shown in Figures 2a and 2b, and in Figures 2c and 2d for the exposure time $T_i^e$. The lowest values are found near the inlets since they are the primary regions for exchange with the adjacent North Sea. Particles deployed around them leave the system in less than one week, with the corresponding areas being larger during autumn-winter. The highest values are found farther into the basins and mostly in the Western DWS (west of the Terschelling watershed). These values are up to a factor of two larger during spring-summer than during autumn-winter. Most of the particles deployed in the Western DWS during spring-summer tend to return to the DWS (see difference between $T_i^e$ and $T_j^e$ in the inset of Figure 2d). Nonetheless, during autumn-winter (inset of Figure 2c) this effect is observed only in the southern-most part of the domain. Consistent with all of the previously mentioned behavior, the wind roses show a marked difference between autumn-winter (Figure 2e) and spring-summer (Figure 2f), with the former exhibiting more frequent and stronger winds from the W, SW and S directions.

To get a representative seasonal cycle of the LTTS in the full DWS, we computed the spatial mean of the residence and exposures times (i.e., $T_j^e$ and $T_j^e$ from equation (2)). Then, the annual cycle for the residence and exposure times are estimated by fitting $T_j^e$ and $T_j^e$ to a model with a free constant and an annual harmonic. The system-wide annual signal of $T_j^e$ varies from 10-11 days in November-January to 17-18 days in May-July, and for $T_j^e$ from 14-16 days to 24-25 days, respectively (Figure 3). This means that the extra time that particles spend in the DWS system after they leave for the first time is smaller in November-January (around 4 days) than during May-July (around 7 days).

To understand the variability superimposed on the seasonal cycle, high-frequency effects (e.g., tides and energetic synoptic-scale events) from $T_j^e$ (which has an M2 resolution) were removed by computing a 15-day mean, which is shown as $\hat{T}_e$ in Figure 4a. Afterwards, we performed a wavelet analysis (Torrence & Compo, 1998) of this spatially-averaged 15-day-mean residence time ($\hat{T}_r$), using the rectification of the bias proposed by Liu et al. (2007), to capture the localized time-frequency information in our time series. The wavelet power spectrum exhibits the strongest signal around the annual period (Figure 4b). However, anomalous behavior is still observed, with periods displaying a strong annual power (e.g., around 1983, 1990, 2000, and 2014) or a weak one (e.g., around 1986, 1996, 2006, and 2010). Similar results are obtained for the equivalent exposure time $\hat{T}_r$ (Figure 5). Clearly, studies of the DWS based on time series of a few years, like those for 2009-2011 by Duran-Matute et al. (2014, 2016) and for 2005-2015 by Donatelli et al. (2022a, 2022b), cannot capture well this rich temporal variability of the system-wide transport characteristics.

The wavelet power spectrum of $\hat{T}_r$ (Figure 4b) also contains significant power outside the annual signal, like the time spans with strong four-month periodicity around 1984, 1990 and 1997. There are also higher frequency events with a still significant signal but they are close to the background noise. These events cause large peaks with a relatively low persistence of only a few weeks. Thus, to focus on the system-wide low-frequency (seasonal and interannual) variations of the LTTS and to find links with the wind forcing (which we discuss in section 3.2) and large-scale circulation and atmospheric patterns (which will be addressed in section 3.3), we filtered the time series. We removed variability from $\hat{T}_r$ using a wavelet filter with a cutoff period of half a year. This procedure resulted in the half-year low-pass filtered signal of the spatially-averaged 15-day-mean residence time ($\tilde{T}_r$) and exposure time ($\tilde{T}_r$) (see Figures 4a and 5a, respectively). Most of the variability at low frequencies is due to the seasonal cycle. However, there are fluctuations at interannual time scales that modulate it. Clear examples are the anomalous winters (DJF) with the lowest $\tilde{T}_r$ (5-7 days) of 1983, 1990, 1995, 2000, 2007, 2008, and
Figure 2. The time-averaged residence time $T_{ir}$ for a) autumn-winter (September-February) and b) spring-summer (March-August) based on the 36-year simulation; and the mean exposure time $T_{ie}$ for c) autumn-winter (September-February) and d) spring-summer (March-August). The insets in c) and d) show the difference between $T_{ie}$ and $T_{ir}$. Regions in white within the DWS were removed from the analysis (see section 2.1.2). The grey line indicates the -5 m isobath. e) Autumn-winter and f) spring-summer wind rose, in which the purple numbers indicate the percentage of time that the wind blows from a particular direction.
2014 (using the year after December as the name of the winter); or the anomalous win-
ters with the largest $\tilde{T}_r$ (12-17 days) of 1996, 2003, 2006, 2009, and 2010. In summer (JJA),
the variability of the peaks is less pronounced, with values that vary between 15 and 20
days. For $\tilde{T}_e$ (Figure 5a), a similar behavior is observed during those winters, with the
lowest values around 7-8 days and the largest between 16-28 days. During summer, $\tilde{T}_e$
mainly varies between 21 and 30 days.

3.2 Impact of the wind on the system-wide LTTS

To show the dominance of the wind on the variability of the LTTS, we propose a
reconstruction of $\tilde{T}_r$ (and an identical one for $\tilde{T}_e$) using the energy of the most dominant
wind sectors (W, SW, and S). Winds from these directions are the most efficient for driv-
ing a strong residual flow from the Texel inlet to the Vlie inlet and the Terschelling wa-
tershed (Duran-Matute et al., 2014). We refer to this reconstruction as the wind-based
model and is given by

$$\tilde{T}_r = Ae^{-\tilde{E}/B},$$

where $\tilde{E}$ is the sum of the half-year low-pass filter signal of the 15-day-mean wind
energy of the dominant sectors (see Appendix A for the definition of the 15-day-mean wind
energy per sector, and for the computation of $\tilde{E}$). Because $\tilde{T}_r$ and $\tilde{T}_e$ are quantities that
depend on the future, the wind-based model employs $\tilde{E}$ of the next 15-day interval in com-
parison to the LTTS time series. The constants $A$ and $B$ are fitting coefficients. The neg-
ative sign in the argument of the exponential reflects the anti-correlation between $\tilde{T}_r$ and $\tilde{E}$ (Figure 6a), which means that strong $\tilde{E}$ conditions result in low $\tilde{T}_r$ and $\tilde{T}_e$; while the
opposite holds during weak $\tilde{E}$ conditions. The constant $A = 19.29 \pm 0.16$ days (with
95% CI) for $\tilde{T}_r$ represents the maximum value that can be predicted with $\tilde{T}_r$, which is
reached during $\tilde{E} = 0$ conditions. This constant contains the mean effects of the resid-
ual tides, freshwater discharge, and other wind directions not included in the reconstruc-
tion. The constant $B = 2.31 \pm 0.06$ MJ is an e-folding wind energy scale for $\tilde{T}_r$, which
indicates that an increase in $\tilde{E}$ equal to $B$ would lead to a reduction of $\tilde{T}_r$ by 63%. For
the exposure time, there is also a strong anti-correlation between $\tilde{T}_e$ and $\tilde{E}$ (Figure 6b).
The maximum value predicted by $\tilde{T}_e$ is given by $A = 27.96 \pm 0.13$ days, and its e-folding
wind energy scale is $B = 2.07 \pm 0.03$ MJ.
The values of $\overline{T}_r$ (Figure 6a) match the numerical data quite well, with a Pearson correlation coefficient $R = 0.94$ and a root mean square error $RMSE = 1.05$ days (see Wilks (2011) for the definition of $R$ and $RMSE$), with the latter representing 7% of the difference between the largest and lowest $\overline{T}_r$ (15 days). Similar results are obtained for the exposure time (Figure 6b), with $R = 0.95$ and $RMSE = 1.58$ days, which represents 6% of the difference between the largest and lowest $\overline{T}_e$ (25 days). These results reflect the capacity of the wind-based model to capture the seasonality, the energy transfer of most of the anomalous autumn-winter seasons to $\overline{T}_r$ and $\overline{T}_e$, and some of the small spring-summer $\overline{E}$ fluctuations that modify both time scales during these seasons.

An exponential relationship between the residence time and the local forcing was also found in the Pearl River estuary (Sun et al., 2014), but with the freshwater discharge as predictor in this riverine dominated estuary. The exponential model used in their study and in ours captures the asymptotic behaviour of the TTS keeping physical values larger than zero during strong forcing conditions. For our case, the wind-based model can provide robust predictions if, for example, the model would be exposed to larger $\overline{E}$ values not seen during the fitting step. These attributes are hard to achieve with linear or polynomial models, which make the exponential one a good and a simple tool to predict TTS.

An example of the ability of the wind-based model to capture anomalous $\overline{T}_r$ values is the winter of 1990. During this period, the lowest $\overline{T}_r$ is well reproduced, which is related to the largest $\overline{E}$ (3 MJ) of our 36-year record (Figure 6a). On the opposite side, we have the winter of 1996, which is a famous period in the North Sea region due to its eagerness.
Figure 5. As in Figure 4, but for the exposure time.

Figure 6. (a) Time series of the half-year low-pass filter of the spatially-averaged 15-day-mean residence time ($\tilde{T}_r$), which is the same as the red line in Figure 5a; the reconstruction of $\tilde{T}_r$ using the wind-based model ($\tilde{T}_r$, equation (4)); and the sum of the half-year low-pass filter of the 15-day-mean wind energy of the dominant wind sectors W+SW+S ($\tilde{E}$). (b) Time series of the half-year low-pass filter of the spatially-averaged 15-day-mean exposure time ($\tilde{T}_e$); the reconstruction of $\tilde{T}_e$ using the wind-based model ($\tilde{T}_e$, instead of $\tilde{T}_r$ in equation (4)); and $\tilde{E}$.

low temperatures (Loewe, 1996). In this season, winds from the most dominant directions were unusually weak, but strong E winds were predominant, with most of their variability contained in periods of less than half a year. During this winter, $\tilde{T}_r$ shows larger values than expected from the climatological winter months and exhibited closer values to the climatological summer months. The wind-based model (Figures 6a and 6b for $\tilde{T}_r$...
Figure 7. Mean sea level pressure and wind at 10 m above ground for a) autumn-winter (September-February) and b) spring-summer (March-August). These averages were obtained using the monthly NCEP/NCAR Reanalysis 1 data for the 1980-2015 period. The mean wind vector is obtained by separately computing the average wind direction and speed following Farrugia and Micallef (2017). The small purple rectangle in panels (a)-(b) represents the DWS numerical domain. The location of the Azores High (AH) and Icelandic Low (IL) pressure systems are also highlighted.

and $T_e$, respectively) suggests that the large values of the LTTS in winter of 1996 are explained by the weak wind energy from the usually dominant directions and not by the strong easterly winds observed (which are not explicitly included in the wind-based model).

### 3.3 The role of the large-scale atmospheric circulation and patterns on the system-wide LTTS

The annual cycle of the large-scale wind in the subtropical North Atlantic is related to the seasonality (a meridional shift and change in intensity) of the the Azores High and the semi-permanent Icelandic Low North Atlantic pressure systems (Trenberth et al., 1990) (Figure 7). This variability is transferred to the regional wind, which induces a local wind response, and ultimately to the LTTS. As a result, a prevailing climatological wind energy (from the SW quadrant) is induced in the DWS, which was computed fitting the sum of the 15-day-mean wind energy of the dominant sectors (W+SW+S, see equation (A2) in appendix A for the formal definition) to a model with a free constant and an annual harmonic. This signal is aligned with the geographical orientation of the system, and characterized by larger values in autumn-winter than in spring-summer (seven times more when contrasting the peaks in November-January with the lowest values in June-July, see Figure 3). Thus, it explains why the DWS is at its most efficient climatological state for flushing in autumn-winter, which are the seasons when the LTTS are the lowest (Figures 2a, 2b, and 3).

Other low-frequency variations of the wind and sea level pressure, which are not explained by the seasonality, are mainly related to large-scale atmospheric patterns, such as the NAO, EAP and SCAN (Frederikse & Gerkema, 2018). Therefore, our final objective is to determine if interannual variations of the LTTS in the DWS are driven by
Figure 8. The three leading modes of the empirical orthogonal function (EOF) analysis based on the deseasonalized monthly-mean sea level pressure over the North Atlantic sector. (a)-(c) EOFs with units of Pressure (Pa), and (d) the monthly PCs (dotted lines) and their half-year low-pass filtered component (thick lines). The EOF and PC modes are defined following the common positive convention for NAO, EAP and SCAN (see the website of the Climate Prediction Center, https://www.cpc.ncep.noaa.gov/data/teledoc/telecontents.shtml). The first two EOFs (NAO and EAP) are displayed during their positive phases, whereas the third one (SCAN) is depicted during its negative phase. The geostrophic winds computed from the EOFs are depicted with arrows. The variance of the three monthly PCs (PC1 for NAO, PC2 for EAP, and PC3 for SCAN) is scaled to 1, and the numbers in the legend of (d) highlight the fraction of variance explained by the low-pass filtered PCs with respect to their monthly values. The small purple rectangle in panels (a)-(c) represents the DWS numerical domain.
these large-scale patterns. First, we obtain the three leading modes of variability from
the EOF analysis of the deseasonalized monthly-mean SLP in the North Atlantic region
(see section 2.3.2). Their spatial structure (EOFs) and their temporal variations (PCs)
are shown in Figure 8, and they are very similar to those showed by Chaif et al. (2017)
and Frederikse and Gerkema (2018). These first three modes at a monthly scale explain
32%, 17% and 15% of the SLP variability in the North Atlantic domain. They exhibit
large-scale atmospheric structures that are akin to the NAO, EAP and SCAN telecon-
nection patterns. In comparison to the method used by the Climate Prediction Center
(CPC, https://www.cpc.ncep.noaa.gov/data/teledocs/telecontents.shtml), our
EOFs and the CPC teleconnection patterns are quite similar, but our PCs and the CPC
indices are not necessarily fully interchangeable (Frederikse & Gerkema, 2018). Our first
mode (NAO) is characterized by a north-south dipole between the Icelandic low and the
Azores high, and it enhances the intensity of the westerlies in the North Sea basin dur-
ing its positive phase (Figure 8a), whereas the opposite holds during its negative one.
Our second mode (EAP) highlights a strong monopole pressure core south of Iceland with
meridionally oriented geostrophic winds in the North Sea (Figure 8b). Two weak cores
of the opposite sign are also present in the southern part of the subtropical North At-
lantic region and over Eastern Europe respectively. The NAO and EAP teleconnection
patterns modulate the variations in the speed of the jet stream, whereas the NAO mostly
describes the latitudinal shifts of the jet, and hence, the main Atlantic storm track (Woollings
& Blackburn, 2012). Our third mode (SCAN) displays a zonal pressure dipole between
Greenland and Scandinavia, with the strongest center of action over Scandinavia and with
a southeastward extension from Greenland towards the Iberian Peninsula (Figure 8c).
Its associated geostrophic winds exhibit a strong meridional shear in the North Sea with
zonal orientation over much of Western Europe. A positive SCAN is closely related to
the well-known Scandinavian blocking weather regime, which in combination with per-
sistent negative NAO phases, can induce extreme cold outbreaks in Europe during win-
ter (Cattiaux et al., 2010; Kautz et al., 2020).

To link the interannual variations of $T_T$ (and $T_e$) to the large-scale patterns, we re-
move the seasonal component from $T_T$, and then this deseasonalized or anomalous $T_T$ was
reconstructed using a multi-linear regression model. The predictors are based on the monthly
PCs, which were interpolated to match the 15-day resolution of both LTTS, and then
low-pass filtered using a cutoff period of half-year to remove high-frequency variations.
We call this reconstruction the $PCs$ model. Similar to the $wind-based$ model, the PCs of
the next 15-day interval are used as predictors. The reconstruction of $T_T$ is obtained by
joining the seasonal component with the $PCs$ model. This combination is referred to as
the $large-scale$ model and is shown in Figure 9a; whereas the reconstruction of the de-
seasonalized $T_e$ given by the $PCs$ model is shown in Figure 9b. The $large-scale$ model matched
$T_T$ quite well, with $R = 0.94$ and $RMSE = 1.03$ days. It also explains 96% of the vari-
ance of $T_T$ (VAR$_{exp}$ in Figure 9c), from which 72% is attributed to the seasonality, 21%
to SCAN and NAO, and the remaining 3% to EAP. In general, the model captures most
of the autumn-winter variability, but it has difficulties in reproducing the variations of
the spring-summer peaks (Figure 9a), as was also the case for the $wind-based$ model (Fig-
ure 6a). Similar results ($R = 0.92$ and $RMSE = 1.97$ days) and weak spring-summer
predictability for the $large-scale$ model are obtained for $T_e$ (Figure 10).

The maximum predictability of the $PCs$ model in terms of VAR$_{exp}$ and $R$ is found
between November and February (Figure 9d), and it is mainly attributed to SCAN and
NAO. This behavior is expected since the effects of the large-scale patterns are notice-
able when the PCs show strong changes and largest values, which is more common dur-
ing autumn-winter (Figure 8d). The lowest $T_T$ observed during autumn-winter (Figure
9a) are predominantly associated with the interplay between negative SCAN, positive
NAO, and positive EAP (Figure 8d), with the latter having the lowest contribution. The
combination of their spatial patterns tend to induce along-coast anomalous winds (mostly
from W and SW directions) that favor the flushing efficiency of the DWS system. This
Figure 9. (a) Time series of the half-year low-pass filter of the spatially-averaged 15-day-mean residence time ($\bar{T}_r$), its seasonal component, and its reconstruction with the large-scale model (seasonal + PCs model). (b) The deseasonalized $\bar{T}_r$ and its reconstruction with the PCs model. (c) Explained variance $\text{VAR}_{exp}$ and correlation $R$ for the reconstruction of $\bar{T}_r$ using cumulative components of the large-scale model: only the seasonal component; seasonal + SCAN (+SCAN); seasonal + SCAN + NAO (+NAO); and the large-scale model, i.e., seasonal + SCAN + NAO + EAP (+EAP). The $\text{VAR}_{exp}$ is defined as the ratio between the variance of the cumulative components of the large-scale model and the variance of $\bar{T}_r$. (d) Monthly statistics ($\text{VAR}_{exp}$ and $R$) of the reconstruction of the deseasonalized $\bar{T}_r$ with the PCs model. In this case, the $\text{VAR}_{exp}$ is defined as the ratio between the variance of the PCs model and the variance of the deseasonalized $\bar{T}_r$ per month.

behavior is consistent with the study of Chafik et al. (2017), in which negative SCAN and positive NAO patterns explain most anomalous high monthly sea level values observed at several North Sea tidal gauge stations during autumn-winter. According to our results, they are concurrent with strong flushing conditions and with a low likelihood for the particles to return to the DWS (represented by low $\bar{T}_r$ and $\bar{T}_e$, respectively).

Winters with the strongest flushing were well captured by the PCs model (Figures 9a and 9b). For example, in the winters of 1990, 1995, 2007, and 2014, a decrease of $\bar{T}_r$ of around 3-5 days with respect to the December-January climatological value of 10 days was observed, which was related to high $\bar{E}$ (Figure 6a). Therefore, the lowest $\bar{T}_r$ values were induced by large-scale atmospheric patterns and not by storms, which induce high-frequency variations and are commonly associated with the presence of well-known weather regimes (Hochman et al., 2021). For example, during the well-known winter of 1990, two exceptionally strong storms (“Daria” and “Vivian”) passed over central Europe and crossed the North Sea in just few days (Pinto et al., 2009). As a result, they trigger the strongest hourly wind speeds from SW and W directions in our 36-year record (around 30 m/s or 60 MJ), but induced 15-day-mean peaks in the wind energy similar to other less stormy periods. On the other hand, the most anomalous winters with the largest $\bar{T}_r$ values (1996 and 2006) were also well explained by the PCs model. During these winters, an increase
of $\tilde{T}_r$ of about 7 and 4 days with respect to the December-January climatology were observed. However, the PCs model underestimates these values by around 2-3 days and 1 day, respectively. The most extreme change between two consecutive winters (10 days for $\tilde{T}_r$ and about 20 days for $\tilde{T}_e$) occurred between the winters of 1995-1996. In 1995, a combination of negative SCAN with positive NAO and EAP triggered a $\tilde{E}$ stronger than its December-January climatology and induced one of the lowest $\tilde{T}_r$ (around 6 days). The following year, the largest $\tilde{T}_r$ during winter was observed (about 17 days). During this famous winter, positive SCAN and negative NAO induced strong $E$ winds. However, as was stated in the previous section, the lack of $\tilde{E}$ (and hence, the background forcing by the tides and freshwater discharge) is enough to explain why $\tilde{T}_r$ during the 1996 winter was similar to its May-July climatology. In agreement with this, during the winter of 2006 (and to a lesser extent for 2003, 2009, and 2010), $\tilde{T}_r$ was also larger than its climatological value, which was related to quite low $\tilde{E}$, but also to low-frequency energy from the other directions.

### 3.4 Other sources of variability on the LTTS

Variations of the bathymetry were neglected in our simulation, which was done intentionally to isolate the role of the atmospheric forcing in our results. Relative stability in the location and orientation of the major channels connected to the Texel inlet has been observed since approximately 1972 or 40 years after the construction of the Afs-luitdijk in 1932 (Elias et al., 2003, 2006), which is a closure dyke of around 30 km where the two main sluices feeding freshwater into the are located (Figure 1). Changes in the sedimentation-erosion patterns of the channels were observed in these studies, but with only minor modifications of the bathymetry profiles. Thus, during our period of analysis, we expect small effects of these bathymetry variations compared to the large effects of wind, particularly when focusing on the variability of system-wide LTTS, as is the case in most of our results.

The time series of the freshwater discharge from the sluice located at Den Oever is correlated with $\tilde{E}$ ($R = 0.56$) and anti-correlated with $\tilde{T}_r$ ($R = -0.68$) and $\tilde{T}_e$ ($R = -0.6
 Whereas for the sluice located at Kornwerderzand non-significant correlations are obtained. Because of this, it is not trivial to isolate the effect of both sluices on the variability of $\tilde{T}_r$ and $\tilde{T}_e$ under our current approach. However, it is known that the residual volume flow rate through the DWS during strong wind conditions from the dominant directions is one order of magnitude larger than the one associated with the tides and the freshwater discharge (Duran-Matute et al., 2014), and that the total freshwater discharge of both sluices can only explain less than 5% of the variability of the residual transport in this system (Donatelli et al., 2022a). Therefore, we expect that the freshwater discharge and the residual tidal currents are the main factors controlling the background $\tilde{T}_r$ ($A = 19.29$ days) and $\tilde{T}_e$ ($A = 27.96$ days), which are obtained when the wind energy of the most energetic sectors ($\tilde{E}$) is null in the wind-based model. In addition, these forcing mechanisms also seem to explain part of the variability of $\tilde{T}_r$ and $\tilde{T}_e$ not explained by the wind-based model and the large-scale model during calm conditions (mainly spring-summer months), which are the periods in which both these models show strong lack of predictability.

Because our main results are based on the characterization of the system-wide LTTS, the vertical structure of the LTTS was ignored using depth-averaged currents. Locally, there might be a marked heterogeneity in this vertical structure (Wolk, 2003; Du & Shen, 2016), which might be associated to, for example, a strong gravitational circulation. However, it is not currently feasible to perform a 3D Lagrangian analysis for 36-year of the DWS due to the amount of data required to compute the necessary 3D particle trajectories. Nonetheless, our results can be useful to select, simulate, and understand the 3D-behaviour of the LTTS during particular and striking conditions, like the transition between the winters with strong and weak winds from the most energetic directions in 1995-1996.

4 Conclusions

While it has been acknowledged that high-frequency events, like storms crossing the Dutch Wadden Sea (DWS) in few days or bora winds in the Venice lagoon, can completely renew the water in multiple-inlet systems, we show here that low-frequency wind variability can also play a large role in modulating the transport time scales in a multiple-inlet system. The broad and immediate implication of our results is that interannual changes in the atmospheric patterns can have a much larger effect on the variations of the water transport than may have been expected, and hence, on the long-term ecology and functioning of multiple-inlet systems.

For the case of the DWS, the lowest system-wide Lagrangian transport time scales (LTTS) are observed in several years during autumn-winter months and are well explained by the concurrent negative phase of the Scandinavia Pattern (SCAN) and the positive phase of the North Atlantic Oscillation (NAO), which induce stronger SW and W winds in this system. These winds trigger an anomalous eastward flow that enhances the flushing efficiency, which is typically already strong in autumn-winter. The opposite happens during positive SCAN and negative NAO, and weaker flushing during autumn-winter is observed. In contrast to single-inlet systems (like in the study of Du and Shen (2016)), our results show that system-wide LTTS in multiple-inlet systems, like the DWS, are representative of the overall system when studying the influence of winds on the seasonal and interannual variations of the LTTS. This response is in agreement with the fact that winds from specific intensities and directions are very efficient in forcing net residual transport across watersheds (i.e. tidal divides) and trough the inlets of multiple-inlet systems (Li, 2013; Duran-Matute et al., 2016). A similar response can be expected in other wind-dominated multiple-inlet systems (e.g., along the North Sea coast), leading to seasonal and interannual variations of the LTTS driven by the large-scale circulation and atmospheric patterns, respectively.
Our findings also reveal that care should be taken when observing variations of the long-term values of the residual volume flow rate across inlets and watersheds, when events with strong wind conditions from the analysis are removed. Using this approach, Donatelli et al. (2022a) found changes of the long-term residual volume transport using a 11-year simulation of the DWS. According to our results, this does no necessarily indicate that extreme events can alter these long-term values. Instead, we expect that long-term variations of the residual flow rate in other wind-dominated multiple-inlet systems would be also driven by large-scale atmospheric patterns, as was the case for the interannual variations of the LTTS in the DWS (from our current study), and for the multi-decadal sea level variability along the North Sea coastal areas (Frederikse & Gerkema, 2018).

Finally, our study highlights the importance of understanding the water transport variability due to local and remote forcing to, for example, explain better why large-scale atmospheric patterns affect biological processes (see e.g., Straile & Adrian, 2000; Golubkov & Golubkov, 2021), and to improve analytical models that use TTS to model ecological processes (see e.g., Lucas & Deleersnijder, 2020). From a practical point of view, analytical models like those proposed here to predict the LTTS using the wind and the large-scale atmospheric patterns could be employed to estimate the LTTS during periods not covered by such detailed simulations, particularly, for seasonal forecasts and future climate-change scenarios.

**Conflict of Interest**

The authors declare no conflicts of interest relevant to this study.

**Data Availability Statement**

Data and scripts (based on Python v3.8) used to reproduce the figures of this study are available at the GitHub repository [https://github.com/JeancarloFU/paper_Atmospherically_Driven_Seasonal_Interannual_LTTS_MultipleInlet](https://github.com/JeancarloFU/paper_Atmospherically_Driven_Seasonal_Interannual_LTTS_MultipleInlet). The wavelet analysis is based on the Python package Pycwt v0.3.0a22 ([https://anaconda.org/conda-forge/pycwt](https://anaconda.org/conda-forge/pycwt)), but we added a script to perform the bias correction (Liu et al., 2007) and a wavelet filter (Torrence & Compo, 1998). Monthly-mean sea level pressure and wind at 10 m above ground were obtained from The NCEP-NCAR Reanalysis 1 data, which is provided by the NOAA PSL, Boulder, Colorado, USA, from their website at [https://psl.noaa.gov/data/gridded/data.ncep.reanalysis.html](https://psl.noaa.gov/data/gridded/data.ncep.reanalysis.html). Eulerian data was produced with the GETM/GOTM model, and its set-up is described in Duran-Matute et al. (2014) and Grüwe et al. (2016). The Lagrangian model (Parcels v2.1.1) can be downloaded from [https://anaconda.org/conda-forge/parcels](https://anaconda.org/conda-forge/parcels) or [https://oceanparcels.org](https://oceanparcels.org).

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**Appendix A  Wind energy averaging**

To establish connections with the LTTS and to smooth the noisy, hourly, high-resolution wind energy data from equation (3), and to remove most of the high-frequency effects (e.g., storms), we compute the mean wind energy during 15-day intervals. For a given
sectorial direction $s$, the 15-day-mean wind energy is defined as

$$E_s = N^{-1} \sum_n E_{s,n} = \frac{1}{2} \rho A \Delta t N^{-1} \sum_n W_{s,n}^3 = C \Delta t N^{-1} \sum_n W_{s,n}^3, \quad (A1)$$

where $N = 360$ is the total amount of hourly data points, $C = \frac{1}{2} \rho A = 0.6125$ kg m$^{-1}$, and the total wind energy is obtained from $E_T = \sum_s E_s = C \Delta t N^{-1} \sum_n W_n^3$, where $W_n^3 = \sum_n W_{n,s}$ is the cube of the hourly wind speed. A similar expression to equation (A1), but for yearly averages, was used by Gerkema and Duran-Matute (2017) and Donatelli et al. (2022a).

The sum of the wind energy of the most energetic sectors (W+SW+S) is obtained from equation (A1) yielding

$$E = E_W + E_{SW} + E_S. \quad (A2)$$

This time series, with 15-day resolution, was employed to compute the annual cycle showed in Figure 3.

Then, we apply a half-year low-pass filter to each $E_s$ (equation (A1)), as was done for the LTTS, which we call $\tilde{E}_s$. Due to the undulatory nature of the wavelet filter (and other similar ones like the Lanczos filter) and to the fact that $E_s$ could be near zero, slightly negative values appear. To be physically correct, we set all negative values of $\tilde{E}_s$ to zero. Finally, we add $\tilde{E}_s$ from the most energetic sectors (W+SW+S), and get $\tilde{E}$, which we call the sum of the half-year low-pass filter of the 15-day-mean wind energy of the dominant sectors. Almost identical results are obtained if we apply the low-pass filter directly to $E$ defined in equation (A2).

References


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Supporting Information for
“Atmospherically Driven Seasonal and Interannual
Variability in the Lagrangian Transport Time Scales of
a Multiple-inlet Coastal System”

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Contents of this file

Text S1

Introduction

This supporting information contains the text S1 that provide details about the
validation of the Eulerian numerical model, which was employed to feed a Lagrangian
model to obtain particles trajectories. The references used in Texts S1 are also provided.

Text S1

Model validation using sea-surface height (SSH), currents, temperature, and salinity
during the year 2009-2010 was done by Duran-Matute et al. (2014) and Gräwe et al.
(2016) using similar model configurations. We have validated our simulation only for the
years 2009-2010, as was done by Duran-Matute et al. (2014), because the bathymetry
is mostly based on those years. Thus, it is expected that the simulation during this time-
span is most compatible with observations. We contrast our numerical results with SSH
measured at 14 tidal stations located within and around the DWS (Figure 1 from the
main manuscript), and with the amplitude and phase of the M2, S2 and M4 tides. In
general, our simulation shows similar performance to that of Duran-Matute et al. (2014)
(see Table 1), which is remarkable because Duran-Matute et al. (2014) used results from
a two-dimensional model with data assimilation to impose SSH at the boundaries. The
good performance of the model is also reflected in the form factor F=(K1+O1)/(M2+S2),
which is defined as the ratio of the amplitudes of the K1 and O1 harmonics to those of
the M2 and S2 ones (Defant, 1961). The observations and the simulation by Duran-Matute
et al. (2014) yield F=0.166, whereas F=0.175 for our case. We have not validated directly
our simulated particles trajectories with observational data in the DWS due to the dif-
ficulty of acquiring it in shallow coastal systems containing large areas of intertidal flats.
However, our model configuration was employed recently by Donatelli et al. (2022a, 2022b),
whose results showed good agreement with those of previous numerical setups in the DWS
region (Duran-Matute et al., 2014; Gräwe et al., 2016). Therefore, we expect that this
performance is also reflected in our Lagrangian analysis.

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Table 1. Summary of the Model Skill Assessments of the SSH, and M2, S2 and M4 Tides for the Period 2009–2010

<table>
<thead>
<tr>
<th></th>
<th>SSH</th>
<th>M2</th>
<th>S2</th>
<th>M4</th>
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<td></td>
<td>R</td>
<td>MAE&lt;sub&gt;amp&lt;/sub&gt; (%)</td>
<td>MAE&lt;sub&gt;pha&lt;/sub&gt; (min)</td>
<td>MAE&lt;sub&gt;pha&lt;/sub&gt; (min)</td>
</tr>
<tr>
<td>RMSE (m)</td>
<td>0.15 (0.10)</td>
<td>4.3 (6.1)</td>
<td>10.6 (4.3)</td>
<td>15.0 (8.7)</td>
</tr>
<tr>
<td>NRMSE (%)</td>
<td>3.5 (2.3)</td>
<td>4.6 (8.7)</td>
<td>9.6 (9.3)</td>
<td>46.5 (27.5)</td>
</tr>
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</table>

The values displayed in this table represent the average of the 14 tidal stations located around the DWS (Figure 1 from the main manuscript). In the second column the performance of the SSH is shown in terms of the correlation R, the root mean square error RMSE, and the NRMSE, which is the RMSE normalized with the difference between the largest and lowest observed SSH. In the last three columns the results for the M2, S2, M4 in terms of the mean absolute error MAE are displayed (see Wilks (2011) for the definition of R, RMSE and MAE). The MAE is in percent for the amplitude and in minutes for the phase. In parenthesis, we give the statistics obtained with the simulation of Duran-Matute et al. (2014).

References


