Mesoscale eddies enhance the air-sea CO$_2$ sink in the South Atlantic Ocean

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Abstract

Mesoscale eddies are abundant in the global oceans and known to affect marine biogeochemistry. Understanding their cumulative impact on the air-sea carbon dioxide (CO$_2$) flux is likely important for quantifying the ocean carbon sink. Here, observations and Lagrangian tracking are used to estimate the air-sea CO$_2$ flux of 67 long lived (i.e. > 1 year) mesoscale eddies in the South Atlantic Ocean over a 16 year period. We find that anticyclonic eddies originating from the Agulhas retroflection and cyclonic eddies originating from the Benguela upwelling act as net CO$_2$ sinks over their lifetimes. In combination, the eddies significantly enhanced the CO$_2$ sink into the South Atlantic Ocean by 0.08 ± 0.01%. Although this modification appears small, long lived eddies account for just ~0.4% of global ocean eddies and eddy activity is increasing; therefore, explicitly resolving eddy processes within all models used to assess the ocean carbon sink would appear critical.
Supporting Information for

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Figure S1: Example output from the Lagrangian eddy tracking approach for an anticyclonic eddy. (a) Blue line indicates the monthly $p\text{CO}_2\text{(sw)}$ estimated with the SA-FNN$_{NCP}$, and shading indicates the uncertainty on the SA-FNN$_{NCP}$ retrieval. Red line indicates the monthly atmospheric $p\text{CO}_2$ for the mean location of the eddy in the respective month. (b) Blue line indicates the daily sea surface temperature (SST) for the eddy lifetime. Red line shows the calendar month medians of SST. (c) Blue line indicates the daily net community production (NCP) for the eddy lifetime. Red line shows the calendar month medians of NCP. (d) Red line shows the geographic track of the eddy over the lifetime. (e) Black line indicates the monthly $p\text{CO}_2\text{(sw)}$. Red line indicates the thermal contribution and blue line indicates the non-thermal contribution to the $p\text{CO}_2\text{(sw)}$ variability. (f) Black line shows the cumulative net $\text{CO}_2$ flux, where the shading indicates a 95% confidence interval.
The global ocean ship-based hydrographic investigations program (GO-SHIP) research cruises conduct hydrographic observations which include Dissolved Inorganic Carbon (DIC) and Total Alkalinity (TA) along CLIVAR/WOCE repeat hydrographic sections. Transects within the South Atlantic Ocean between 2002 and 2018 were downloaded from the NODC/NOAA data centre (https://www.ncei.noaa.gov/access/ocean-carbon-data-system/oceans/RepeatSections/, last accessed: 29/09/2021), which included sections A10 (2003; 2011; 2017), A9.5 (2009; 2018), A13.5 (2013) and A16S (2005; 2013; Fig. S2 a). Each transect was analysed for measurements which coincided with anticyclonic or cyclonic eddies tracked in our study. \( p\text{CO}_2 \) (sw) was calculated from DIC and TA using CO2SYSv3 (van Heuven et al., 2011; Lewis et al., 1998; Orr et al., 2018; Sharp et al., 2021), and the reported uncertainties in DIC (~2 µmolkg\(^{-1}\)), TA (~2 µmolkg\(^{-1}\)), carbonic acid (Waters et al., 2014) and \( \text{H}_2\text{SO}_4 \) dissociation constants (Dickson, 1990) were propagated to retrieve the \( p\text{CO}_2 \) (sw) uncertainty. The in situ \( p\text{CO}_2 \) (sw) were corrected to a consistent temperature and depth dataset (Reynolds et al., 2002), following the methodology described in Goddijn-Murphy et al. (2015), to be consistent with the SA-FNN\(_{\text{NCP}}\) sub skin \( p\text{CO}_2 \) (sw) observations (Ford et al., 2022; Woolf et al., 2016).

The Following Ocean Rings in the South Atlantic (FORSA) cruise, sampled six anticyclonic eddies with a continuous underway \( p\text{CO}_2 \) (sw) system, described in Orselli et al. (2019). These \( p\text{CO}_2 \) (sw) observations were reanalysed to a consistent temperature and depth dataset (Goddijn-Murphy et al., 2015; Reynolds et al., 2002) using the “fe_reanalyse_socat.py” functions within the open source FluxEngine (Holding et al., 2019; Shutler et al., 2016), and the cruise track analysed for anticyclonic and cyclonic eddies tracked in our study. The mean and standard deviation of in situ \( p\text{CO}_2 \) (sw) for matching eddies were extracted for the region within the AVISO+ eddy radius.

In total six anticyclonic (GO-SHIP = 4; FORSA = 2; Fig. S2a) and two cyclonic (GO-SHIP = 1; FORSA = 1; Fig. S2b) eddies tracked in our study were sampled in situ. The in situ \( p\text{CO}_2 \) (sw) were compared with the SA-FNN\(_{\text{NCP}}\) \( p\text{CO}_2 \) (sw) estimates for the month the eddy was sampled in situ (Fig. S2c). The SA-FNN\(_{\text{NCP}}\) \( p\text{CO}_2 \) (sw) estimates were accurate compared to the \( p\text{CO}_2 \) (sw) in anticyclonic eddies with a low root mean square difference (RMSD; 10.2 µatm; Fig. S2c) but showed a higher RMSD for the cyclonic eddies (20.9 µatm; Fig S2c), although this was lower than the SA-FNN\(_{\text{NCP}}\) accuracy (21.48 µatm) (Ford et al., 2022).
Figure S2: (a) Dashed coloured lines indicate the trajectories of tracked anticyclonic eddies that were sampled in situ, where the sampling location is highlighted by the same coloured point. Solid coloured lines indicate cruise tracks which sampled the respective eddy. (b) Same as (a) but for cyclonic eddies. (c) Comparison of in situ pCO$_2$ (sw) with SA-FNN NCP pCO$_2$ (sw) for anticyclonic (red errorbars) and cyclonic eddies (blue errorbars). Central coloured point represents the respective eddy sampled in (a) or (b). In plot statistics are root mean square deviation (RMSD), bias and the number of eddies (n). Inset indicates an eddy centric diagram identifying the location the in situ stations sampled (coloured points) with respect to the eddy radius (dashed line). Note the FORSA cruise sampled pCO$_2$ (sw) continuously and therefore does not appear on the inset.
Supplementary C – Are mesoscale eddies distinct from their environment?

Daily anomalies in MODIS-A SST, SSS and NCP within both anticyclonic and cyclonic eddies were calculated with respect to the environmental conditions surrounding the eddy (described in section 2.2). The daily anomalies were fit with a ‘smoothing spline’ function within MATLAB (smoothing parameter = 4.14 × 10^{-7}) to identify the longer term variations in the anomalies for each eddy (Fig. S3; Fig. S4). The anticyclonic eddies generally showed initial positive SST (Fig. S3a) and SSS (Fig. S3b) anomalies, which were converted to negative SST anomalies within ~6 months from the start of eddy tracking. The strength of negative SST anomalies were generally greater in austral winter, than summer. SSS anomalies indicated a linear decrease over time, as the eddy moved into the South Atlantic gyre. The cyclonic eddies showed initial negative SST anomalies which rapidly increase to ~ 0, but with seasonal fluctuations (Fig. S3c). The SSS anomalies however showed no clear pattern and were generally weak (Fig.S3d).
Figure S3: Smoothed anomalies in physical parameters (SST and SSS) within mesoscales eddies with respect to the environmental conditions. (a) and (c) show SST anomalies for anticyclonic (Agulhas) and cyclonic eddies respectively. (b) and (d) show SSS anomalies for anticyclonic (Agulhas) and cyclonic eddies respectively. Black solid line indicates an anomaly of 0.
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Key Points

- Satellite and in situ observations with Lagrangian tracking were used to estimate the cumulative CO$_2$ flux of long lived mesoscale eddies
- Both anticyclonic and cyclonic eddies enhance the CO$_2$ sink into the South Atlantic Ocean.
Abstract

Mesoscale eddies are abundant in the global oceans and known to affect marine biogeochemistry. Understanding their cumulative impact on the air-sea carbon dioxide (CO$_2$) flux is likely important for quantifying the ocean carbon sink. Here, observations and Lagrangian tracking are used to estimate the air-sea CO$_2$ flux of 67 long lived (i.e. > 1 year) mesoscale eddies in the South Atlantic Ocean over a 16 year period. We find that anticyclonic eddies originating from the Agulhas retroflection and cyclonic eddies originating from the Benguela upwelling act as net CO$_2$ sinks over their lifetimes. In combination, the eddies significantly enhanced the CO$_2$ sink into the South Atlantic Ocean by $0.08 \pm 0.01\%$. Although this modification appears small, long lived eddies account for just $\sim 0.4\%$ of global ocean eddies and eddy activity is increasing; therefore, explicitly resolving eddy processes within all models used to assess the ocean carbon sink would appear critical.

Plain Language Summary

Ocean mesoscale eddies are formed when part of a main current becomes separated to form circular rotating currents that propagate across the oceans. These eddies last from weeks to years and can modify the ocean properties of the water captured within them, which in turn affects the net exchange of carbon between this water and the atmosphere. Little is known about how these eddies modify the absorption of carbon across the global ocean, collectively referred to as the ocean carbon sink, despite them being ubiquitous features of the global oceans. Using satellite-based observations and in situ observations, we show that eddies in the South Atlantic Ocean enhance the absorption of carbon from the atmosphere, thus modifying the ocean to be a stronger net sink of carbon. These results are important as they quantify how much eddies contribute to the absorption of carbon from the atmosphere to the ocean. Our results highlight the need to include the impact on carbon uptake by eddies in models used to assess ocean carbon budgets.

1. Introduction

Mesoscale eddies, characterised by radii on the order of 100 km and lifetimes of weeks to years, are ubiquitous in the global oceans (Chelton et al., 2011; Pegliasco et al., 2022). Eddies
modify the physical (Laxenaire et al., 2019; Nencioli et al., 2018), biological (Carvalho et al., 2019; Dufois et al., 2016; Lehahn et al., 2011; Roughan et al., 2017), and chemical (Arhan et al., 2011; Chen et al., 2007; Orselli, Goyet, et al., 2019; Orselli, Kerr, et al., 2019) characteristics of the ocean compared to the surrounding waters and can be advected far away from their origin. Alteration of the ocean surface conditions can modulate the air-sea exchange of CO$_2$ through changes in the partial pressure of CO$_2$ ($p_{CO_2}$(sw)) (Chen et al., 2007; Jones et al., 2017; Orselli, Kerr, et al., 2019; Song et al., 2016), solubility of CO$_2$, and the overlying atmospheric conditions (Frenger et al., 2013; Pezzi et al., 2021; Souza et al., 2021). Despite their abundance however, few studies have investigated the role of eddies in the air-sea exchange of CO$_2$ (Chen et al., 2007; Jones et al., 2017; Pezzi et al., 2021) and estimated their cumulative impact on the oceanic CO$_2$ sink (Orselli, Kerr, et al., 2019).

Anticyclonic eddies generally display high-pressure centres, displace isopycnals downwards, and have higher sea surface temperatures (SST) than the surrounding environment (McGillicuddy, 2016). The solubility of CO$_2$ in seawater decreases with increasing temperature (Weiss, 1974), and biological activity would hypothetically decrease due to lower nutrient inputs into the surface layer (Gaube et al., 2014; Liu et al., 2018). Therefore, these anticyclonic features are commonly thought to increase $p_{CO_2}$(sw) and considered as weak CO$_2$ sink or even source of CO$_2$ to the atmosphere. Cyclonic eddies are expected to follow the opposite convention with low-pressure centres, lower SST, elevated isopycnals, enhanced biological activity and therefore decreased $p_{CO_2}$(sw), potentially enhancing the CO$_2$ sink.

Mesoscale eddies are, however, intricate structures, and the way they modify the air-sea CO$_2$ fluxes is likely to be more complex. Jones et al. (2017) identified that both anticyclonic and cyclonic eddies were hotspots for CO$_2$ drawdown in the Southern Ocean. Orselli, Kerr et al. (2019) showed that anticyclonic (Agulhas) eddies are a stronger CO$_2$ sink than the surrounding water in the South Atlantic. By contrast, Pezzi et al. (2021) identified an anticyclonic eddy as a CO$_2$ source and Chen et al. (2007) reported that a single cyclonic eddy in the North Pacific weakened the CO$_2$ sink by ~17%. Song et al. (2016) showed that the way in which eddies modify the air-sea CO$_2$ flux can change seasonally in the Southern Ocean: anticyclonic eddies were stronger CO$_2$ sources in winter and stronger CO$_2$ sinks in summer, and the opposite was found for cyclonic eddies. The ability of mesoscale eddies to modify the CO$_2$ flux as they age (Orselli, Kerr, et al., 2019), may also have a seasonal variability.
The South Atlantic Ocean has some of the largest long-lived (>1 year) anticyclonic eddies globally, originating from the Agulhas retroflection (Lutjeharms, 2006), and can propagate to the Brazilian Coast (Guerra et al., 2018). In conjunction, cyclonic eddies forming from the Benguela upwelling system also propagate across the basin (Chelton et al., 2011; Pegliasco et al., 2022; Rubio et al., 2009). The effect of eddies on the air-sea CO₂ flux, differences between anticyclonic and cyclonic, and their role in the global ocean CO₂ sink requires further investigation, especially since eddy kinetic energy has been increasing globally (Martínez-Moreno et al., 2021).

The objective of this study is to estimate the air-sea CO₂ flux of long-lived mesoscale eddies in the South Atlantic Ocean using satellite and in situ observations. A total of 67 eddies, 36 Agulhas anticyclonic and 31 Benguela cyclonic, were tracked using satellite observations (2002 - 2018) and Lagrangian cumulative air-sea CO₂ fluxes were estimated in order to assess their role in the South Atlantic CO₂ sink. To help understand which processes are controlling any detected change in flux over the lifetime of each eddy, the pCO₂(sw) timeseries for each eddy was decomposed into the thermal and non-thermal drivers.

2. Data and Methods

2.1. Sea surface temperature, salinity, biological and wind speed data

Daily 4 km resolution chlorophyll a (chl a) composites were calculated from Moderate Resolution Imaging Spectroradiometer on Aqua (MODIS-A) Level 1 granules, downloaded from the National Aeronautics Space Administration (NASA) Ocean Colour website ([https://oceancolor.gsfc.nasa.gov/; accessed 10/12/2020](https://oceancolor.gsfc.nasa.gov/)), using SeaDAS v7.5, and applying the standard OC3-CI algorithm for chl a ([https://oceancolor.gsfc.nasa.gov/atbd/chlor_a/; accessed 15/12/2020](https://oceancolor.gsfc.nasa.gov/atbd/chlor_a/)). Coincident daily composites of SST (NASA OBPG, 2015) and photosynthetically active radiation (PAR) (NASA OBPG, 2017b) were also downloaded from the NASA ocean colour website ([https://oceancolor.gsfc.nasa.gov/; accessed 10/12/2020](https://oceancolor.gsfc.nasa.gov/)). SST, PAR and chl a were used to estimate net primary production (NPP) using the Wavelength Resolving Model (Morel, 1991) with the look up table described in Smyth et al. (2005). Daily net community production (NCP) composites were generated using NPP and SST data with the algorithm NCP-D described in Tilstone et al. (2015). The chl a, NPP, NCP and SST satellite algorithms were
shown to perform best in the South Atlantic with respect to \textit{in situ} data in an algorithm intercomparison which accounted for \textit{in situ}, satellite and algorithm uncertainties (Ford et al., 2021). Daily 8 km sea surface salinity (SSS) composites were retrieved from the Copernicus Marine Service (CMEMS) physics reanalysis product (GLORYSV12) (CMEMS, 2021). Daily 0.25 ° resolution wind speed at 10 m were downloaded from Remote Sensing Systems Cross-Calibrated Multi-Platform (CCMP) product (Wentz et al., 2015). All data were retrieved for the period July 2002 to December 2018.

\textbf{2.2. AVISO+ Mesoscale Eddy Tracking Product and Lagrangian Tracking}

The AVISO+ Mesoscale Eddy Product META3.1exp (Mason et al., 2014; Pegliasco et al., 2021, 2022) which is based on satellite altimetry was used to identify the trajectories of mesoscale eddies within the South Atlantic Ocean, and provides daily estimates of the eddy location and radius. Anticyclonic (Agulhas) eddies were analysed if: (1) the eddy trajectory started in the Agulhas retroflection region (30 °S – 40 °S; 5 °E – 25 °E; Fig. 1a); (2) the eddy trajectory was longer than 1 year; and (3) the trajectory crossed 0 °E into the South Atlantic gyre region. These criteria identified 36 anticyclonic eddies for analysis between July 2002 and December 2018, that entered the South Atlantic as a single trajectory from formation to dissipation, with limited interactions with other eddies. The selection procedure was repeated for cyclonic eddies originating from the Benguela upwelling system (15 °S – 40 °S; 5 °E – 25 °E; Fig. 1a), which identified 31 cyclonic eddies for further analysis.

For each eddy, a daily timeseries of SST, SSS, NCP and wind speed was constructed using the eddy location and radius estimates from the AVISO+ product. For each parameter, the available data were extracted assuming a circular eddy and the median value taken when at least 30% of the data within the eddy were available. An example of the timeseries extraction is presented in Fig. S1. To quantify the effect of eddies with respect to the surrounding conditions, daily timeseries of the environmental conditions were also extracted from a circular region three times the radius of eddy (radii from two to five were tested; Fig. S5), where data inside the eddy radius were excluded. Median calendar month SST, SSS, NCP and wind speeds were calculated from daily timeseries, both for the eddy and the surrounding environment.
2.3. Sea surface $p$CO$_2$ estimates

The sea surface $p$CO$_2$ ($p$CO$_2$(sw)) was determined for each calendar month of the eddy trajectories using the South Atlantic Feed Forward Neural Network approach (SA-FNN$_{NCP}$; Ford et al. (2022)). The SA-FNN$_{NCP}$ estimates $p$CO$_2$(sw) at the base of the mass boundary layer (sub skin $p$CO$_2$(sw)) (Woolf et al., 2016) using non-linear relationships between $p$CO$_2$(sw) and three environmental drivers; $p$CO$_2$(atm), SST and NCP, which were constructed for eight static provinces in the South Atlantic Ocean. The SA-FNN$_{NCP}$ was supplied with the calendar month median SST and NCP, and the $p$CO$_2$(atm) for the mean location of the eddy within the month which was estimated using the dry mixing ratio of CO$_2$ from the NOAA-ESRL marine boundary layer reference, skin SST and sea level pressure following Dickson et al. (2007). The $p$CO$_2$(sw) uncertainty was estimated by propagating the $p$CO$_2$(atm) (1 µatm), satellite SST (0.441 °C) and NCP (45 mmol O$_2$ m$^{-2}$ d$^{-1}$) (Ford et al., 2021) uncertainties through the SA-FNN$_{NCP}$, and combined in quadrature with the SA-FNN$_{NCP}$ uncertainty (21.48 µatm) (Ford et al., 2022) using standard uncertainty propagation methods (Taylor, 1997).

2.4. Estimation of the cumulative bulk air-sea CO$_2$ flux

The air-sea CO$_2$ flux (F) was calculated for each calendar month of the eddy trajectory using a bulk parameterisation as:

$$ F = k (\alpha_w pCO_2(sw) - \alpha_s pCO_2(atm)) $$

Where $k$ is the gas transfer velocity estimated from median wind speeds following the parameterisation of Nightingale et al. (2000). $\alpha_w$ and $\alpha_s$ are the solubility of CO$_2$ at the base and top of the mass boundary layer at the sea surface (Woolf et al., 2016). $\alpha_w$ was calculated as a function of the skin SST and SSS (Weiss, 1974), applying a cool skin bias of +0.17K to convert the skin SST to sub skin SST (Donlon et al., 1999; Woolf et al., 2016). $\alpha_s$ was calculated as a function of the eddy skin SST and the SSS with a salinity gradient of +0.1 salinity units between the base and top of the mass boundary layer (Woolf et al., 2016). The CO$_2$ flux calculations were carried out with the open source FluxEngine toolbox (Holding et al., 2019; Shutler et al., 2016) using the ‘rapid transport’ approximation (described in Woolf et al., 2016) at monthly time steps. The monthly average daily flux of CO$_2$ (mmol C m$^{-2}$ d$^{-1}$) was multiplied by the number of days and the area of the eddy, assuming a circular eddy with the mean eddy radius, in the respective
month. The fluxes (Tg C mon\(^{-1}\)) were then added cumulatively to retrieve the net cumulative CO\(_2\) flux for each eddy. The uncertainties in \(p\)CO\(_2\) (sw) (temporally varying), \(p\)CO\(_2\) (atm) (1 µatm), SST (0.441 °C) (Ford et al., 2021) and the gas transfer velocity (assumed to be ± 10%; Woolf et al., 2019) were propagated through the cumulative flux calculations using a Monte Carlo uncertainty propagation (N = 1000), and the 95% confidence interval (2 standard deviations) extracted as the uncertainty on the cumulative net CO\(_2\) flux. These cumulative CO\(_2\) flux calculations were repeated for the surrounding environment conditions, assuming the same area as the eddy to estimate the cumulative CO\(_2\) flux as if the eddy were not present. The percentage difference between the eddy and surrounding environment CO\(_2\) flux was computed.

### 2.5. Thermal and non-thermal decomposition of \(p\)CO\(_2\) (sw) timeseries

The eddy \(p\)CO\(_2\) (sw) timeseries was separated into its thermal and non-thermal components as described in Takahashi et al. (2002). The thermal component (\(p\)CO\(_2\) (therm)) was calculated as:

\[
pCO_2 (\text{therm}) = pCO_2 (\text{sw}) \times e^{(0.0423 \times (\overline{SST} - SST))}
\]  

\(\overline{SST}\) and SST are the mean subskin SST across the eddy timeseries and the monthly subskin SST respectively. The non-thermal component (\(p\)CO\(_2\) (bio)) was calculated as:

\[
pCO_2 (\text{bio}) = \overline{pCO_2 (\text{sw})} \times e^{(0.0423 \times (SST - \overline{SST}))}
\]

\(\overline{pCO_2 (\text{sw})}\) was the mean \(p\)CO\(_2\) (sw) for the eddy timeseries. The contributions of the two competing components to the \(p\)CO\(_2\) (sw) timeseries can be determined from the seasonal amplitude of the \(p\)CO\(_2\) (therm) and \(p\)CO\(_2\) (bio):

\[
\Delta pCO_2 (\text{therm}) = [pCO_2 (\text{therm})]_{\text{max}} - [pCO_2 (\text{therm})]_{\text{min}}
\]

\[
\Delta pCO_2 (\text{bio}) = [pCO_2 (\text{bio})]_{\text{max}} - [pCO_2 (\text{bio})]_{\text{min}}
\]

The seasonal amplitudes were calculated using a 12-month moving window for the lifetime of the eddy, and the ratio between the thermal and non-thermal component (R) was determined as:

\[
R = \frac{\Delta pCO_2 (\text{therm})}{\Delta pCO_2 (\text{bio})}
\]

In cases where R is greater (less) than 1, the thermal (non-thermal) contribution was the dominant driver. The anomaly in R was determined by subtracting the mean R across the eddy’s lifetime.
3. Results

A comparison between the SA-FNN$_{\text{NCP}}$ estimated $p_{\text{CO}_2(\text{sw})}$ and in situ $p_{\text{CO}_2(\text{sw})}$ within both anticyclonic ($n = 6$) and cyclonic eddies ($n = 2$; Fig. S2) identified that the SA-FNN$_{\text{NCP}}$ was accurate and precise within anticyclonic eddies (root mean square deviation = 10 µatm; bias = 0 µatm; $n = 6$) but larger differences were apparent in $p_{\text{CO}_2(\text{sw})}$ for the cyclonic eddies, albeit from just two crossovers (root mean square deviation = 21 µatm; bias 11 µatm; $n = 2$).

Both anticyclonic (Agulhas; median = -0.54 Tg C per eddy, minimum = -0.09 Tg C, maximum = -1.01 Tg C) and cyclonic (Benguela; median = -0.27 Tg C per eddy, minimum = -0.02 Tg C, maximum = -0.96 Tg C) eddies acted as cumulative net CO$_2$ sinks over their lifetime (Fig 1b, d). Anticyclonic eddies displayed an exponential decay in the increase of the net cumulative CO$_2$ sink, compared to a more linear increase in cyclonic eddies when fit with the same functional equation (Fig. 1c, e). The anomaly in the thermal to non-thermal contribution to $p_{\text{CO}_2(\text{sw})}$ variability in anticyclonic eddies changed over their lifetimes (Fig. 2a), where a positive anomaly indicates an increasing dominance of temperature on controlling $p_{\text{CO}_2(\text{sw})}$. For cyclonic eddies the anomaly in the thermal to non-thermal component ratio, $R$, did not change significantly over time (Fig. 2b).

The anticyclonic (-3.7%, Mann-Whitney U-Test, $p < 0.001$, $n = 36$) and cyclonic (-1.4%, Mann-Whitney U-Test, $p = 0.007$, $n = 31$) eddies significantly enhanced the cumulative CO$_2$ sink compared to the water surrounding each eddy (Fig. 2c). No significant differences in this enhancement were observed between anticyclonic and cyclonic eddies (Fig. 2c; Mann-Whitney U-Test, $p = 0.16$), although the anticyclonic modification (-3.7%) was double that of the cyclonic eddies (-1.4%; Fig. 2c).
Figure 1: (a) Trajectories of the 36 anticyclonic (red lines) and 31 cyclonic (blue lines) eddies. Red and blue boxes indicate the formation region for the anticyclonic and cyclonic eddies respectively. (b) Red lines indicate the cumulative net CO$_2$ flux for the 36 anticyclonic eddies, where shading is the propagated uncertainty. Black dots indicate the cumulative net CO$_2$ flux at eddy dissipation. Black dashed line indicates the mean cumulative net CO$_2$ flux at eddy dissipation (i.e. mean of black dots). Blue dashed lines indicate the estimates for 6 anticyclonic eddies presented in Orselli, Kerr et al. (2019). (c) Cumulative net CO$_2$ flux for the 36 anticyclonic eddies plotted since eddy formation. Black line indicates a power law fit \( y = a \times x^b + c \) for the temporal evolution of the net CO$_2$ flux of the 36 anticyclonic eddies, where shading indicates the 95% confidence limits. (d) the same as (b), and (e) the same as (c) but for the 31 cyclonic eddies.
Figure 2: (a) Anomaly in the 12-month running thermal to the non-thermal ratio of $\rho$CO$_2$ (sw) for the 36 anticyclonic eddies. Black solid line indicates the linear fit since the formation of the eddy. Black dashed line indicates an anomaly of 0. Statistics within the plot are: Slope is the slope of the linear fit, $R^2$ is the coefficient of determination, Sig is the significance of the linear fit and N is number of samples. (b) Same as (a) but for the 31 cyclonic eddies. (c) Box plots indicating the percent change in the cumulative net CO$_2$ flux at eddy dissipation with respect to the waters surrounding the eddy. Red line indicates the median, blue box indicates the 25th and 75th percentile and whiskers show the minimum and maximum non-outlier values. Red crosses indicate outliers that are more than 1.5 times the interquartile range from the 25th and 75th percentiles. Negative percentages indicate a stronger flux, where positive percentages indicate a weaker flux.

4. Discussion

This is the first study to provide an observation-based assessment of the cumulative net CO$_2$ flux of a large number (67) of long-lived mesoscale eddies. We followed the trajectory of 36 anticyclonic eddies over their lifetime and found that they were a net cumulative CO$_2$ sink (median = 0.54 Tg C per eddy). By comparison anticyclonic (Agulhas) eddies have previously been identified as a net sink for CO$_2$ varying from ~0.6 Tg C to ~1.4 Tg C (median = 1.26 Tg C per eddy; Fig. 1b; Orselli, Kerr et al. (2019)). The Orselli, Kerr et al. (2019) results were based on extrapolation of a snapshot of the eddies CO$_2$ uptake potential from ship observations that
crossed the paths of six eddies. Two of these eddies were tracked in our study (V1, V3; Fig. 1b) and identified as CO$_2$ sinks of 0.64 and 0.40 Tg C compared to 1.34 and 1.36 Tg C by Orselli, Kerr et al. (2019). Orselli, Kerr et al. (2019) sampled eddies in austral winter where they acted as a strong CO$_2$ sink. In our study, the seasonal variability in the CO$_2$ flux is captured, where eddies were stronger sinks in winter and weaker sinks for CO$_2$ in summer, which likely explains the lower cumulative CO$_2$ flux.

Both the anticyclonic and cyclonic eddies showed an increasing cumulative CO$_2$ sink over their lifetime (Fig. 1c, e). For the former, the rate of CO$_2$ uptake decreased exponentially over this period (Fig. 1c). This result is consistent with the geographical propagation of the eddies in the oligotrophic South Atlantic gyre (Fig. 1a), and eddy stirring of the environment (McGillicuddy, 2016). The significant increase in the anomalies of the seasonal thermal to non-thermal $p$CO$_2$ (sw) ratio (becoming more influenced by temperature; Fig. 2a) was found to be mainly driven by a relative reduction in the non-thermal contribution (not shown) and highlights the changing role of biological activity and/or circulation over time as the eddies propagated into the gyre.

Carvalho et al. (2019) showed that the phytoplankton community structure changed as the eddies aged, where younger anticyclonic (Agulhas) eddies were dominated by haptophytes (small flagellates) followed by prokaryotes. Sarkar et al. (2021) highlighted that haptophytes are crucial for the biological CO$_2$ drawdown in the Agulhas retroflection, reinforcing a weaker biological pump as the eddies evolve. In contrast, the cyclonic eddies displayed a linear increase in the cumulative CO$_2$ sink (Fig. 1e). This signature may be because the cyclonic eddies do not propagate as far as anticyclonic eddies into the South Atlantic gyre (Fig. 1a), which is also illustrated by no significant change in the thermal to non-thermal $p$CO$_2$ (sw) ratio anomaly (Fig. 2b).

Both the anticyclonic and cyclonic eddies were shown to significantly increase the CO$_2$ drawdown in the South Atlantic Ocean (Fig. 2c), with respect to the surrounding environment. Jones et al. (2017) showed that both anticyclonic and cyclonic eddies were hotspots for CO$_2$ drawdown of similar magnitude in the Antarctic Circumpolar Current. Dufois et al. (2016) examined chl $a$ variability in anticyclonic eddies and showed that the first two modes of spatial variability were consistent with eddy stirring, and the third mode highlighted the mesoscale modification. In our study, by comparing the cumulative CO$_2$ fluxes of the eddies to a theoretical eddy consisting of surface waters surrounding the eddy, the mesoscale modulation of the air-sea
CO₂ flux was quantified. We showed this modulation to increase the CO₂ sink into anticyclonic and cyclonic eddies by 3.7% and 1.4% respectively (Fig. 2c).

The cyclonic eddies generally showed lower SST, and higher NCP (Fig. S3; Fig. S4) compared to the surrounding waters, suggesting both biological and physical processes are amplifying the CO₂ sink. Chen et al. (2007) showed pCO₂ (sw) to be elevated at the core of a cyclonic eddy in the North Pacific, due to the upwelling of CO₂ rich waters into the surface layer and the eddy acting as a weaker CO₂ sink compared to the surrounding. By comparison, Lovecchio et al. (2022) identified that cyclonic eddies around the Canary upwelling system entrain nearshore nutrient rich waters into the eddy core at formation. Mesoscale upwelling of nutrients was a small component of the total nutrients sustaining the biological production. This suggests that the biological CO₂ drawdown throughout the eddy lifetime is largely supported by the initial nutrient input which ultimately enhances the CO₂ sink through both the physical and biological signatures.

The anticyclonic eddies were associated with elevated SST at formation, which rapidly changed to depressed SST for the remainder of their lifetimes (Fig. S3) compared to the surrounding waters. NCP remained lower than the surroundings (Fig. S4). These characteristics suggest opposing physical and biological forces that modify the air-sea CO₂ flux. Similarly, Laxenaire et al. (2019) showed that the SST anomaly associated with surface water of an anticyclonic (Agulhas) eddy switched from positive to negative over its lifetime, also implying a change from a CO₂ source to sink as it propagated over the South Atlantic basin. This indicates that the physical component exerts the greatest control on amplifying the air-sea CO₂ sink into these anticyclonic eddies.

The work presented here has identified that the ability for eddies to modify the air-sea CO₂ flux (Fig. 2c) is driven by intrinsic differences between individual eddies (Fig. S3, S4). Lehahn et al. (2011) observed an isolated patch of elevated chl a associated with an anticyclonic eddy that was transported into the South Atlantic gyre, perhaps suggesting enhanced biological drawdown of CO₂, but it was not possible to identify if this is a common feature of all anticyclonic eddies.

Entrainment of nutrient rich nearshore waters into the cyclonic eddies (Lovecchio et al., 2022) is likely to be highly variable depending on the location and interaction with other water bodies and the time of year, which will in turn lead to a different biological response and therefore air-sea CO₂ flux. Many mesoscale eddy studies (e.g. Jones et al., 2017; Laxenaire et al., 2019; Orselli,
Kerr, et al., 2019) are limited by the availability of in situ data. The expanding use of Biogeochemical-Argo profilers, especially those with pH sensors (Roemmich et al., 2019), is improving the potential to assess the air-sea CO$_2$ flux both globally and regionally (Gray et al., 2018). However, a synergy of in situ and satellite observations will be required to study mesoscale eddies and the processes that modify the air-sea CO$_2$ flux. Based on a recent assessment by Ford et al. (2022) of the South Atlantic Ocean (20 °S to 44 °S), which estimated the region to be a CO$_2$ sink of 76 Tg C yr$^{-1}$, the long-lived anticyclonic (Agulhas) eddies assuming six eddies are released per year (Lutjeharms, 2006) would contribute 1.3 Tg C yr$^{-1}$ (1.7 %; Table 1). Orselli, Kerr et al. (2019) identified that six anticyclonic (Agulhas) eddies contributed 2.5 Tg C yr$^{-1}$ (3.3 %) to the CO$_2$ sink. Our contribution is likely lower because seasonal variability in the CO$_2$ flux was captured. In combination, the work presented here finds that anticyclonic and cyclonic eddies enhance the oceanic CO$_2$ sink into the South Atlantic Ocean (20 °S to 44 °S) by 0.08% (Table 1). Globally, long lived mesoscale eddies, such as those studied here, make up 0.4% of the eddy trajectories in the AVISO+ dataset (Pegliasco et al., 2022). This suggests that the effect of all eddies on the CO$_2$ flux and net oceanic sink, identified here using observations, is likely to be globally significant as previously indicated by modelling studies. Harrison et al. (2018) for example, showed that mesoscale resolving models may have a modest effect on the global balance of carbon export (<2%), but regionally the effect can be large (±50%). Jersild et al. (2021) highlighted that an Earth System Model (ESM) that explicitly resolved mesoscale eddies was able to produce the observed seasonal biological productivity and $p$CO$_2$$_{sw}$ cycles in the Southern Ocean, but when the eddies were not included, the seasonal cycle was not well reproduced. The results from our study have significant implications on the air-sea CO$_2$ flux in current global ESMs, in which eddies are not explicitly resolved (Hewitt et al., 2017, 2020). Eddy kinetic energy, as a proxy for mesoscale eddy occurrence, has been increasing at a rate between 2 and 5% per decade (Martínez-Moreno et al., 2021), indicating that the role of mesoscale eddies on the oceanic CO$_2$ sink may be becoming more significant. In the context of climate change and increasing global temperatures, further work is required to quantify the influence of these changes on the ocean CO$_2$ sink.
Table 1: The calculation of the modification to the South Atlantic Ocean CO$_2$ sink that mesoscale eddies may contribute. The median percentage change in the eddy flux compared to the surrounding environment is converted to a median Tg C yr$^{-1}$ equivalent and compared to two estimates of the South Atlantic CO$_2$ sink in the region the eddies propagate.

<table>
<thead>
<tr>
<th></th>
<th>Anticyclonic</th>
<th>Cyclonic</th>
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<tbody>
<tr>
<td>Median cumulative CO$_2$ flux (Fig. 1b, d; Tg C per eddy)</td>
<td>-0.54</td>
<td>-0.27</td>
</tr>
<tr>
<td>Median percentage change in CO$_2$ flux compared to surrounding environment (Fig. 2c; %)</td>
<td>-3.7</td>
<td>-1.4</td>
</tr>
<tr>
<td>Additional flux into eddy (Tg C per eddy)</td>
<td>-0.020</td>
<td>-0.004</td>
</tr>
<tr>
<td>Mean eddy lifetime (yr)</td>
<td>2.5</td>
<td>1.7</td>
</tr>
<tr>
<td>Additional flux into eddy per year (Tg C yr$^{-1}$)</td>
<td>-0.008</td>
<td>-0.002</td>
</tr>
<tr>
<td>Spawn Rate (yr)</td>
<td>6 (Guerra et al., 2018)</td>
<td>4 (Chaigneau et al., 2009)</td>
</tr>
<tr>
<td>Additional flux into eddies (Tg C yr$^{-1}$)</td>
<td>-0.05</td>
<td>-0.01</td>
</tr>
<tr>
<td>South Atlantic Ocean CO$_2$ sink estimate of Ford et al. (2022) (-76 ± 8 Tg C yr$^{-1}$) 20 °S to 44 °S</td>
<td>-0.06%</td>
<td>-0.02%</td>
</tr>
<tr>
<td>South Atlantic Ocean CO$_2$ sink estimate of Woolf et al. (Holding et al., 2019; 2019) (-261 ± 28 Tg C yr$^{-1}$) 20 °S to 44 °S</td>
<td>-0.020%</td>
<td>-0.005%</td>
</tr>
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</table>
5. Conclusions

Our analysis presents a novel approach to assess the impact of long-lived mesoscale eddies on the air-sea CO$_2$ flux in the South Atlantic Ocean. Using satellite observations, in situ data and Lagrangian tracking we show that anticyclonic and cyclonic eddies are cumulative net CO$_2$ sinks of 0.54 Tg C and 0.27 Tg C per eddy (median values), respectively. Anticyclonic eddies exhibited an exponential decay in the rate of CO$_2$ uptake, and significant changes in the thermal to non-thermal drivers of the $p$CO$_2$ (sw) ratio anomaly. This shows the thermal and biological contributions to the CO$_2$ sink variability change as the eddies age and propagate over different geographic trajectories in the South Atlantic gyre. The cyclonic eddies showed a more linear rate of change of CO$_2$ uptake, and there was no significant change in the drivers of the seasonal $p$CO$_2$ (sw) ratio anomaly.

Both anticyclonic and cyclonic eddies amplified the CO$_2$ sink compared to the surrounding environment by 3.7% and 1.4%, respectively. For the anticyclonic eddies, physical drivers increased the CO$_2$ sink, whereas the biological component reduced the uptake. In cyclonic eddies both physical and biological components worked synergistically to increase the CO$_2$ sink. Accounting for their typical frequencies, long-lived mesoscale eddies significantly amplify the CO$_2$ sink into the South Atlantic Ocean (20°S to 44°S) by 0.08 ± 0.01%. Although this modification appears small, long-lived eddies make up only 0.4% of eddies in the global oceans, and therefore the amplification of the global CO$_2$ sink from all eddies is likely to be much larger than previously estimated. The inclusion of these mesoscale features within models used to estimate the global ocean carbon sink would improve estimates of the role of the global ocean in the uptake and absorption of anthropogenic CO$_2$.

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**Open Research**

Daily Moderate Resolution Imaging Spectroradiometer on Aqua (MODIS-A) estimates of chlorophyll-a (NASA OBPG, 2017a), photosynthetically active radiation (NASA OBPG, 2017b) and sea surface temperature (NASA OBPG, 2015) are available from the National Aeronautics Space Administration (NASA) ocean colour website (https://oceancolor.gsfc.nasa.gov/). Modelled sea surface salinity from the Copernicus Marine Environment Modelling Service (CMEMS) global ocean physics reanalysis product (GLORYS12V1) are available from CMEMS (CMEMS, 2021). The CCMP daily wind speed products are available from Remote Sensing Systems (www.remss.com/measurements/ccmp; Wentz et al., 2015). *In situ* GO-SHIP DIC and TA
samples can be downloaded from the NOAA/NODC data centre 

(https://www.ncei.noaa.gov/access/ocean-carbon-data-system/oceans/RepeatSections/). FORSA

_in situ_ pCO$_2$ (sw) data can be requested from IBMO. Optimum Interpolated SST (OISST) v2

(Reynolds et al., 2002) data used in the reanalysis of pCO$_2$ (sw) can be downloaded from

https://psl.noaa.gov/data/gridded/data.noaa.oisst.v2.html. The AVISO+ Mesoscale Eddy Product

META3.1exp can be downloaded from https://doi.org/10.24400/527896/a01-2021.001

(Pegliasco et al., 2021).

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Dickson, A. G. (1990). Standard potential of the Standard potential of the reaction - AgCl(s)+1/2H$_2$-2(g)=Ag(s)+HCl(aq) and the standard acidity constant of the ion HSO4$^-$ in synthetic sea-water from 273.15-K to 318.15-K. *The Journal of Chemical Thermodynamics, 22*(2), 113–127. https://doi.org/10.1016/0021-9614(90)90074-Z


