Classifying Magnetosheath Jets using MMS - Statistical Properties

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Abstract

Using Magnetospheric Multiscale (MMS) data, we find, classify and analyze transient dynamic pressure enhancements in the magnetosheath (jets) from May 2015 until May 2019. A classification algorithm is presented, using in-situ MMS data to classify jets (n = 8499) into different categories according to their associated angle between IMF and the bow shock normal vector (θ). Jets appearing for θ < 45° are referred to as quasi-parallel, while jets appearing for θ > 45° as quasi-perpendicular jets. Furthermore, we define those jets that occur at the boundaries between quasi-parallel and quasi-perpendicular magnetosheath as boundary jets. Finally, encapsulated jets are jet-like structures with similar characteristics to quasi-parallel jets while the surrounding plasma is of quasi-perpendicular nature. We present the first statistical results of such a classification and provide comparative statistics for each class. Furthermore, we investigate correlations between jet quantities. Quasi-parallel jets have the highest dynamic pressure while occurring more often than quasi-perpendicular jets. The infrequent quasi-perpendicular jets, have a much smaller duration, velocity, and density and are therefore relatively weaker. We conclude that quasi-parallel and boundary jets have similar properties and are unlikely to originate from different generation mechanisms. Regarding the encapsulated jets, we suggest that they are a special subset of quasi-parallel jets originating from the flanks of the bow shock, for large IMF cone angles although a relation to FTEs and magnetospheric plasma is also possible. Our results support existing generation theories, such as the bow shock ripple and SLAMS-associated mechanisms while indicating that other factors may contribute as well.
Classifying Magnetosheath Jets using MMS - Statistical Properties

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Key Points:

• Classification of a jet database based on $θ_{Bn}$, using MMS magnetosheath data is presented.
• All classes show different properties with some classes being compatible with existing generation mechanisms.
• Bow shock ripple mechanism and SLAMS are generally supported by statistical properties.

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Abstract
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dynamic pressure enhancements in the magnetosheath (jets) from May 2015 to May 2019.
A classification algorithm is presented, using in-situ MMS data to classify jets ($N = 8499$)
into different categories according to their associated angle between IMF and the bow
shock normal vector ($\theta_{Bn}$). Jets appearing for $\theta_{Bn} < 45$ are referred to as quasi-parallel,
while jets appearing for $\theta_{Bn} > 45$ as quasi-perpendicular jets. Furthermore, we define
those jets that occur at the boundaries between quasi-parallel and quasi-perpendicular
magnetosheath as boundary jets. Finally, encapsulated jets are jet-like structures with
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and SLAMS-associated mechanisms while indicating that other factors may contribute
as well.

1 Introduction
The magnetosheath plasma can have strong fluctuations in velocity, density, and
associated magnetic field. A key component that influences the level of fluctuation is the
angle between the IMF and the bow shock normal vector ($\theta_{Bn}$). It has been shown that
in the case of the quasi-parallel shock ($\theta_{Bn} < 45$) the downstream plasma is strongly
turbulent whereas in the quasi-perpendicular shock ($\theta_{Bn} > 45$) there is a much smoother
and calmer environment (Fuselier, 2013; Wilson III, 2016). The main reason the two re-
gions have different characteristics is that in the quasi-parallel case, reflected ions can
travel upstream along the magnetic field lines causing instabilities, and associated wave
growth. This creates a foreshock region characterized by a suprathermal ion distrib-
tution. This region is not present in the quasi-perpendicular case where the transition be-
tween upstream and downstream flow is distinct and straightforward (Schwartz & Burgess,
1991). As a result, in the quasi-perpendicular bow shock, there are much sharper and
well-defined transitions between the upstream and downstream plasma.

Magnetosheath jets are local enhancements of dynamic pressure above the surround-
ing background level, reaching values even higher than the upstream solar wind. The dy-
namic pressure enhancements can be attributed to a density increase (Savin et al., 2008;
Karlsson et al., 2012, 2015), a velocity increase (Archer et al., 2012) or may result from
an enhancement of both (Amata et al., 2011; Plaschke et al., 2013). These jets are mainly
found downstream of the quasi-parallel bow shock and the current prominent formation
theory is that they result from foreshock fluctuations interacting with the bow shock.

Many terms and definitions have been used in the literature to describe the jet phe-
nomenon, as thoroughly discussed in the review paper by Plaschke et al. (2018). In prin-
ciple, the jet determination can be done via two methods. The first one is by using a slid-
ing average time window which indicates a background value on the magnetosheath dy-
namic pressure and searches for enhancements that are 100% - 200% higher than that
value. (Archer & Horbury, 2013; Gunell et al., 2014; Karlsson et al., 2015; Gutynska et
al., 2015). Another way is to apply a minimum threshold to the x component of the dy-
The dynamic pressure enhancements can reach up to \( \sim 15 \) times of the background value. Their duration can be of the order of seconds, up to several minutes with an average of 30 seconds (Archer & Horbury, 2013). Parallel to the flow, the scale is \( \sim 0.5 R_E \) and in the perpendicular direction slightly more at roughly \( \sim 1 R_E \) (Archer & Horbury, 2013; Plaschke et al., 2018). While as mentioned above, jets' dynamic pressure enhancement is usually attributed to both density and velocity increase (Amata et al., 2011; Archer & Horbury, 2013), there are cases where some jets exhibit a density decrease. Specifically, Plaschke et al. (2013), found 10.5% of jets showing a density decrease. On the other hand, Archer et al. (2012) using a different jet criterion found up to 18% of jets exhibiting a density drop. Furthermore, jets can generate a vortical motion in the background magnetosheath plasma, causing a deceleration to the ambient plasma around the jet (Plaschke & Hietala, 2018). It has been recently shown that jets occur roughly 9 times more often downstream of the quasi-parallel bow shock compared to the quasi-perpendicular one (Vuorinen et al., 2019). This is in agreement with the observations showing low solar wind cone angles favoring the formation of subsolar magnetosheath jets, while other solar wind parameter variations have no significant effect (Plaschke et al., 2013).

Magnetosheath jets may have an important impact on the magnetosphere. Their increased momentum can create local deformation of the magnetopause and trigger local magnetic reconnection (Hietala et al., 2018), drive compressional waves (Plaschke & Glassmeier, 2011) or even cause direct plasma penetration in the magnetosphere (Karlsson et al., 2012; Dmitriev & Suvorova, 2015). Furthermore, they can affect the radiation belts through the loss of outer belt electrons, (Turner et al., 2012; Xiang et al., 2016). Additionally, jets can cause aurora brightening through the compression of the magnetosphere (Wang et al., 2018) or can affect the aurora via the mechanism of "dayside throat aurora" which has been connected to magnetosheath particle precipitation (Han et al., 2017). The link between jets and energy transfer through the magnetosphere was also observed recently when surface eigenmodes were found to be excited through a collision between a jet and the magnetopause (Archer et al., 2019). Finally, jets seem to be a universal phenomenon that is speculated to occur in other planetary and astrophysical bow shocks (Giacalone & Jokipii, 2007; Plaschke et al., 2018).

## 1.1 Generation of jets

While the generation of jets is not yet fully explained, a prominent theory is that the majority of the jets are associated with ripples of the quasi-parallel bow shock. Hietala et al. (2009) and Hietala and Plaschke (2013) propose that through the interaction with a locally curved bow shock, plasma flows are less decelerated while still being compressed. This results in a relative velocity difference compared to the surrounding flow that gets more decelerated, explaining the dynamic pressure enhancement ("jet") observed in the magnetosheath region. A similar mechanism, where foreshock short large-amplitude magnetic structures (SLAMS) interact with the local bow shock ripples may be responsible for generating some jets. SLAMS (upstream pulsations) are typical phenomena in the quasi-parallel foreshock and have very large magnetic field amplitudes (\( \sim 5 \) times higher than the background) (Schwartz et al., 1992). Regarding jets, it has been suggested that jets associated with SLAMS can have a relative increase of density and magnetic field strength whereas the ones associated with purely bow shock ripple mechanism may be mainly velocity driven (Karlsson et al., 2015). Furthermore, there have been recent simulations supporting the generation of a SLAMS-like subset of jets (Palmroth et al., 2018).
Another theory associates the formation of jet-like transient phenomena with IMF rotational discontinuities. Early simulations have shown that pressure pulses may be generated when there is a switch between quasi-perpendicular and quasi-parallel bow shock or vice versa (Lin et al., 1996). Later, Dmitriev and Suvorova (2012) reported evidence of a jet, generated by a rotational discontinuity. Archer et al. (2012) found several jets that were consistent with this picture by using upstream and downstream solar wind data while Karlsson et al. (2018) investigated the anatomy of some typical cases that exhibit a magnetic field rotation in the magnetosheath.

Additional mechanisms have been suggested, involving solar wind discontinuity-related hot flow anomalies (HFAs) which can act as an obstacle to the upstream solar wind flow (Savin et al., 2012). Another possible mechanism relates jets to the spontaneous hot flow anomalies (SHFAs) resulting from foreshock cavitons (Zhang et al., 2013; Omidi et al., 2013). Retinò et al. (2007), connected magnetic reconnection inside the magnetosheath with local particle acceleration which could appear as jets. This mechanism, however, is not sufficient to explain jets with velocities much greater than the local Alfvén speed (Archer et al., 2012). Other proposed mechanisms describe the jet phenomenon in terms of a slingshot effect (Chen et al., 1993; Lavraud et al., 2007). This effect attributes the velocity enhancement of jets to a release of magnetic tension of a flux tube along the flanks.

There is no consensus regarding which of the above theories is responsible for the origin of jets. Furthermore, there has been no investigation regarding statistical differences that may arise in the properties of the jets depending on the angle between the IMF field and the bow shock normal vector. In this work, we address both of these knowledge gaps by defining different classes of jets and investigating their statistical properties to give insight into how likely each generation mechanism is for each class.

1.2 Different Types of Jets

Using MMS data we identify and classify the jets into 4 main categories. Jets have been observed for over 20 years now downstream of the quasi-parallel bow shock (Němeček et al., 1998). It is believed that the majority of jets are occurring in a quasi-parallel configuration and therefore the first category we search for are the "Quasi-parallel (Qpar) jets". As a complementary category, we are investigating cases of jets that are downstream of the quasi-perpendicular bow shock that we call "Quasi-perpendicular (Qperp) jets". Furthermore, we classified jets that are found at the boundary between a Qpar and a Qperp geometry or vice versa. Our goal is to investigate if these jets are connected to the mechanism proposed by Archer et al. (2012), and we call them "Boundary jets". It has been hypothesized that maybe these jets are different than the other classes and may hold separate properties (Archer et al., 2012; Archer & Horbury, 2013; Karlsson et al., 2018). Finally, after inspecting the derived dataset, we introduce a category called "Encapsulated jets". These jets contain plasma with very similar characteristics to Qpar, while the surrounding plasma is of Qperp nature.

Apart from the main categories, in the jet database, we include 2 more classes. The first are the ones that were identified as jets but were not classified by the algorithm by not fulfilling all necessary criteria. These jets, therefore, remain as ‘Unclassified jets’ until further inspection. Secondly, jets found very close to either the bow shock or the magnetopause (‘Border jets’) are not investigated in this work to exclude possible edge effects. The main goal of this work is to investigate the statistical properties and the differences between these classes. As a result, the goal of the classification procedure is to derive enough samples to provide meaningful comparison and not to provide a class for every observed event. This was done in order to minimize misclassification and to only have very clear cases for each class.
2 Data

In this study, we use data starting from the 1st of September 2015 until the 1st of May 2019. For the measurements that characterize the jets in the magnetosheath, we use data from the MMS (Magnetospheric Multiscale) mission (Burch et al., 2016), while for the upstream values of the solar wind we use data primarily from the ACE (Advanced Composition Explorer) mission (Stone et al., 1998a). The measurements used for both solar wind and magnetosheath regions are presented in Geocentric Solar Ecliptic (GSE) coordinates.

2.1 MMS - Magnetosheath Data

For magnetic field measurements, we use the fluxgate magnetometer (FGM) (Russell et al., 2016) which has a resolution of 1/0.125 sample/sec in the slow survey mode. Furthermore, we use the fast plasma investigation (FPI) (Pollock et al., 2016) which has a time resolution of 4.5 seconds for ion measurements. Finally, for determining the position of MMS, the Magnetic Ephemeris Coordinates (MEC) data that are included in the MMS dataset are used (Burch et al., 2016).

During their orbit, the MMS spacecraft are regularly traversing the magnetosheath region. The small separation of the four MMS spacecraft allows us to only use data from MMS1 for the purposes of this paper.

2.2 OMNIweb/ACE - Solar Wind Data

For parts of the analysis, we use upstream solar wind measurements, publicly available through the 1-minute resolution OMNI database. This dataset is created using multiple spacecraft measurements (primarily ACE & Wind (Stone et al., 1998b)) and is smoothed and time-shifted to the nose of the Earth’s bow shock. The bow shock location changes according to the solar wind parameters and is automatically adjusted for every time-shifted measurement (King & Papitashvili, 2005). The time resolution of the OMNIweb high-resolution database is 1 data point per minute. To associate OMNIweb data to the jets we took average solar wind values of a 15-minute window, starting 10 minutes before the jet’s observation time and up to 5 minutes after. This value seemed to provide accurate results in the cases that we tested manually, and was done to compensate for several possible errors that are explicitly analyzed in the method section below. As a result, every jet that has been measured by MMS in the magnetosheath is associated to average solar wind quantities from the OMNIweb database.

3 Method

3.1 Magnetosheath Identification

The determination of each region (magnetosheath/solar wind/magnetosphere) is done based on manually derived thresholds for ion number density ($n_i$), velocity ($V_i$), temperature ($T_i$), and differential energy flux of high-energy ions ($F_i$). Furthermore, we require three (3) sequential data points to be classified as a different region in order to change the region’s characterization (e.g. transitioning from the magnetosheath to the solar wind). This was done to avoid cases where due to the variance of the measurements, one point might be misclassified as another region. Finally, we impose a minimum duration for each region to be 15 minutes. Smaller regions were considered to be possibly influenced by bow shock or magnetopause crossings.
Table 1. Initial dataset of the magnetosheath jets for the period 10/2015 - 04/2019.

<table>
<thead>
<tr>
<th>Subset</th>
<th>Number (n)</th>
<th>Percentage (%)</th>
<th>Criteria</th>
</tr>
</thead>
<tbody>
<tr>
<td>All</td>
<td>16034</td>
<td>100</td>
<td>Eq. (1)</td>
</tr>
<tr>
<td>Combined</td>
<td>8499</td>
<td>53</td>
<td>Eqs. (1), (3)</td>
</tr>
</tbody>
</table>

3.2 Jet Determination

For jet determination, we rely only on local magnetosheath data. Doing so, we increase the dataset sample size by not limiting observations to time periods where upstream solar wind data are available. We found that roughly $\sim 27\%$ of the jets contained missing data in their corresponding solar wind dynamic pressure. As a result, the choice of local MMS measurements for jet determination appears to be superior regarding the size of the derived dataset.

For the initial dataset, we impose a minimum relative dynamic pressure threshold, which defines a jet as the time interval in which the dynamic pressure is at least twice as large as a 20-min average value. Specifically, we use:

$$P_{msh} \geq 2\langle P_{msh} \rangle_{20\text{ min}}$$ (1)

where,

$$P_{msh} = m_p n_i V_i^2$$ (2)

and angular brackets denote an averaging by a 20 min sliding window. When magnetosheath regions are less than 20 minutes, the average window is taken to be equal to the available region. The choice of this criterion was primarily done to compare with other statistical works done with a similar criterion (e.g. (Archer et al., 2012)). Furthermore, criteria using solar wind values were avoided since the presented work contains jets occurring at the flanks of the magnetosheath, and such criteria would be met all the time.

We then implement an additional criterion, combining all the jets that have a shorter time separation than 60 seconds from each other.

$$t_{start,i+1} - t_{end,i} \geq 60\text{s}$$ (3)

Where $i = 1, 2, 3...n$ is the number of the jet in the database.

This was done based on the assumption that jets with such a small time separation are part of the same fast plasma flow. A similar technique is also applied when studying flows that occur in the plasma sheet, known as bursty bulk flows (BBFs) (Angelopoulos et al., 1994). Furthermore, not combining jets may lead to skewed statistics since it can result in an artificially increased number of jets with much shorter duration and similar properties, possibly causing misleading results.

After obtaining the jet dataset, as shown in Table 1, we implement an automatic classification algorithm to create a subset of jets for each class. The algorithm includes 5 stages of classification that are implemented sequentially. The purpose of this method is to increase the number of jets that are classified after every stage while only slightly increasing the misclassification cases. In the following subsections, we will briefly explain
Table 2. Properties of the four main classes of jets.

<table>
<thead>
<tr>
<th>Name</th>
<th>Characteristics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Quasi-parallel</td>
<td>High energy ion flux, low ion temperature anisotropy, high magnetic field variance</td>
</tr>
<tr>
<td>Quasi-perpendicular</td>
<td>Low energy ion flux, high ion temperature anisotropy, low magnetic field variance</td>
</tr>
<tr>
<td>Boundary</td>
<td>Switch between Qpar characteristics to Qperp or Vice Versa</td>
</tr>
<tr>
<td>Encapsulated</td>
<td>Switch from Qperp characteristics to Qpar and back to Qperp</td>
</tr>
</tbody>
</table>

some key ideas and components of the algorithm, while more details can be found in Appendix A, Appendix B and in the supplementary material.

3.3 Jet Classification

For the jet classification, we only use MMS data. Similar to the jet determination algorithm, the classification code avoids the use of solar wind measurements. This was done for several reasons. The solar wind values available are measured at \( L_1 \) and are time-lagged, introducing an error from the artificial propagation to the bow shock nose. The generated error in such a time-lagging procedure can reach values up to 30 minutes (Mailyan et al., 2008; Case & Wild, 2012), while producing large uncertainty in short time scale phenomena (e.g. rotations of magnetic field). Furthermore, the available measurements are averaged to 1 minute, which makes certain short time scale features impossible to detect. Additionally, the jets are identified throughout the whole magnetosheath region, meaning that one has to time-shift the associated solar wind values after the bow shock interaction, differently for each jet, in order to accurately characterize the jets, providing additional uncertainty to the measurements. Finally, for roughly 1/4 of the jets IMF measurements were not available for a sufficiently long period of time to accurately classify them. All the above reasons led us to primarily use magnetosheath data rather than solar wind for the classification.

It has been shown that the quasi-parallel (Qpar) magnetosheath has different properties than the quasi-perpendicular (Qperp) magnetosheath. Specifically, in Qpar magnetosheath, temperature anisotropy is typically different compared to the Qperp one (Anderson et al., 1994; Fuselier et al., 1994). Furthermore, stronger fluctuations in the plasma density, velocity, and the magnetic field have been associated with Qpar magnetosheath (Formisano & Hedgecock, 1973; Luhmann et al., 1986). Finally, the most striking difference is a distinct high energy ion population that can be observed in the Qpar magnetosheath (Gosling et al., 1978; Fuselier, 2013). Therefore, the classification code works by applying manually derived thresholds to the ion energy flux, temperature anisotropy and, magnetic field standard deviation. The quantities used for the classification are discussed later, while the values for each threshold are provided in Appendix A.

The characteristics of the 4 main classes of jets are summarized in Table 2.

In order to verify that we can accurately distinguish between Qpar and Qperp magnetosheath, we checked the measurements of MMS when it was close to the subsolar point of the bow shock. Due to the proximity to the subsolar point, there is a smaller error in the propagation of the solar wind measurements to the bow shock, and a shorter distance for the plasma flow to propagate inside the magnetosheath. Therefore, we can confirm the expected characteristics of the magnetosheath plasma. An example of such a test can be seen in Figure 1. The cone angle is defined as:

\[
\theta_{cone} = \arccos \left( \frac{|B_x|}{|B|} \right)
\]
which in the case of subsolar point it is identical to $\theta_{Bn}$ since the bow shock normal vector $\hat{n}$ is pointing in the x direction.

As shown in Figure 1, there are distinct magnetosheath characteristics associated with the quasi-parallel and quasi-perpendicular bow shock. The high energy ion flux is the one that is most noticeable, while the ion temperature anisotropy, and the magnetic field variance are also correlated with the change of the cone angle. The exact computation of these quantities can be found in Appendix A. Interestingly, the region which is not shaded with any color is a typical example where the high resolution measurements of MMS provide evidence of a short-time scale change of IMF while the cone angle measurements of 1-min resolution fully miss the rapid change that is seen in the magnetosheath. The purpose of this example is to verify that the classification of jets into Qpar and Qperp can be performed using only local MMS measurements by comparing with a proxy for $\theta_{Bn}$. MMS1 is located at $(11.37, -0.02, -1.01)R_E$ in GSE coordinates. This position was chosen to be close to the subsolar region. This was done to minimize the difference between $\theta_{cone}$ and $\theta_{Bn}$ while limiting the time-shift effect from the bow shock to MMS position.

**Figure 1.** Visualization of associated changes between Qpar and Qperp magnetosheath. From top to bottom, ion energy spectrogram, solar wind cone angle, very high energy ($16 \rightarrow 28$ keV) averaged differential ion flux, high energy ($7 \rightarrow 12$ keV) averaged differential ion flux, ion temperature anisotropy, and sum of the magnetic field standard deviation. Blue shaded region represent Qpar regions while red show Qperp ones. More information about the computation of each quantity can be found in Appendix A.
Typical examples of each jet class can be seen in Figure 2. In Figure 2(a), we show a quasi-parallel jet whereas in Figure 2(b) a quasi-perpendicular one. A boundary jet can be seen in Figure 2(c) and finally an encapsulated one in Figure 2(d).

3.3.1 Pre-jet and Post-jet Periods

The classification scheme is based on the assumption that there are three distinct phases in the jet phenomenon. Since the jet crosses MMS, observations include the plasma environment propagating in front of the jet, the jet flow and the plasma behind the jet. These plasma environments are called, pre-jet, jet and post-jet periods, respectively.

The jet period is the duration in which the criterion of Eq. (1) is satisfied. In the case that the jet contains only one data point (~30%), we re-adjust the starting and ending point of the jet to include one extra data point before and after the jet respectively. The pre-jet period is a period of time before the actual jet which is usually characterized by a gradual increase in dynamic pressure. The post-jet period is an equally long period of time, characterized by a gradual drop of dynamic pressure associated with a non-jet magnetosheath region.

The pre/post-jet time periods are set based on jet duration as:

\[
\Delta t_{\text{pre,post}} = \begin{cases} 
45 \text{ sec}, & \Delta t_{\text{jet}} < 45 \text{ sec} \\
60 \text{ sec}, & 45 \text{ sec} \leq \Delta t_{\text{jet}} < 75 \text{ sec} \\
75 \text{ sec}, & \Delta t_{\text{jet}} \geq 75 \text{ sec}.
\end{cases}
\] (5)

It was decided to have the pre/post jet time increasing with jet duration mainly to assist the classification routine which is categorizing data points and chooses the class of each jet based on the percentage of them that fit the classification criteria. Furthermore, by manually inspecting cases of extensive duration jets (\(\Delta t_{\text{jet}} > 45 \text{ sec}\)) we found that a slight increase to their pre/post jet times made the classification algorithm more accurate.

3.3.2 Verification and Validation of Data Set

In order to determine the settings for the classification scheme, a test data set was created through visual inspection, containing jets of every class. After testing the accuracy of our classification procedure the best stage from which the output was sufficient to derive statistical results was chosen (Appendix B).

As a final validation, a visual inspection accompanied by a manual reclassification was made for a few misclassifications that the automatic procedure produced (~10–20%). This resulted in some slight changes to the dataset while ensuring that the accuracy of the classification is satisfactory. Typically, the majority of automatic misclassifications were found in the boundary and encapsulated cases. This was expected since these classes had much more precise criteria to be met both in the jet and in the surrounding plasma region. More information regarding the verification of the data set and the accuracy determination of the procedure can be found in Appendix B and in the supplementary material.

The number of jets in the final classified dataset is shown in Table 3.

The position for all the main class jets is shown in Figure 3. There, the MMS position at the time of observation of the maximum dynamic pressure is shown. The magnetopause and bow shock regions are plotted based on the model found in Chao et al. (2002) and by using the average solar wind conditions that were found for all the jets in the dataset. In particular, the model used here and below uses the following quan-
Table 3. Classified dataset of the magnetosheath jets for the period 09/2015 - 04/2019. Using as initial dataset the combined \((N = 8499)\) jets of Table 1. The properties of each class are shown in Table 2.

<table>
<thead>
<tr>
<th>Subset</th>
<th>Number</th>
<th>Percentage (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Quasi-parallel</td>
<td>2284</td>
<td>26.9</td>
</tr>
<tr>
<td>Final cases</td>
<td>860</td>
<td>10.1</td>
</tr>
<tr>
<td>Quasi-perpendicular</td>
<td>504</td>
<td>5.9</td>
</tr>
<tr>
<td>Final cases</td>
<td>211</td>
<td>2.5</td>
</tr>
<tr>
<td>Boundary</td>
<td>744</td>
<td>8.8</td>
</tr>
<tr>
<td>Final cases</td>
<td>154</td>
<td>1.8</td>
</tr>
<tr>
<td>Encapsulated</td>
<td>77</td>
<td>0.9</td>
</tr>
<tr>
<td>Final cases</td>
<td>57</td>
<td>0.7</td>
</tr>
<tr>
<td>Other</td>
<td>4890</td>
<td>57.5</td>
</tr>
<tr>
<td>Unclassified/Uncertain</td>
<td>3499</td>
<td>41.2</td>
</tr>
<tr>
<td>Border</td>
<td>1346</td>
<td>15.8</td>
</tr>
<tr>
<td>Data Gap</td>
<td>45</td>
<td>0.5</td>
</tr>
</tbody>
</table>

For the magnetopause model, the model uses the z-component of the interplanetary magnetic field \((B_z)\) and the ion dynamic pressure \((P_{\text{dyn}})\). In addition, the bow shock model also uses the magnetosonic Mach number \(\mathcal{M}_m\) and the beta plasma parameter \((\beta)\). For the average model shown in Figure 3, the conditions used are, \(B_z = -0.075\ \text{nT},\ P_{\text{dyn}} = 2.07\ \text{nPa},\ \mathcal{M}_m = 5.97\) and \(\beta = 2.45\).

### 3.4 Derived quantities

In order to derive statistical results for each of the classes, the "final cases" listed in Table 3 are used. These jets met all necessary criteria from the automatic procedure and have also been manually verified. As a result, unless explicitly mentioned, we use the verified ("final") cases for our analysis. Finally, when we are referring to "main" classes we mean the four classes described in Table 2. More information regarding the criteria and the exact determination of these cases are given in the appendices (Appendix A and Appendix B) of this article and in the supplementary material.

For all the jets, different variations of the minimum, mean and maximum values of their properties are investigated. Most importantly, an analysis on how these quantities are distributed compared to the background magnetosheath plasma is being done. This analysis is conducted by introducing "difference" values, referring to quantities that are either minimum, mean, or maximum within a jet from which a 5-minute background magnetosheath value is subtracted.

\[
\Delta X_{\text{max/mean/min, 5}} = X_{\text{max/mean/min}} - \langle X \rangle_{\text{MSH}}.
\]  
\[
\langle X \rangle_{\text{MSH}} = \frac{1}{2n} \sum_{i}^{n} (X_{\text{start} - i} + X_{\text{end} + i})
\]  

where start/end is the starting and ending point of the jet period, and \(n = 33\) measurements.
Figure 2. Examples of the four main categories of jets. (a): Quasi-parallel, (b): Quasi-perpendicular, (c): Boundary, and (d): Encapsulated jet. From top to bottom, in each subplot: dynamic pressure, ratio of the dynamic pressure to the background level, ion velocity, ion number density, magnetic field components averaged with a moving window of 18 seconds, ion energy spectrum and parallel and perpendicular components of ion temperature. The red vertical line shows the time of maximum dynamic pressure, blue vertical lines the jet period, and green vertical lines indicate the pre-jet and post-jet times. Finally, the black dotted line on the second panel of every subplot indicates a 200% enhancement of dynamic pressure compared to the background.
Figure 3. Location of the 4 magnetosheath jet classes projected to the $xy$-plane in GSE coordinates, identified in MMS data between May 2015 and May 2019. The green and black dashed lines mark the approximate location of the magnetopause and the bow shock during solar wind conditions averaged over the periods that a jet was found. Coordinate system is the Geocentric Solar Ecliptic (GSE) and both axes are normalized to Earth radius ($R_E = 6.371 \, \text{km}$).

The differences between the mean and max values were, statistically speaking, insignificant due to the short duration of the jets. Therefore, in order to make the visualization easier, the maximum values are primarily shown. It should be noted that the "difference" values (Eq. (6)) can give insight in the cases of Qpar and Qperp jets but should be treated with caution when referring to the boundary and encapsulated jets. The reason is that the background normalization in the first two cases is being done with plasma which is more or less similar throughout the 5 minute period that was taken. On the other hand, for the boundary and encapsulated cases, due to the nature of plasma being different between the jet and the surrounding measurements, the difference values can be unreliable.

To determine the distance of each jet from the bow shock, a model for every jet based on its associated solar wind values was generated. The average associated solar wind conditions are derived from values 10 min before the jet and up to 5 minutes after. The asymmetric usage of measurements before and after the jet was done to compensate for the time plasma takes to travel from the bow shock to the MMS position.
Later, the maximum velocity vector ($V_{\text{max}}$) of each jet was used to propagate it back in time until a bow shock crossing was found. This procedure took $\Delta T_{BS}$, time for each jet ($i$) which was calculated as the number of steps multiplied by the time resolution of the FPI instrument (4.5 seconds). After approximating a point of origin for each jet, the distance from the bow shock is computed as:

$$\Delta X_{BS} = X_{BS} - X_{MMS}$$

where $X$ can be radial distance ($R$), distance along the $yz$ plane ($\rho$), or distance along the $x$ axis ($X$). It should be noted, that the modeled position of the bow shock may have a significant error as shown in several studies (e.g. (Merka et al., 2003; Turc et al., 2013) and therefore any statistical results should be considered with caution.

Furthermore, the algorithm which computed the point of origin for each jet, assumes that no breaking nor change in the direction of the jet occurred from its creation until its observation by MMS. This assumption is certainly not ideal and it produced some cases where the jet was found to originate from a non-physical origin (e.g. $\Delta R > 30 R_E$). In these cases, we used the dominant component of the velocity to propagate the jet to the bow shock as an alternative option. However, there were cases that still provided unphysical results. An algorithm identified these cases by checking whether the origin was extremely far away from the position the jet was found or if the time it took a jet to reach the bow shock was more than 30 minutes. In these cases, we simply removed the jet from this specific analysis. This procedure reduced the number of jets in all classes slightly. Specifically, 4 Qpar, 2 Qperp, 2 boundary, and 1 encapsulated jets were removed.

Similarly, a magnetopause model was generated using the model by Chao et al. (2002) and the solar wind conditions at the time of each jet observation. The magnetopause model, while also prone to several errors, can provide vital information regarding the relative position of jets of different classes. After, modeling the magnetopause for each jet, the radial distance from the closest point was measured as

$$\Delta R_{MP} = R_{MP} - R_{MMS}$$

where, $R_{MP}$ is the closest point of the magnetopause to the position of MMS $R_{MMS} = (X, Y, Z)$.

Throughout the text, when referring to subsolar jets an extra criterion is applied:

$$|Y_{GSE}| < 2R_E$$
$$|Z_{GSE}| < 2R_E$$

where $|Y_{GSE}|$ and $|Z_{GSE}|$ are the absolute value of the $y$ and $z$ coordinate of the MMS satellite at the time of maximum dynamic pressure of each jet. Applying this criterion generated a smaller subset of jets ($n = 298$). This set is used to investigate relations between distances from the bow shock. We do so because a jet close to a subsolar position with a dominant $x$ velocity component is more likely to have travelled a distance approximately equal to the $x$ distance between MMS and the bow shock.

To investigate the orientation of the flow, we calculate two more quantities. First, we calculate the velocity in the $yz$ plane ($V_\rho$), and then the angle between that velocity and the $x$ axis. The velocity $V_\rho$ is defined as:

$$V_\rho = \sqrt{V_y^2 + V_z^2}$$
while the angle is defined as:

\[ \theta_{V_\rho} = \arctan \left( \frac{V_\rho}{|V_x|} \right). \]  

(12)

An interesting quantity we investigated is the angle between the magnetic field vector before and after the jet. This was done in order to search for any interesting properties that could link a jet class to the pressure pulses connected to rotational discontinuities that were first described by Archer et al. (2012). To calculate the magnetic field angle we took the average of the magnetic field vector for 30 sec, 1 min and 2 min before and after the jet and determined the angle between the “averaged” magnetic field measurements. All the derived quantities provided similar average and median results, although the actual values varied slightly. We have decided to use the 30 sec averaged magnetic field for the computation of the presented magnetic field angle.

\[ \theta_B = \arccos \left( \frac{\langle \mathbf{B} \rangle_{\Delta t_1} \cdot \langle \mathbf{B} \rangle_{\Delta t_2}}{|\langle \mathbf{B} \rangle_{\Delta t_1}| \cdot |\langle \mathbf{B} \rangle_{\Delta t_2}|} \right) \]  

(13)

where \( \Delta t_1 \) is a 30 sec duration before the jet and \( \Delta t_2 \) a 30 sec duration after the jet.

Another quantity that is considered is the angle between the average velocity vector of the jet and the velocity vector of the surrounding plasma. This is computed by taking the average vector of the jet period and finding its angle to the average velocity vector taken 5 minutes before and after the jet. In order to have a velocity that better characterized the background flow of the plasma, we removed 30 seconds before and after the jet when computing the average background velocity vector.

\[ \theta_V = \arccos \left( \frac{\langle \mathbf{V} \rangle_{\Delta t_{\text{jet}}} \cdot \langle \mathbf{V} \rangle_{\Delta t_2}}{|\langle \mathbf{V} \rangle_{\Delta t_{\text{jet}}}| \cdot |\langle \mathbf{V} \rangle_{\Delta t_2}|} \right) \]  

(14)

where, \( \Delta t_{\text{jet}} \) is the jet period and \( \Delta t_2 \) is an 9-minute duration, of 4.5 minutes before \( t_{1,\text{start}} - 30s \) and after \( t_{1,\text{end}} + 30s \).

To investigate the total effect of each jet we calculated the integrated dynamic pressure over the jet’s duration along the flow (total fluence) as:

\[ f_{\text{total}} = \int P_{\text{dyn}} \cdot |\mathbf{V}| \cdot dt = \sum_{i} P_{\text{dyn},i} \cdot |\mathbf{V}_i| \cdot \Delta t \]  

(15)

where, \( n \) is the number of measurements within each jet period and \( \Delta t \) is the time resolution of the FPI instrument (4.5 seconds).

We also present correlation coefficients between a number of jet properties. The most commonly used correlation coefficients are the Pearson’s correlation coefficient (PCC) and Spearman’s rank correlation coefficient (\( \rho_{Sp} \)). The former describes a possible linear relationship between the two variables while the second is showing the strength of a monotonic relation (Myers et al., 2013). For our analysis, we use the Spearman’s coefficient to determine correlations between jets’ quantities.

Throughout the results section, all plots are color-coded the same way. Qpar jets are represented by blue, Qperp by red, boundary by black and encapsulated by orange.
4 Results

The first observation, as shown in Table 3, is that the number of jets found downstream of the quasi-parallel shock is significantly higher than the number found in other classes. Boundary and quasi-perpendicular jets are less frequent and, finally, encapsulated jets occur very rarely. While we cannot derive how frequently each jet occurs for each magnetosheath region (Qpar and Qperp), one can assume that on average the magnetosheath region during MMS orbits is equally distributed between the two regions (S. Petrinec, 2013). With that assumption, we can estimate that quasi-parallel jets occur much more frequently than quasi-perpendicular jets. Specifically, they can occur \( \sim 5 - 10 \) more often, depending on how many of the uncertain jets could be classified as Qpar jets (41.2\% of the detected jets are unclassified, see Table 3). This result is in agreement with recent results showing that the frequency of Qpar jets can be \( \sim 9 \) higher than Qperp jets (Vuorinen et al., 2019).

4.1 Properties of the Jet Classes

In Figures 4 - 10, the basic properties of each class along with the quantities defined in the previous section are shown.

Starting with the basic properties of the jets in Figure 4, quasi-parallel and boundary jets have on average much higher dynamic pressure \((\langle P_{\text{max}}\rangle \sim 3 \text{ nPa})\) compared to the quasi-perpendicular jets \((\sim 0.5 \text{ nPa})\), while encapsulated jets lie somewhere in between. Similar contrast between classes can be observed for the differences in dynamic pressure from the background magnetosheath plasma with or without solar wind normalization. The distributions and the average values of the absolute ion velocity show that the velocities of Qperp jets are much lower than these of Qpar, boundary and encapsulated jets. Interestingly, while this effect holds regardless of the normalization technique, when normalizing to the solar wind, the difference in velocity between classes is reduced. This could mean that on average the velocity of a jet primarily depends on the solar wind velocity at the time of its formation. Furthermore, it shows that the majority of Qperp jets are found under low solar wind velocities. Regarding the ion density, Qpar and boundary jets have on average twice as high density as the Qperp and encapsulated jets. When looking at the difference values however, the actual density gain is an order of magnitude more for the Qpar and boundary cases compared to the other two. Finally, the overall net gain of density and velocity for the jets is much higher for the rest of the classes compared to the Qperp jets.

In general, Figure 4 shows that the properties of Qpar and boundary jets are very similar, while both velocity and density changes in the Qperp jets are much smaller. This could imply differences in their generation mechanisms. Finally, encapsulated jets are dominated by an increase in velocity with absolute velocities gain being even higher than Qpar jets while their density distribution is very similar to Qperp jets.

For all jet classes, there are several jets where the dynamic pressure reaches values even higher than the dynamic pressure of the solar wind as expected from earlier studies (Plaschke et al., 2013). Only one encapsulated jet was found to have a higher velocity than its associated average solar wind velocity, while all other jets had a lower one. We can conclude that the main contribution of the dynamic pressure increase compared to the solar wind is due to the compression that solar wind undergoes after interacting with the bow shock. This, in turn, causes a density increase that can be several times higher in the jets compared to the solar wind.

The average and median jet duration of the main class jets is found to be 39 and 18 seconds respectively. As shown in Figure 5, Qpar and encapsulated jets have a slightly longer duration than boundary jets, while the Qperp jets have a much shorter duration, with the majority consisting of only 1 data point which corresponds to 4.5 seconds. To
Figure 4. Histograms showing distributions, average and median values for the maximum values of the basic jet quantities. Maximum dynamic pressure, absolute velocity and density are shown. First columns show the measured values, the second describe the difference from the background and the third are normalized to the associated solar wind values.

investigate the low duration of Qperp jets, we explored the statistical properties of Qperp jets that contained at least 3 data points (69/211 cases). Doing so, we discovered that their basic properties (Figure 4.) are statistically similar to the whole subset and therefore it was decided that all the jets can be included in the analysis. It should be noted that the duration of encapsulated jets is biased to appear longer by their definition (Table 2), since shorter jets would be classified as Qpar.

In Figure 5, when looking at the dynamic pressure integrated over the jet period (Eq. (15)) we see a consistent picture where the shorter duration along with the lower dynamic pressure make the Qperp jets much weaker in comparison to the rest of the jet classes. On average the rest of the jets seem to be similar while the Qpar and boundary jets, again hold very similar properties. The distance from the bow shock (Eq. (8)) is quite different for each class. While boundary and Qpar have similar relative positions, the Qperp jets are found further inside the magnetosheath. This difference is more vis-
Figure 5. Histograms showing distributions, average and median values for scale sizes and distances, estimated from a point of origin at the bow shock for each jet. $\Delta T_{BS}$ describes the time that was estimated for the jet to arrive to MMS from its origin point at the bow shock.

Figure 6. Showing the distance of the jet from the Earth and the distance from a magnetopause model (Eq. 9). It is shown that while jets of every class are found in similar distances, they are also found at a much higher radial distance ($R$) from the bow shock, again with the $\rho$ component having much higher values than the rest of the classes. It should be noted that Qperp jets are found to occur primarily under low-velocity solar wind conditions. As a result, the bow shock model used for those cases generates a bow shock further away from the Earth than for the cases of Qpar and Boundary jets. Finally, the time that it took each jet to reach the MMS is much different. Qpar and boundary jets need on average $\sim 3$ minutes while the much slower Qperp jets require much more at around $\sim 8$ minutes. Encapsulated jets also take a long time to reach MMS from their origin point ($\sim 7$ min) but in contrast to Qperp jets, this is due to the large distance that they have to cover rather than their velocity.

To analyze the different geometric properties of each class, we also include Figure 6, showing the distance of the jet from the Earth and the distance from a magnetopause model (Eq. 9). It is shown that while jets of every class are found in similar distances
from the Earth (position of MMS), the distance from the magnetopause varies considerably. While Qperp jets are expected to appear closer to the magnetopause from their corresponding distance of the bow shock (Figure 5), it is now clear that they occur so close to the magnetopause that often they appear to be within the magnetosphere due to the inaccuracies of the model in use. It should be stressed that encapsulated jets are not only found close to the magnetopause but they are also found closer to the Earth (Figure 6, right).

Figure 6. Histograms showing distributions, average and median values of the jets’ distance from the magnetopause and from the Earth

Figure 7 shows that the ion temperature profiles are quite different between each class. On average, the temperature is lower on Qperp jets (\(\sim 100\) eV) compared to the rest of the jets (\(\sim 300\) eV). The difference of both \(T_{\perp}\) and \(T_{\parallel}\) compared to the background is negative and very similar between boundary and Qpar jets. On the other hand, it is around zero for Qperp jets and positive for the encapsulated jets. Most of the observed differences are expected due to the nature of the magnetosheath region and from the definition of each class. As mentioned in the previous subsection, encapsulated and boundary jets have a very different background magnetosheath. Therefore, a direct comparison between each class can be misleading, especially in the case of the highly variant temperature measurements.

An interesting difference regarding the mean absolute magnetic field appears in Figure 7. Qpar jets have on average, a smaller mean absolute magnetic field than the rest of the classes (\(\langle |B|_{\text{mean}} \rangle \sim 25\, \text{nT}\)). Encapsulated jets have almost twice as high values while the mean absolute magnetic field of Qperp and boundary jets’ is in between, at \(\langle |B|_{\text{mean}} \rangle \sim 30\, \text{nT}\).

The difference in the mean absolute magnetic field (\(\Delta |B|_{\text{mean}}\)) is higher in Qpar and boundary jets compared to Qperp and encapsulated jets. Specifically, Qpar and bound-
ary jets have a bigger absolute magnetic field than their background magnetosheath. On the other hand, Qperp jets have on average a slightly smaller magnetic field although the actual values range for individual events vary significantly ($\Delta |B|_{mean} \in [-10, 10]$ nT).

Figure 8 shows how plasma (thermal) and magnetic pressures vary between each class along with their ratio ($\beta$ parameter). For all the classes, the maximum plasma pressure is on average higher than the maximum magnetic pressure. However, when looking at the difference values, the Qpar, and the boundary jets have higher maximum magnetic pressure ($\Delta P_{magnetic,max}$) than maximum plasma pressure ($\Delta P_{plasma,max}$). On the other hand, Qperp and encapsulated jets still have a higher maximum thermal pressure difference than maximum magnetic pressure difference. Looking at the maximum magnetic pressure and its difference to the background can also be directly interpreted as a measurement of the maximum absolute magnetic field. This information shows us that although from the previous histograms (Figure 7), the average magnetic field ($|B|_{mean}$) is higher in the case of Qperp jets, the maximum ($|B|_{max}$) values are higher in the Qpar and boundary cases. This could originate from the higher duration of Qpar jets, along
with the higher time resolution of the FGM data compared to the FPI. These two factors can allow very high magnetic field values to occur within a jet period since in principle $|B|$ can have a higher variance in the quasi-parallel environment. The behavior of the $\beta$ parameter is consistent with the previous results. While it is higher for the $\text{Qpar}$ and boundary classes, it is on average smaller than that of the background plasma around the jets. On the other hand, encapsulated and $\text{Qperp}$ jets have on average smaller beta values but still maintain a positive difference when compared to the background.

Specifically, average beta values appear to be closer to unity for the $\text{Qperp}$ and encapsulated cases, while they are on average higher ($\langle \beta_{\text{Qpar}} \rangle \sim 10, \langle \beta_{\text{boundary}} \rangle \sim 6$) for the other classes. When looking at the difference to the background, it appears that $\text{Qpar}$ and boundary jets have a negative beta difference ($\Delta \beta < 0$). This could indicate that magnetic pressure has a larger effect in the jet than in the surrounding magnetosheath plasma.

The velocity components of each class are shown in Figure 9. Here, we present the absolute velocity for the $y$ and $z$ component. This was done because all jets and espe-
Figure 9. Histograms showing distributions, average and median values for each velocity component at $|V|_{\text{max}}$.

Cliquically encapsulated jets had a distribution that produced an average velocity close to zero, in both components, due to equally frequent jets exhibiting a high negative and positive $V_{y,z}$. As a result, providing a histogram without the absolute values would limit the information of each class, and would not contribute to a meaningful comparison.

As expected, almost every jet has a dominating negative (earthward) $x$ component, with the Qperp jets on average having smaller values on every velocity component compared to the other classes. Furthermore, Qperp jets seem to have very similar velocities in all three components which are different from the rest of the classes that tend to have a more significant imbalance between components. An interesting difference can be seen in the encapsulated jets where the dominant component of their velocity is surprisingly $V_y$ and $V_z$. The same effect can be seen when we look at the absolute difference ($|V_{\text{jet}} - V_{\text{MSH}}|$), where the difference to the background seems to be higher for the Qpar and boundary jets than Qperp jets, while encapsulated exhibit values much higher than the rest of the classes.
Finally, in Figure 10, directional information and rotation angles of the magnetic field and the velocity are given. As expected, the $yz$ plane velocity ($V_y$) is much higher for the encapsulated jets compared to the other three classes. This can also be seen when calculating the angle between the jet’s velocity and the $x$ axis (Eq. (12)), in which the Qpar and boundary jets show similar behavior, while Qperp jets have on average a higher angle and encapsulated jets the highest. This picture is consistent when comparing to the background plasma in which Qpar and boundary jets show a net decrease in the angle while Qperp and encapsulated show a net increase. Looking at the magnetic field rotation angle (Eq. (13)), there seems to be a significant difference between the Qperp jets and the other classes. Qperp have on average a very small ($\sim 6^\circ$) difference while the rest of the classes have on average higher values, particularly the Qpar jets. Considering velocity rotation angles (Eq. (14)), Qperp jets exhibit the least changes, although all classes seem to have similar statistical values and distributions.
It should be noted that since both velocity and magnetic field rotation angles describe the changes between the plasma before and after jet, the results are heavily affected by the duration of the jet. Specifically, it is expected that jets with a shorter duration such as Qperp jets would statistically have a smaller angle change since measurements taken are spatially and temporally closer to each other.

4.2 Relation Between Jet Properties

In this subsection, we will report on some observations on correlations between different jet properties. It should be noted that all correlations mentioned were found to have a p-value of less than 0.01, unless stated otherwise. The computation of the p-value was done through the exact permutation distributions of each subset (Edgington, 2011).

There is a moderate correlation between the magnetic field rotation angle ($\theta_B$) and both the maximum dynamic pressure ($P_{\text{max}}$) and the difference of maximum dynamic pressure compared to the background ($\Delta P_{\text{max}}$).

Specifically, regardless of the way we calculated the magnetic field rotation angle, for all jets found in the main classes, we found a moderate correlation using Spearman’s coefficient, $\rho_{\text{Sp,All}} = 0.43 \pm 0.02$. Considering only subsolar jets this correlation was increased, reaching $\rho_{\text{Sp,Subsolar}} = 0.6 \pm 0.05$.

A possible interpretation could be that the jets distort the magnetic field lines that are embedded in the plasma in front of them. On weaker jets such as in the majority of Qperp jets (Figures 4 and 10) this effect would be hardly visible since we see the dynamic pressure being an order of magnitude less compared to the other classes and the magnetic field rotation angle is also close to zero. On the other hand, on jets that on average have a higher velocity and density gain, magnetic field vector seems to be different in the plasma in front and behind the jet. To investigate this possible link, we look at class-specific correlation coefficients. For the classes of Qperp and Qpar jets, it was found that the correlation is almost non-existent ($\rho_{\text{Sp,\perp||}} = 0.1 \pm 0.05$ (p-value $= 0.04$)). As a result, we conclude that the correlation was caused by the different properties of each class causing an artificial correlation that does not necessarily represent a physical property. The above result emphasizes the importance of classifying jets that physically occur in different environments before drawing any strong conclusions.

In Figure 11, a comparison between the density and the velocity squared difference normalized by the total dynamic pressure gain is shown, similar to Figure 3 of Archer and Horbury (2013). Figure 11(a) shows the relative change in density and velocity with measurements taken at the point of maximum dynamic pressure. In Figure 11(b) however, the difference is taken by using the measurements of maximum density, velocity and dynamic pressure for each quantity. As shown in Figure 11, the majority of the jets have a combination of velocity and density increase, contributing to the overall dynamic pressure enhancement. For the Qpar and boundary cases, less than 0.5% jets are purely velocity driven, exhibiting a density decrease compared to the background plasma. On the other hand, Qperp jets can have a decrease in density up to 22% and encapsulated jets up to 68% of the times, making their dynamic pressure to mainly originate from a velocity increase. More information regarding the velocity and density distribution of each class can be found in Table 4. As expected, most of the jets regardless of their class exhibit an increase in both density and velocity when comparing to the background magnetosheath. This result shows that the increased frequency of Qpar and boundary jets can be at least partially attributed to density enhancements taking place, while being insignificant or even absent in the case of Qperp jets. It should be noted that the values in parentheses shown in Table 4 correspond to the same time ($P_{\text{max}}$) and are therefore a better metric for quantifying the cases that exhibit a density decrease. However, the calculation that includes the maximum density and velocity points are also important as they are measured within the jet period as seen by MMS. These values act as
When comparing our results to earlier studies, we find that they are quite similar. In particular, depending on the normalization technique 7 – 11% of the jets exhibit a relative decrease in density with the increase in dynamic pressure being caused by a very high enhancement of absolute velocity. Plaschke et al. (2013) found 10.5% using a different jet criterion, while Archer et al. (2012) using essentially the same criterion as this work found 18%. In the main classes, we find no cases exhibiting a velocity decrease as shown in Figure 11 and Table 4. In order to see if there are any jets showing a velocity decrease, we searched the full jet database ($N = 8499$). The only cases with a velocity decrease were 158 jets from which 151 have been classified as "Border" jets, found too close to either the magnetopause or the bow shock. Therefore, since any calculation averaging over different plasma regions is statistically unreliable, we exclude them. Careful examination on the rest of the 7 cases showed that they were jets that occurred very close to another jet but not close enough to fulfill the criteria of jet combining (Eq. (3)). As a result, we conclude that there are no jets showing a relative velocity decrease at their maximum dynamic pressure measurement.

In Figure 12 we present two different types of cross-plots. In subplots (a) and (c), plots of the difference in maximum density ($\Delta n_{\text{max}}$) against difference in maximum magnetic field ($\Delta |B|_{\text{max}}$) with and without solar wind normalization are shown. This was done in order to test a hypothesis that connects SLAMS to the generation of Qpar jets (Archer et al., 2012; Karlsson et al., 2015) We, therefore, search for some kind of correlation between the density increase and the magnetic field increase since SLAMS have such a correlation (Schwartz & Burgess, 1991; Behlke et al., 2003). In the sub-figures (b) and (d) we similarly investigate the difference of maximum velocity ($\Delta V_{\text{max}}$) against the difference in minimum ion temperature ($\Delta T_{\text{min}}$). This was done to see if a correlation can be found that could support the mechanism proposed by Hietala et al. (2009) that associates jets with ripples of the quasi-parallel bow shock. As discussed and shown in
Table 4. Velocity and density distribution of jets that exhibit a dynamic pressure increase. First values are based on the maximum quantity met within jet’s duration and values in parenthesis are derived from the density and velocity value found at $P_{\text{max}}$.

<table>
<thead>
<tr>
<th>Class</th>
<th>Velocity Decrease (%) $V_{V_{\text{max}}} (V_{P_{\text{max}}})$</th>
<th>Density Decrease (%) $n_{n_{\text{max}}} (n_{P_{\text{max}}})$</th>
</tr>
</thead>
<tbody>
<tr>
<td>All</td>
<td>1.6 (1.8)</td>
<td>6.9 (10.9)</td>
</tr>
<tr>
<td>Main Classes</td>
<td>0 (0)</td>
<td>7.3 (10.8)</td>
</tr>
<tr>
<td>Quasi-Parallel</td>
<td>0 (0)</td>
<td>2.9 (5.23)</td>
</tr>
<tr>
<td>Quasi-Perpendicular</td>
<td>0 (0)</td>
<td>15.6 (22.3)</td>
</tr>
<tr>
<td>Boundary</td>
<td>0 (0)</td>
<td>3.9 (5.2)</td>
</tr>
<tr>
<td>Encapsulated</td>
<td>0 (0)</td>
<td>50.1 (68.4)</td>
</tr>
</tbody>
</table>

earlier studies, it is expected that the background plasma surrounding the ripple-generated jet would be more decelerated and would, in turn, have a higher temperature compared to the jet flow created by passing through a ripple of the bow shock, undergoing less deceleration, and heating (Hietala & Plaschke, 2013; Plaschke et al., 2013).

As shown in Figure 12(a,c), for the quasi-perpendicular jets, there is no significant correlation between the difference in maximum magnetic field ($\Delta B_{\text{max}}$) and the difference in maximum density ($\Delta n_{\text{max}}$). However, in the case of quasi-parallel jets, there is a moderate monotonic relationship between the two quantities. Spearman’s rho value ($\rho_{Sp}$) for the quasi parallel case is $\rho_{Sp,a ||} = 0.57$ and $\rho_{Sp,c ||} = 0.55$, whereas for the quasi-perpendicular jets is $\rho_{Sp,a \perp} = -0.2$ and $\rho_{Sp,c \perp} = -0.27$. For all the jets together, a total correlation of $\rho_{Sp,a} = 0.66$ and $\rho_{Sp,c} = 0.63$ is reached. Indices $a, b, c, d$ refer to the subplots of Figure 12, while the symbols of parallel and perpendicular refer to Qpar and Qperp jets respectively.

These results support the idea that a subset of quasi-parallel jets may originate from a SLAMS interacting with bow-shock ripples as described by Karlsson et al. (2015). Further support of this mechanism is shown when looking back at the general characteristics of each class. In Figure 4 it is shown that $\Delta n_{\text{max}}$ is an order of magnitude higher for the Qpar jets compared to the Qperp. Furthermore, in Figure 7, Qpar jets exhibit on average a positive difference on the average absolute magnetic field compared to the Qperp jets that do not. Maximum magnetic pressure and average $\beta$ values shown in Figure 8 also support SLAMS since Qpar and boundary jets have not only a higher magnetic pressure than Qperp jets, but also a higher value than their surrounding plasma.

It should be noted, however, that the anti-correlation observed for Qperp jets can not be directly explained through any known mechanism. The observed anti-correlation should be treated with caution since it was only found for the "final cases" of Qperp jets (Table 3). When we look at the whole body of Qperp jets the observed correlation disappears.

In Figure 12(b,d) a weak/moderate linear correlation between the difference in minimum temperature ($\Delta T_{\text{min}}$) and the difference in maximum absolute ion velocity ($\Delta V_{\text{max}}$) is shown. Correlation coefficients are found to be $\rho_{Sp,b} = -0.35$ and $\rho_{Sp,d} = -0.5$ when looking at the whole body of the jets. While looking exclusively at Qpar jets, we find $\rho_{Sp,b ||} = -0.28$ and $\rho_{Sp,d ||} = -0.43$. On the other hand, when looking at Qperp jets, we find correlation coefficients of $\rho_{Sp,b \perp} = -0.24$ and $\rho_{Sp,d \perp} = -0.23$.

All main class jets have a small to medium anti-correlation relation between the ion temperature and the velocity difference within the jet period (Figure 12(b,d)). As discussed previously, we can interpret this result as indirect support of a mechanism that
Figure 12. (a): $\Delta n_{\text{max}}$ against $\Delta |B|_{\text{max}}$ normalized over solar wind data. Linear regression lines are shown for visual guidance, for the Qpar (blue) and Qperp (red) cases. (b): $\Delta V_{\text{max}}$ against $\Delta T_{\text{min}}$ normalized over solar wind data. (c): $\Delta n_{\text{max}}$ against $\Delta |B|_{\text{max}}$. Linear regression lines are shown for visual guidance, for the Qpar (blue) and Qperp (red) cases. (d): $\Delta V_{\text{max}}$ against $\Delta T_{\text{min}}$. In all figures every point represents a jet while the color shows its class.

is based on the bow shock ripple idea (Hietala et al., 2009; Hietala & Plaschke, 2013). This result is also supported by the general properties shown in Figure 7, where for Qpar jets there is a larger difference between the temperature of the background magnetosheath plasma and the jet. Finally, it has been recently found that similar ripples can be found also at the quasi-perpendicular bow shock which could mean that the generation mechanism of these jets is of the same nature (Johlander et al., 2016). Although the majority of the jets seem to have a medium anti-correlation that could support Hietala’s mechanism (Hietala et al., 2009; Hietala & Plaschke, 2013), we cannot say the same for the quasi-perpendicular where the anti-correlation is weaker. It should be noted, however, that due to the very small duration of the jets, there is usually only one measurement for the temperature and the velocity. Therefore, there is a higher uncertainty regarding this result compared to the other classes.
Finally, based on the differences between thermal and magnetic pressure shown in Figure 8, we investigate possible relationships with other jet properties.

Regarding the difference in maximum magnetic pressure, there is a moderate to strong correlation with the total integrated dynamic pressure \( \rho_{Sp,All} \approx 0.72 \). This result could be interpreted in terms of SLAMS similarly to the analysis of Figure 12 since to calculate the total dynamic pressure we include the ion density \((n)\). However, it was found that all the factors of Eq. (15) are correlated to the maximum magnetic pressure \( P_{mag,max} \), including the difference in maximum absolute velocity \( \Delta V_{max} \) which had a correlation coefficient of \( \rho_{Sp,All} = 0.59 \) and the duration which had a correlation of \( \rho_{Sp,All} = 0.62 \). This result is unexpected and can be considered an indication that magnetic forces play a more important role than previously thought. Qpar jets have similar correlations, while Qperp jets are also alike, apart from the same anti-correlation shown in Figure 12, regarding the density difference and \( \Delta |B| \). It should be noted that this effect appears on all the jets and not only in the Boundary jets as initially speculated.

However, when looking at each class exclusively, the results show that the effect decreases significantly for the duration and velocity for both Qpar and Qperp jets \( \rho_{Sp} \sim 0.2 \). The correlation (when taking all classes together) seems to have been artificially created because in jets with higher velocities and duration it is relatively easier to measure the magnetic field in higher values. This is made possible by the fact that longer duration jets could in principle allow more measurements of the magnetic field to occur and due to the variance of the FGM measurements, reach a higher peak. This, in turn, creates a non-physical correlation between the maximum magnetic field measurement found within a jet and its duration. The only effect that seems to be robust and even enhanced when taking average quantities is the correlation between the density difference \( \Delta n_{mean,max} \) and the absolute magnetic field difference \( \Delta |B|_{mean,max} \). Specifically, Qpar jets have a positive correlation in all four possible combinations of the absolute magnetic field and ion density quantities. The four combinations result when taking the average and maximum density and test their correlation with the average and maximum absolute magnetic field. Looking at these pairs, it as found that Qpar maintain a positive correlation coefficient, \( \rho_{Sp||} \in [0.3,0.6] \). Similarly, the anti-correlation of the Qperp jets remains in all cases, \( \rho_{Sp,\perp} \in [-0.28,-0.65] \). Once more, we should point out that the correlation found in the Qpar jets remains high even when looking at all the Qpar jets rather than the 'final cases' (Table 3). On the other hand, the observed anti-correlation is considerably smaller for the Qperp jets.

From this result, we conclude that the magnetic field seems to play an important role in forming the density profile of each class, possibly explained through SLAMS mechanism. The correlation found on other jets’ properties although less consistent, could still indicate that magnetic fields could have a more important role regarding the velocity and duration of each jet.

An interesting difference was also found when investigating the difference in both the maximum and the average thermal plasma pressure difference \( \Delta P_{th,mean,max} \).

Qpar jets when investigated with the maximum differences in density and thermal pressure have a moderate correlation \( \rho_{Sp,||} = 0.36 \). However, when we take average values for density or thermal pressure, this correlation disappears fully. On the other hand, as discussed previously, density changes are heavily correlated with the magnetic pressure of the Qpar jets. This result shows that the changes in temperature are more important than the changes in density in deriving the thermal pressure difference. On the other hand, Qperp jets have a high correlation of density change and thermal pressure \( \rho_{Sp,\perp} = [0.5,0.7] \). This indicates that the contribution of density change in thermal pressure difference is more important than the temperature difference for the Qperp jets.
5 Discussion and Conclusion

We have investigated the properties of an extensive dataset of magnetosheath jets \((N = 8499)\) using MMS and classified them in different categories based on local magnetosheath measurements. The characteristics of the different classes correspond to plasma originating from the different values of the angle \((\theta_{Bn})\) between the IMF and the bow shock’s normal vector. The general properties found were in agreement with earlier studies. In particular, our dataset contains jets with an average duration of \(\sim 30\) seconds, similar to what has been reported in other studies (Němeček et al., 1998; Savin et al., 2012; Archer & Horbury, 2013; Plaschke et al., 2013). Their dynamic pressure enhancement was found to be in most cases due to both velocity and density enhancement (Amata et al., 2011; Archer & Horbury, 2013; Plaschke et al., 2013; Karlsson et al., 2015). There was no clear case exhibiting a velocity decrease compared to the background magnetosheath, while for all the jets, velocity appears to always be smaller than the associated solar wind measurements. Finally, on average, most of the jets that can be appropriately normalized, have a lower temperature compared to their background. This is in principle expected for a flow that has been less heated and decelerated from the bow shock interaction as shown in previous studies (Savin et al., 2008; Amata et al., 2011; Hietala et al., 2012; Archer et al., 2012; Plaschke et al., 2013, 2018). We have additionally made a number of new observations that are discussed in the following subsections.

5.1 Quasi-Parallel and Quasi-Perpendicular Jets

The results of this study show that quasi-parallel jets are considerably more frequent than quasi-perpendicular jets. Specifically, similar to recent results (Vuorinen et al., 2019), they were found to occur \(\sim 5-10\) times more frequently than quasi-perpendicular jets. On average they have a dynamic pressure around 3.5 nPa, with the majority of them exhibiting both a density and a velocity increase. Their density increase shows a significant correlation with the absolute magnetic field increase \((\rho_{Sp} = 0.5 \pm 0.2)\) indicating a possible association of at least a subset of them to SLAMS. A moderate anti-correlation was found between the maximum velocity difference \((\Delta V_{max})\) and the minimum temperature difference \((\Delta T_{min})\). This could be interpreted as a relatively weak support of the bow shock ripple mechanism. Furthermore, the high magnetic field values and variance found could indicate possible wave activity that may contribute to their properties. Finally, most of the quasi-parallel jets are earthward with very high velocities, making them very interesting candidates to investigate phenomena such as jet-triggered magnetopause reconnection or other magnetosphere coupling phenomena.

Quasi-perpendicular jets have a much smaller dynamic pressure than the rest of the classes and their dynamic pressure is mainly due to a velocity increase rather than a density enhancement. Their duration is significantly smaller (median: 4.5 seconds per jet) and their total integrated dynamic pressure is more than an order of magnitude lower than the corresponding values of the other jet types. While their existence is clear according to the criterion used, their importance regarding magnetospheric influence is to be questioned.

Their properties, when compared to Qpar jets, suggest that either a different mechanism or a smaller scale version of Qpar generation mechanism causes their generation. The density differences can be in principle, attributed to the absence of SLAMS that are believed to occur only in the ion foreshock generated under quasi-parallel bow shock. On the other hand, we hypothesize that their low velocities compared to the other classes could be the result of one or more of the following effects. The jet criterion used (Eq. (1)) is fulfilled more easily during low dynamic pressure conditions compared to high dynamic pressure ones. As a result, there might be an observational bias causing MMS to observe primarily jets that occur under low-velocity solar wind conditions. Secondly, there might be a link between the actual solar wind conditions and the IMF orientation, in
which slower solar wind flow could be attributed to IMF conditions where $B_y$ and $B_z$
components are more dominant. Finally, assuming that ripples in the quasi-perpendicular
bow shock (Johlander et al., 2016) are related to the jets generation mechanism, maybe
the smaller amplitude and scales of these ripples can affect the jet properties. Specifi-
cally, the smaller amplitude of Qperp ripples can create a geometry in which the Qperp
jet undergoes a larger breaking compared to the case of the sharper (more inclined) tran-
sitions of the ripples associated with Qpar jets. The different scales could also contribute
to the short duration of the Qperp jets. The smaller scale ripples would benefit the for-
mation of smaller flow structure than larger ones regarding their tangential size. In turn,
when these flows meet MMS under some random angle, their measured duration would
be significantly smaller.

To investigate the possibility of an observational bias, we examine the distributions
of the solar wind velocities associated with and without jets. We find that indeed, on av-
erage the associated solar wind velocities are much higher for the quasi-parallel jets ($\langle V_{SW,||} \rangle \approx 495\ km/s$) than for the quasi-perpendicular jets ($\langle V_{SW,\perp} \rangle \approx 400\ km/s$). The stan-
dard deviations were found to be $\sigma_{||,Jets} = 96\ km/s$ and $\sigma_{\perp,Jets} = 46\ km/s$ re-
tpectively. To calculate the total solar wind distribution, we used eleven months containing
long periods of magnetosheath and jet observations and calculated the average velo-
city. These months are: 10–12/2015 - 1, 2, 11, 12/2016 - 1, 2, 12/2017 and 1/2019, and
contained 87% of the jets. The separation between quasi-parallel and quasi-perpendicular
was done based on the cone angle being lower or higher than 45 degrees, when observ-
ing the total solar wind distribution, solar wind velocities associated with the Qperp bow
shock ($\langle V_{SW,\perp} \rangle \approx 421\ km/s$) have a smaller difference to the solar wind velocities as-
associated with Qpar bow shock ($\langle V_{SW,||} \rangle \approx 444\ km/s$). The standard deviation are found
to be $\sigma || = 100\ km/s$ and $\sigma \perp = 101\ km/s$ respectively. As a result, while the differ-
ence of the solar wind conditions associated to jets is around $\sim 100\ km/s$, for the so-
lar wind, it is only $\sim 20\ km/s$. It should be noted that, the difference between the Qpar
and Qperp solar wind is smaller than one standard deviation. Therefore it is statistically
unlikely that it is the effect contributing the most.

From the discussion above, we can conclude that all four effects (absence of SLAMS,
observational bias, differences in SW, smaller scale ripples) could in principle take place
and contribute to the differences that were observed between the jet properties of Qpar
and Qperp jets.

The distance from the bow shock appears to be different for quasi-parallel and quasi-
perpendicular jets, with Qpar jets occurring on average closer to the bow shock than Qperp
jets. It should be noted, that this result might be artificial since (as discussed above) Qperp
jets are found more frequently during low solar wind dynamic pressure conditions, which
affects the positions of the bow shock and the magnetopause. As a result, when MMS
measures a Qperp jet it will be further away from the bow shock and closer to the mag-
etopause than a Qpar jet found in the same position. To quantify this effect, we used
the average conditions found in the solar wind when Qpar and Qperp jets were observed
and derived a model for the magnetopause and the bow shock. It was found that the av-
erage standoff distance for the bow shock is $R_{0,BS,\parallel} = 14.8\ Re$ for the Qpar jets and
$R_{0,BS,\perp} = 15.3\ Re$ for the Qperp jets. This difference can explain Figure 5. This was
expected since in Figure 6, it was already shown that the average position of MMS for
both classes is the same. Furthermore, by performing the same procedure for the mag-
etopause standoff distance, it was found that the average standoff distance is $R_{0,MP,\parallel} =
10.0\ Re$ for the Qpar jets and $R_{0,MP,\perp} = 10.9\ Re$ for the Qperp jets. Once more, this
can explain the results shown regarding the magnetopause distance in Figure 6. It should
be noted that modeling the bow shock under the typical Qperp SW conditions (very low
dynamic pressure) is problematic since in such cases, BS models may overestimate the
bow shock distance (Dmitriev et al., 2003). While currently we can compare the posi-
tion of jets and justify the observed distributions we cannot draw strong conclusions re-
regarding the relative position of the classes. To do that, a normalization over the magnetosheath regions covered by MMS is required. However, at this point the classification code has been only applied for the jet measurements. Therefore classified (Qpar and Qperp) magnetosheath observations are not yet available.

It should, however, be noted that while possibly affected by modeling issues, the Qperp jets are indeed found closer to the magnetopause and further away from the bow shock as shown in Figure 5 and 6. While at this point a conclusion regarding their nature cannot be drawn, it is possible that Qperp jets are connected to either small scale bow shock ripples or to FTEs that as reported in other studies (Archer & Horbury, 2013) have similar characteristics to Qperp jets shown in this work. While as mentioned above the bow shock ripple mechanism is consistent with our observations, some Qperp jets exhibit properties similar to FTEs. This include density decrease (∼20% of Qperp jets), Alfvénic velocities and southward IMF (∼50% of Qperp jets). As a result, it is possible that the subset of Qperp jets include more than 1 distinct population with possibly different origin. A possible connection to FTEs is planned to be investigated in more detail in the near future.

Finally, Qperp jets have a velocity increase that is on average equally distributed between each velocity component (Figure 9) and more importantly, velocities of the Qperp jets seem to have a different angle compared to the background flow as shown in Figure 10. This result could mean several things. One possibility would be that the observed subset of Qperp jets originating from low-velocity solar wind can have a specific, predetermined velocity orientation. On the other hand, Qpar jets may also originate from a particularly high-velocity solar wind subset which has another distinct, yet different, velocity orientation. Another possible explanation is that Qperp jets have travelled a longer distance in the magnetosheath region compared to Qpar jet (see Figure 5) which could cause the Qperp jet to have a less distinct difference compared to the background magnetosheath flow.

Qpar and Qperp jets exhibit differences regarding their beta values and how magnetic and thermal pressure contribute to their properties. While a higher β is found in the Qpar jets, when subtracting the contribution of the background magnetosheath, another picture arises. Qpar jets have Δβ_{mean} < 0, which means that the magnetic pressure is more important for the jets than for the surrounding magnetosheath. In Qperp jets, however, the jet has a Δβ_{mean} ∼ 0. Specifically, while the overall region (magnetosheath) is basically dominated in both cases by gas dynamics (β_{mean} > 1), the Qpar jets are maybe controlled relatively more by magnetic pressure and the Qperp jets are governed slightly more by thermal pressure.

These changes in β parameter can be interpreted via three different mechanisms. First of all, SLAMS originating from the ion foreshock increase the magnetic field of Qpar jets and create an initial increase in the magnetic pressure compared to the Qperp cases where SLAMS are absent. Secondly, the background magnetosheath regions have differences in density, temperature and possibly magnetic field, which could contribute to different results both in their total β parameter but also when subtracting the background (Δβ). Finally, if we assume that Qperp jets indeed travel longer distances from the bow shock than Qpar jets, the differences in β might provide insight regarding the fate of the jets as they travel in the magnetosheath. Qperp jets are created further away and may have reached a later stage of their existence in which the magnetosheath background flow and the jet are guided equally by the gas dynamics and the background magnetic field. In this case, the weaker Qperp jets are maybe seen in a later stage of their magnetosheath propagation in which their already weak properties make them relatively insignificant to the magnetospheric environment.
5.2 Quasi-Parallel and Boundary Jets

As for the boundary jets, we did not find any significant differences in their properties compared to Qpar jets, indicating a very similar phenomenon. Although some differences can be observed between the two classes, almost all of them can be attributed to the different properties of the background magnetosheath before and after the jet. Specifically, for the boundary jets, by definition, the plasma surrounding them is of both Qpar and Qperp nature. Some authors have speculated that maybe boundary jets are driven primarily by magnetic field tension forces and therefore point to a different origin than the rest of the classes (Archer et al., 2012; Karlsson et al., 2018). However, our results clearly show, both the magnetic field components (Figure 5) and the magnetic field rotation angles (see Figure 10) being very similar to the quasi-parallel jets. Also, all their basic properties are almost identical. Their dynamic pressure and its components have very similar distributions and average values to these of Qpar jets (see Figure 4). The temperature and the magnetic field profiles along with their distance from bow shock are also alike (see Figures 5 & 7). Moreover, the correlations between the different quantities were very similar to the ones found in Qpar jets.

We, therefore, suggest that Qpar and boundary jets form a superset of jets with very similar properties and possibly the same origin. It is unlikely that different physical mechanisms may generate two subsets of jets with so similar statistical properties. One of the things that was not tested however, is how frequent these jets occur compared to how often we exhibit a switch between Qpar and Qperp magnetosheath. A detailed analysis of that could point out a frequency difference if any.

To summarize, our results suggest that the quasi-parallel and the boundary jets are the classes connected to jet-related phenomena, such as the throat aurora (Han et al., 2017; Wang et al., 2018), magnetopause reconnection (Hietala et al., 2018) and possibly the radiation belts (Turner et al., 2012; Xiang et al., 2016). Finally, both Qpar and boundary jets exhibit high earthward velocities and duration, making them important to investigate magnetosphere coupling phenomena and geoeffective properties.

5.3 Encapsulated Jets

From the observations of the encapsulated jets, we can infer that there are at least two distinct subgroups of jets that are perhaps associated to a different formation mechanism.

The first ones are those that exhibit a positive $V_x$ or that have an extremely small velocity, $|V_x| < 20$ km/s (Figure 9, top left). These rare cases (7/57) could be the result of a plasma reflection from the magnetopause (e.g. (Shue et al., 2009)). This picture is also consistent with the general trend that encapsulated jets are found closer to the magnetopause than the rest of the jets, and could also explain why some of the jets have positive $V_x$ since these reflected flows could in principle point to any direction when measured by MMS at any point of their lifetime.

For the encapsulated jets that have a strong enough negative $V_x$ (50/57), a possible scenario is that they are associated with a rotation of the IMF, generating a Qpar and a Qperp plasma environment sequentially. The jet is created in the quasi-parallel plasma environment, having a higher velocity, it gradually overtakes the quasi-perpendicular plasma allowing the formation of a region of Qpar plasma 'encapsulated' within the Qperp magnetosheath plasma to be measured by MMS. Another explanation of the encapsulated jets’ statistical properties is that some of them are FTE events, connected to reconnection events occurring at the magnetopause. Structures with similar properties have been suggested to be FTEs (e.g. (Bosqued et al., 2001; Phan et al., 2004; S. M. Petrinec et al., 2020)) and it is possible that part of their set corresponds to such events. This
Another possible explanation which we propose as the main hypothesis is that the majority of encapsulated jets are a subset of quasi-parallel jets, created at the flanks of the bow shock. This picture provides a direct explanation to the similarities that are generally found between Qpar and encapsulated jets (high velocity increase, low temperature anisotropy, distinct high energy ion population, etc.). After investigating the associated solar wind conditions it was found that encapsulated jets appear when the IMF is dominated by a \( y \) component. This would result in a quasi-perpendicular bow shock close to the subsolar region of the magnetosheath. At the same time, an ion foreshock is formed in the flanks allowing the same effects that apply to Qpar jets to take place.

This picture allows a mechanism similarly described to the bow shock ripple mechanism (Hietala et al., 2009; Hietala & Plaschke, 2013) to generate jets. We hypothesize that the orientation of the normal vector (\( \hat{n} \)) close to the flanks, can deflect the downstream flow into a higher \( yz \) velocity component. Then one can speculate that other effects (e.g. local magnetic field deformation, slingshot effects, etc.) cause a dominant \( yz \) velocity component to be achieved. Finally, the definition we used for encapsulated jets, to be Qpar plasma surrounded by Qperp, creates an observational bias, since in the case that encapsulated jets remain in quasi-parallel environment, they would simply be classified as Qpar jets.

As a result, we believe that encapsulated jets are quasi-parallel jets generated at the flanks, that travel a long distance and are finally measured by MMS in quasi-perpendicular background magnetosheath. This hypothesis is illustrated in Figure 13.

The presented hypothesis also explains how a few encapsulated jets exhibit velocities higher than the upstream solar wind conditions associated to them. First, we have an error at the propagation of solar wind measurements to the bow shock. The data we are using are propagated to the bow shock nose and as a result, there is a time lag error for the solar wind that arrives at the flanks of the bow shock. Secondly, such a jet, originating from the flanks of the bow shock, would take a long time to reach the observation point (MMS). As a result, the solar wind measurement association done for each jet is more unreliable for these cases. It should be noted that while this hypothesis could explain the majority of the encapsulated jets, it may not apply for all of them.

None of the presented mechanism can directly explain why encapsulated jets have a density distribution similar to the quasi-perpendicular jets. In Figure 4 we can see that there is little to no density increase within an encapsulated jet. This effect can be seen more clearly when calculating the difference of the mean density for the jet (\( \Delta n = \langle n \rangle_{\text{jet}} - \langle n \rangle_{\text{min}} \)). Doing so we find that on average there is a density decrease in an encapsulated jet (\( \Delta n_{\text{mean}} = -1.7 \text{ cm}^{-3} \hat{n} \)). This is also supported by the distribution of the relative difference in velocity and density that can be seen in Figure 11 and in Table 4. Here, we see several encapsulated jets showing a density decrease.

One mechanism that can explain the density decrease is if expansion takes place while the jet travels through the magnetosheath region. This could also help to explain the difference of the densities found in Qperp jets that are also found at larger distances from the bow shock. To investigate this hypothesis, we search for correlations between the radial (\( R \)) distance from the bow shock origin point, and the difference in maximum density (\( \Delta n_{\text{max}} \)). Doing so for the subsolar jets (\( n = 289 \)), it was found that they are moderately anti-correlated, \( \rho_{\text{Sp,subsol,}z} = -0.5 \pm 0.05 \). It should be noted that this effect remained when looking at class-specific correlations for the case of subsolar Qpar jets (\( \rho_{\text{Sp,subsol,}z} = -0.27 \)). For the rest of the classes, the sample size of subsolar jets was too small to derive any meaningful results. These results could possibly be interpreted as a weak indication of expansion taking place while the jets travel in the mag-
Figure 13. Visualization of encapsulated jet generation model. We assume a purely $y$ component IMF which creates a large region of quasi-perpendicular angles around the subsolar point while the flanks are of quasi-parallel nature. The formation of the jet is done at the flanks of bow shock where ion foreshock is generated. Sequentially, MMS measures the jet travelling from the flanks towards the subsolar point, while the surrounding plasma is characterized by a constant flow originating from the quasi-perpendicular bow shock (red shaded area).

Another possibility could be that a diffusion process due to magnetic reconnection or Kelvin-Helmholtz instabilities at the boundary between the jet and the background flow occurs, reducing the density of the jet as it travels in the magnetosheath.

To summarize, the encapsulated jets are found on average further away from the bow shock, they have on average a very large velocity in the $yz$ plane while they usually exhibit a density drop. Their exact nature still needs to be determined. If their origin is associated to the bow shock and not other magnetospheric related events, they can provide vital information regarding the evolution of the jet since we hypothesize that they are flows that while having a high velocity they have undergone an expansion that lowers their density compared to Qpar jets. As a result, such a jet, if created at the flanks of the bow shock, it could create a very interesting case study to investigate the dynamic
evolution of its properties from its formation at the bow shock until its observation. However, a possible connection to FTEs could also explain such observations since these jets are occurring close to the magnetopause as shown in Figure 7. A more systematic analysis of these events is required in order to determine the exact nature of this subset of jets.

5.4 Generation Mechanisms of Jets

As mentioned in the previous subsections, the bow shock ripple mechanism (Hietala et al., 2009; Hietala & Plaschke, 2013) is supported indirectly by Figure 7 where we can see that the difference between the temperature of the jet and the background is negative ($\Delta T < 0$) in $Q_{par}$ jets, indicating that the jet flow could be less decelerated than the background flow by passing through a bow shock ripple. Furthermore, in Figure 12(b,d), it was shown that there is a moderate correlation between the maximum velocity difference and the minimum temperature difference. However, it is very hard to draw any conclusion since the correlations are not robust enough. Although it seems that jet generation could be related to the ripples of the bow shock, there could be more factors that influence their generation that may or may not be connected to this mechanism. A more direct way to evaluate the bow shock ripple mechanism would be to analyze the jets that appear close to the bow shock and compare with those found closer to the magnetopause. Doing so, one can quantify how well the initial properties of the jets are explained through the ripple mechanism and whether this effect gradually diminishes as the jets travel towards the Earth. For the sake of completeness, we looked at jets close to the subsolar point and to the bow shock and we found that the anti-correlation increases ($\rho_{Sp,subsolar} \approx -0.65 \pm 0.1$). However, more careful analysis is needed to investigate this effect, and is planned to be done in future studies.

We find support for the SLAMS-related mechanism (Karlsson et al., 2015) when looking at the differences of maximum magnetic pressure (Figure 8) and most importantly at the correlations shown in Figure 12(a,c) between $\Delta n_{max}$ and $\Delta |B|_{max}$. We conclude that SLAMS play an important role in contributing to the dynamic pressure enhancement of some of the $Q_{par}$ jets. This can explain some of the differences in the properties of $Q_{perp}$ jets where SLAMS do not occur since they are a phenomenon typically associated with the quasi-parallel bow shock.

Both the bow shock ripple and SLAMS-associated mechanisms are therefore supported and appear to be key elements of jet formation. However, it could be the case that there are more contributing mechanisms to the formation and composition of jets. As previously discussed, the magnetic field is quite different for each class, while it is consistently correlated to several basic properties of most jets. It is possible that the IMF frozen into the solar wind has a more important impact on the jets than previously thought. The high variance of the magnetic field shown in various jets could indicate instabilities and wave activity that may play a role in establishing the jet properties. We believe that more careful investigation regarding phenomena such as acceleration mechanisms, instabilities, and wave interactions might lead to a more complete answer regarding the origin of the jets.

Finally, there have been several cases where the correlations shown in all the jets disappear when investigating class-specific correlations. This can be interpreted as a validation of the classification, showing that the derived classes indeed represent a very similar yet distinct physical phenomenon. However, it also indicates that, on large scale statistics that include phenomena of diverse nature, correlation-driven conclusions can be unreliable and require further investigation. With the use of advanced techniques originating from probability and information theory (e.g. mutual information) along with careful classification, sampling, and interpretation, we might in the future be able to derive stronger conclusions regarding the origin and generation of jets.
Appendix A Classification Thresholds and Stages

For the classification process we use the following physical quantities:

Averaged "very high" ion differential energy flux
\[ F_{VH} = \frac{1}{3} \sum_{i}^{30-32} F_i \]  
(A1a)

Averaged "high" ion differential energy flux
\[ F_H = \frac{1}{3} \sum_{i}^{27-29} F_i \]  
(A1b)

Averaged "medium" ion differential energy flux
\[ F_M = \frac{1}{5} \sum_{i}^{18-22} F_i \]  
(A1c)

Summed magnetic field standard deviation
\[ \sigma(B) = \sum_{j}^{13} \sigma(B_j) \]  
(A1d)

Ion temperature anisotropy
\[ Q = \frac{T_{T}}{T_{L}} - 1 \]  
(A1e)

Total high / medium energy flux ratio
\[ C = \frac{F_{VH} + F_H}{F_M} \]  
(A1f)

where, \( i \) is the energy channel of the ion energy spectrum and \( j \) is the component of the magnetic field in GSE coordinates. We choose to not multiply with the energy difference \((\Delta E)\) for every bin of the energy flux in order to avoid weighting each flux component differently when averaging over. Very high energy flux represents ions of 16 – 28 keV, high energy is of 7 – 12 keV and medium is between 0.55 and 1.7 keV. More information regarding each energy bin can be found by accessing the MMS file repository (https://lasp.colorado.edu/mms/sdc/public/about/browse-wrapper/)

The classification process holds several stages, thresholds, and methods. In principle, the thresholds of each quantity are varied according to the values shown in Table A1. It should be noted that not all the thresholds have to be met in order for a classification to be made. Necessary criteria include \( F_{VH}, F_H, \) and \( \sigma(\vec{B}) \), while the others serve mainly as quality indicators and were used only for the classes of Qpar and Qperp jets. Furthermore, the actual classification is being done by separating the jet into three periods as explained in the main text (pre-jet, jet, post-jet). Then we apply these thresholds and classify each period depending on the class of the majority of the data points. During each stage, we vary the time period of pre-jet and post-jet slightly in order to allow the algorithm to take into consideration the different time scales that can occur for every jet.

A simplified flowchart is shown in Figure A1, while a more detailed one can be found in the supplementary material. Figure A1 describes the algorithm after the initial cleanup of jets is being done. Jets that are found very close to a bow shock crossing or that contain missing data within their pre/post jet time are not included in the classification algorithm.

As shown in Figure A1, in stage 1 the jet is classified without any iterative process and by using the thresholds found in Table A1. If a jet does not get classified into one of the main classes it is moved to stage 2. In this stage, the algorithm varies the pre/post jet time for a number of tries to take under consideration possible differences between each jet. There are two kinds of variations that we utilize. First, we change the position of the pre and post jet periods to be further away from the jet. Then, we slightly increase the period of time that is initialized as described in Eq. 5. The next stages take the remaining unclassified jets and change the time average window along with the thresholds (Table A1) while again varying the pre/post jet times. At this point, the routine final-
izes the Qpar and Qperp classes that are shown in Table 3. Moving on to stage 4, the algorithm identifies potential boundary and encapsulated jets by normalizing the data and using relative thresholds for the classification. The last stage removes one criterion ($F_H$) in order to allow more jets to be classified to increase the sample size. This stages finalizes the non-emphasized list shown in Table 3. The last step is to manually verify the cases and determine if certain misclassifications occurred, this results in the emphasized (bold) cases shown in Table 3, that are called "final cases". More information regarding the exact procedure can be found in the supplementary material.

### Appendix B Verification Procedure - Fine Parameter Searching

In order to verify the accuracy of the classification scheme, we created a test set of 180 jets (identified by visual inspection) that represent the 4 main classes as shown in Table 2, or that has been categorized as "unclassified". This set has been thoroughly checked by visual inspection in order to represent a characteristic sample of the desired classes that we are looking to classify.

To create an initial classification scheme, some coarse threshold values and techniques are implemented which we evaluated using the manually derived test set in order to quantify the accuracy and the misclassification ratio of the code. The first accuracy results can be seen in Table B1.

Accuracy is defined as the percentage of correct classifications. Misclassification is defined as the percentage of classifications that were incorrectly classified to another main class. For example, if a Qpar jet (class 1) was classified as unknown (class 0), the accuracy is reduced but the misclassification rate does not increase. On the other hand, if it had been classified as one of the main classes (e.g. boundary (class 3)) then the misclassification percentage would increase accordingly.

Based on these results, we adjusted the thresholds several times, slightly changed the procedure and introduced 1 more stage. Then adjustments were made until a maximum value of accuracy and a minimum value of misclassifications were achieved. The final result of the classification scheme regarding its accuracy can be seen in Table B2.
Table A1. Quantities and thresholds used for each stage of the classification procedure. Number in the subscript indicates the average time window in seconds used for each quantity. Prime quantities ($X'$) indicate a re-scaling of the quantity (min-max normalization: $X \in [0, 1]$). Average quantities ($\langle X \rangle$), are computed starting from 1 minute before the jet up to 1 minute after. Finally, $\Gamma = 0.05$ representing a threshold barrier for the normalized quantities. The differential ion energy flux is given in (keV/cm$^3$·s·sr·keV) and the standard deviation of the magnetic field vector in (nT).

<table>
<thead>
<tr>
<th>Stages</th>
<th>Quasi - Parallel</th>
<th>Quasi - Perpendicular</th>
</tr>
</thead>
<tbody>
<tr>
<td>1, 2</td>
<td>$F_{V,H,30} &gt; 2.9 \cdot 10^5$</td>
<td>$F_{V,H,30} &lt; 2.6 \cdot 10^5$</td>
</tr>
<tr>
<td></td>
<td>$F_{H,30} &gt; 4 \cdot 10^5$</td>
<td>$F_{H,30} &lt; 3 \cdot 10^5$</td>
</tr>
<tr>
<td></td>
<td>$\sigma(B)_{60} &gt; 14$</td>
<td>$\sigma(B)_{60} &lt; 13$</td>
</tr>
<tr>
<td></td>
<td>$Q_{30} &lt; 0.4$</td>
<td>$Q_{30} &gt; 0.45$</td>
</tr>
<tr>
<td></td>
<td>$C &gt; 0.1$</td>
<td>$C &lt; 0.075$</td>
</tr>
<tr>
<td>3</td>
<td>$F_{V,H,0} &gt; 3.0 \cdot 10^5$</td>
<td>$F_{V,H,0} &lt; 2.5 \cdot 10^5$</td>
</tr>
<tr>
<td></td>
<td>$F_{H,0} &gt; 4.1 \cdot 10^5$</td>
<td>$F_{H,0} &lt; 2.9 \cdot 10^5$</td>
</tr>
<tr>
<td></td>
<td>$\sigma(B)_{30} &gt; 14$</td>
<td>$\sigma(B)_{30} &lt; 12$</td>
</tr>
<tr>
<td></td>
<td>$Q_0 &lt; 0.3$</td>
<td>$Q_0 &gt; 0.35$</td>
</tr>
<tr>
<td>4, 5</td>
<td>$F_{V,H,0} &gt; \langle F_{V,H,0} \rangle + \Gamma$</td>
<td>$F_{V,H,0} &lt; \langle F_{V,H,0} \rangle - \Gamma$</td>
</tr>
<tr>
<td></td>
<td>$F_{H,0} &gt; \langle F_{H,0} \rangle + \Gamma$</td>
<td>$F_{H,0} &lt; \langle F_{H,0} \rangle - \Gamma$</td>
</tr>
<tr>
<td></td>
<td>$\sigma(B)<em>{30} &gt; \langle \sigma(B)</em>{30} \rangle + \Gamma$</td>
<td>$\sigma(B)<em>{30} &lt; \langle \sigma(B)</em>{30} \rangle - \Gamma$</td>
</tr>
<tr>
<td></td>
<td>$Q_0 &lt; \langle Q_0 \rangle - \Gamma$</td>
<td>$Q_0 &gt; \langle Q_0 \rangle + \Gamma$</td>
</tr>
</tbody>
</table>

Table B1. Initial accuracy before fine parameter searching.

<table>
<thead>
<tr>
<th>Stage</th>
<th>Q-Par (%)</th>
<th>Q-Perp (%)</th>
<th>Bound. (%)</th>
<th>Encaps. (%)</th>
<th>Unknown (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>94.7 0</td>
<td>36.4 0</td>
<td>10.8 0</td>
<td>4 4</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>94.7 0</td>
<td>39.4 0</td>
<td>10.8 0</td>
<td>20 4</td>
<td>0</td>
</tr>
<tr>
<td>3</td>
<td>94.7 0</td>
<td>84.9 0</td>
<td>10.8 0</td>
<td>20 4</td>
<td>11.9</td>
</tr>
<tr>
<td>4</td>
<td>94.7 2.6</td>
<td>84.9 3.1</td>
<td>89.2 0</td>
<td>80 4</td>
<td>45.3</td>
</tr>
</tbody>
</table>

Table B2. Final accuracy after fine parameter searching & last modifications. Emphasized text shows the stages that were found to work ideally for each class.

<table>
<thead>
<tr>
<th>Stage</th>
<th>QPar (%)</th>
<th>QPerp (%)</th>
<th>Bound. (%)</th>
<th>Encaps. (%)</th>
<th>Unknown (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>100 0</td>
<td>36.4 0</td>
<td>13.5 0</td>
<td>4 4</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>100 0</td>
<td>39.4 0</td>
<td>13.5 0</td>
<td>24 4</td>
<td>2.4</td>
</tr>
<tr>
<td>3</td>
<td>100 0</td>
<td>90.9 0</td>
<td>13.5 0</td>
<td>24 4</td>
<td>11.9</td>
</tr>
<tr>
<td>4</td>
<td>100 0</td>
<td>90.9 0</td>
<td>89.2 0</td>
<td>76 4</td>
<td>26.2</td>
</tr>
<tr>
<td>5</td>
<td>100 0</td>
<td>90.9 0</td>
<td>91.9 0</td>
<td>80 4</td>
<td>26.2</td>
</tr>
</tbody>
</table>
The best sample size and classification accuracy for Qpar and Qperp jets were obtained at stage 3. As a result, these classes do not get classified in the later stages. Moving on, for the boundary and encapsulated jets due to the complexity of their structure, all 5 stages are used.

The final step was to manually verify the cases that were misclassified from the underrepresented classes (boundary & encapsulated). After doing so, we found no significant difference between the characteristics of the automatically derived database and the manually cleaned one. However, to ensure the scientific value of the results, we validated the dataset via manual inspection for the cases that the accuracy results were lower and the number of jets was limited (boundary & encapsulated). This process provided the final dataset shown in Table 3, which was then used for the main analysis of this work.

Acknowledgments
We thank the MMS team for providing data and support https://lasp.colorado.edu/mms/sdc/public/. Furthermore, we acknowledge use of NASA/GSFC’s Space Physics Data Facility’s OMNIWeb service, and OMNI data. OMNI High-resolution data are available through https://omniweb.gsfc.nasa.gov/form/omni_min.html. This work was supported by Swedish National Space Agency (SNSA grant 90/17).

The final database of jets can be found in the supplementary material or accessed via zenodo data repository (Raptis et al., 2020).

References


Hietala, H., Laitinen, T. V., Andréeová, K., Vainio, R., Vaivads, A., Palmroth, M., ...


Contents of this file

Text S1

Additional supporting information (Files uploaded separately)

Caption for Figure S2
Caption for Dataset S3

Introduction

The supporting information consists of:

- (Text S1): A detailed description of the algorithm used for the classification of the jets used in the analysis of the main paper. The purpose of this text is to inform the reader of the details of the procedure not given in the appendix.
- (Figure S2): A detailed flowchart to be read along with text S1 for a detailed step-by-step guide through the algorithm used for the classification of jets.
- (Dataset S3): A full table of the dataset that was primarily used for the analysis (See Table 3 on the main paper) is included.

Text S1.

As described in the main article in subsection 3.2, we first identified 8,499 jets from MMS1 measurements between May 2015 and May 2019 according to the criteria shown in Equations (1) and (3) in the main article.
These are then filtered to remove ‘bad events’ and sorted into the different classes (Qpar, Qperp, Boundary, and Encapsulated jets) according to the algorithm, described here and in the flow chart (Figure S2).

Data Pre-process:

This initial stage consists of finding cases of “Missing data” (Class 8) and “Border” (Class 7) jets from the 8499 unclassified cases. Class 7 jets are those found close to a magnetopause or a bow shock crossing.

As shown in Eq. 3 of the main article, the initial necessary information for the classification of a jet contains the pre-jet, jet and post-jet periods. Therefore, the first step is to find jets containing unreliable measurements within these periods, to remove them from the classification process. These jets correspond to the Class 8.

The second class removed in the initial pre-process is class 7 (“Border jets”) which corresponds to jets found very close to a magnetopause or a bow shock crossing. These jets are found by checking whether a crossing was observed up to 5 minutes before or after the jet. If so, these jets are removed from the dataset. All the crossings were found from an automatic procedure that is also used to find where MMS resides in magnetosheath measurements (See subsection 3.1 on the main article).

These procedures remove 45 (Class 8) and 1346 (Class 7) jets. The rest of the database is filtered with the help of the following stages to determine the different jet classes and provide a sufficiently large sample to conduct statistical analysis.

Each of the remaining jets is moved to the next stages of the algorithm until is classified into one of the main classes. The main classes are the Qpar, Qperp, boundary and encapsulated jets (Table 3). If a jet is not classified in these 5 stages it is automatically considered “Unclassified” (Class 0)

Stage 1 – Initial Classification:

The first stage corresponds to a non-iterative algorithm that tries to directly classify jets to one of the main classes.

This is done by applying the thresholds described in Table 3 while using the pre/post jet time shown in Eq.6 of the main article. In particular, the code assigns a characterization for the three periods (Pre, jet, post) and then depending on these three values determines the class of the jet.

Firstly, the rules N.1 are applied. If the jet is not classified then, by using N.2, the algorithm determines whether there is a good indication that the jet can be classified in a future stage. These rules are used to determine if at least 1 period for possible boundary jets or 2 periods for possible encapsulated jets are not characterized as unknown (class 0). If so, these jets are moved to the next stages for further process.
If a jet is found to have all its corresponding periods (pre, jet, post) classified as “unknown” (class 0) then the whole is moved to the unclassified category and is not analyzed furtherly. This stage is the most robust and works very well for Quasi-parallel (Class 1) and Quasi-perpendicular (Class 2) jets. However, while allowing some cases of boundary and encapsulated jets to be classified, the majority of these jets were moved temporarily to classes 4 and 6 to be further processed in later stages and get possibly classified.

Stage 2 – Adjusting pre/post time:

In the second stage, the pre/post time of each jet that was not classified previously is changed.

The adjustment that takes place is of two different variations. The first one that is applied is to move the pre and post time period by 1/2 of its value backward and forward in time respectively. After doing that, we try to classify the jets once more.

At first, the algorithm determines if 4/5 of the total measurements of the whole period (Including pre-time, jet time and post time) correspond to either quasi-parallel or quasi-perpendicular plasma (Rules N.3). If so, we classify the jet to its corresponding class of Qpar or Qperp jet. This addition compared to the previous stage was done to avoid misclassification cases that could result from the variance of the pre-jet and post-jet periods.

The same rules as stage are then applied to determine if a jet belongs to one of the main classes. The only difference originates from the adjustment of the pre and post jet time periods.

The above variation is repeated 6 times, with each iteration adjusting the pre-jet and post-jet time further away from the jet by 1 measurement (4.5 seconds).

If a jet fails to be classified with the above variation, another one is used. Specifically, the algorithm takes up to a 30% increase of the initial time and up to 30% decrease to account for individual variations per jet that were possibly not accurately captured in Eq. 6.

Once more, the procedure follows the method described in Stage 1. Therefore, in total 6 tries for variation A of time adjustment and 6 more tries of Variation B are applied. If a jet remains in classes 4 and 6 it is moved to the next stage.

Stage 3 – Changing average time window:

In the third stage, the same adjustments of the pre and post jet time periods are used, while changing the thresholds that are required to be satisfied.

In all previous stages, we have used a 60-second average window for the magnetic field and a 30 second one for the rest of the quantities. However, doing so, we filtered out small time scale changed that are useful to determine boundary and encapsulates cases. As a result, as shown in Table A1 of the main article (second row), a new set of thresholds is used corresponding to different smoothing of the quantities. In particular, a 30-second window is now used for the magnetic field while the rest of the quantities remain as originally obtained from the MMS.
This stage was effective in finding a few more cases of Boundary (Class 3) and Encapsulated (Class 5) jets. Most importantly, it finalizes the dataset for the Qpar and the Qperp jets.

At this point, it was found that both Qpar and Qperp jets that fit the necessary and the extra criteria (Table A1 and discussion in appendix) have a large enough sample to treat them statistically. As a result, to avoid any false-positive cases, we stop searching for classes 1 and 2 and we keep the jets that reached stage 3 as our final sample for these two classes.

It is important to mention that at this point only a very few cases of boundary and encapsulated jets (Tables B1, B2) are found. This shows that the complexity of these jets is difficult to be captured by the techniques used so far. To increase the sampling of the underrepresented classes (boundary/encapsulated), the algorithm uses only possibly candidates (Classes 4 and 6) to pass through the next stages.

Stage 4 – Normalizing each quantity:

In this stage, a normalization technique is applied to the measurements creating relative thresholds for each case (Table A1).

This procedure increases the number of cases that were initially not classified due to the strict thresholds imposed in the previous stages. On the other hand, it could also increase the number of false positives, making manual verification in a later stage necessary.

At this point, the code introduces a normalization to the quantities (Table A1, last row) and utilizes only one variation of pre/post jet time adjustment (variation B).

Jets that still did not get classified to either category are moved to the final stage.

Stage 5 – Removing a necessary criterion:

In stage five, the exact same procedure as in stage 4 is applied but with removing one necessary criterion. The criterion removed from necessary criteria is the one corresponding to high energy flux $F_H$ (Table A1)

By doing so, more samples were allowed to be classified, enlarging significantly the database. Every jet that fails to be classified at this stage is automatically named “Unclassified” (class 0).

Manual Verification:

As described above, while Qpar and Qperp jets contained a few to no false positives, this is not the case for the boundary and encapsulated ones. Stages 4 and 5 allowed us to significantly increase the size of the database but at the cost of allowing several false-positive cases.

As a result, the first and the second author of the article did the following procedure to ensure that the database accurately reflects the intended classes:
At first, we removed the very few cases of Qpar and Qperp jets that appeared to be close to partial crossing of bow shock or magnetopause. From that procedure, we also found very few cases that contained rapid changes of the magnetosheath (from Qpar to Qperp or vice versa). It was decided that these jets should be moved to “Unclassified” as part of the manual verification procedure.

Finally, plenty of boundary cases were removed since they were considered false positives. These cases originated from stages 4 and 5 which due to the relative thresholds applied (Table A1) classified many jets but were prone to false positives. The same procedure was done for the encapsulated jets, which reduced slightly their final number (Table 3).

This final process provides the “final” cases that are highlighted in Table 3 of the main articles. These cases are also given in the accompanying supplementary material (Data set S3).

**Figure S2.** Flowchart of classification algorithm along with basic information of the algorithm.

**Data Set S3.** Class, starting time, and ending time of all the jets used in the analysis of the main article (“final” cases in Table. 3).