The influence of spacecraft latitudinal offset on the accuracy of corotation forecasts

Harriet Turner¹, Mathew J Owens¹, Matthew Simon Lang¹, and Siegfried Gonzi²

¹University of Reading  
²UK Met Office

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Abstract

Knowledge of the ambient solar wind is important for accurate space-weather forecasting. A simple-but-effective method of forecasting near-Earth solar-wind conditions is “corotation”, wherein solar-wind structure is assumed to be fixed in the reference frame rotating with the Sun. Under this approximation, observations at a source spacecraft can be rotated to a target location, such as Earth. Forecast accuracy depends upon the rate of solar-wind evolution, longitudinal and latitudinal separation between the source and target, and latitudinal structure in the solar wind itself. The time-evolution rate and latitudinal structure of the solar wind are both strongly influenced by the solar cycle, though in opposing ways. A latitudinal offset is typically present, introducing an error to corotation forecasts. In this study, we use observations from the STEREO and near-Earth spacecraft to quantify the latitudinal error. Aliasing between the solar cycle and STEREO orbits means that individual contributions to the forecast error are difficult to isolate. However, by considering an 18-month interval near the end of solar minimum, we find that the latitudinal-offset contribution to corotation-forecast error cannot be directly detected for offsets <6°, but is increasingly important as offsets increase. This result can be used to improve solar-wind data assimilation, allowing representivity errors in solar-wind observations to be correctly specified. Furthermore, as the maximum latitudinal offset between L5 and Earth is [7]50, corotation forecasts from a future L5 spacecraft should not be greatly affected by latitudinal offset.
The influence of spacecraft latitudinal offset on the
accuracy of corotation forecasts

Harriet Turner¹, Mathew Owens¹, Matthew Lang¹, Siegfried Gonzi²

¹Department of Meteorology, University of Reading, Reading, Berkshire, UK
²Met Office, Exeter, UK

Key Points:

- Solar wind speed corotation forecast error is affected by solar activity and spacecraft longitudinal and latitudinal separation.
- Latitudinal separation has little effect when it is below 6°, but increasing importance above this.
- A period in solar minimum gives a 46% increase in mean absolute error from low to high latitudinal offset for STEREO-A and B corotations.

Corresponding author: Harriet Turner, h.turner3@pgr.reading.ac.uk
Abstract
Knowledge of the ambient solar wind is important for accurate space-weather forecasting. A simple-but-effective method of forecasting near-Earth solar-wind conditions is “corotation”, wherein solar-wind structure is assumed to be fixed in the reference frame rotating with the Sun. Under this approximation, observations at a source spacecraft can be rotated to a target location, such as Earth. Forecast accuracy depends upon the rate of solar-wind evolution, longitudinal and latitudinal separation between the source and target, and latitudinal structure in the solar wind itself. The time-evolution rate and latitudinal structure of the solar wind are both strongly influenced by the solar cycle, though in opposing ways. A latitudinal offset is typically present, introducing an error to corotation forecasts. In this study, we use observations from the STEREO and near-Earth spacecraft to quantify the latitudinal error. Aliasing between the solar cycle and STEREO orbits means that individual contributions to the forecast error are difficult to isolate. However, by considering an 18-month interval near the end of solar minimum, we find that the latitudinal-offset contribution to corotation-forecast error cannot be directly detected for offsets < 6°, but is increasingly important as offsets increase. This result can be used to improve solar-wind data assimilation, allowing representivity errors in solar-wind observations to be correctly specified. Furthermore, as the maximum latitudinal offset between L5 and Earth is ≈ 5°, corotation forecasts from a future L5 spacecraft should not be greatly affected by latitudinal offset.

Plain Language Summary
Space weather can damage our technologies, from power lines to satellites, as well as pose a hazard to humans in space. Forecasting space weather requires prediction of solar wind, a continuous outflow of material from the Sun, conditions in near-Earth space. A simple way to achieve this is “corotation”, which assumes the structure of the solar wind is unchanging, but simply rotates around with the Sun. Thus solar wind which sweeps past one spacecraft will arrive at Earth some time later. This forecast will be less accurate when the spacecraft is far from Earth, as we need to wait longer for the solar wind to rotate around, during which time its structure may have changed. If the spacecraft is at a different latitude to Earth, it will also create problems for the forecast. In this study, we quantify the contribution of these factors to the forecast error. This knowledge will improve corotation forecasts, but also aid in other, more sophisticated, forecast techniques. By defining how close spacecraft need to be to Earth to sample the same solar wind, it also helps define where future space weather monitoring spacecraft should be positioned.

1 Introduction
Space weather has the potential to damage electricity grids, cause satellite failures, disrupt communications and threaten the health of humans in space (Cannon, 2013). The most severe space weather events are driven by transient coronal mass ejections [CMEs] (Gosling, 1993). However, prediction of the ambient solar wind is still important for space weather for two reasons. Firstly, the structure of the solar wind impacts the evolution of CMEs through interplanetary space and can determine their arrival time and severity at Earth (Case et al., 2008). Secondly, steady-state structures in the solar wind can also be a driver for space weather events in their own right (e.g. Alves et al. (2006)). High speed streams emanating from coronal holes can compress into the slower solar wind and form stream interaction regions (SIRs), which become corotating interaction regions (CIRs) if they persist for several solar rotations (Reiss et al., 2016). These are regions of higher plasma density and magnetic field strength and can cause geomagnetic disturbances at Earth (Richardson & Cane, 2012). Thus, for accurate space weather forecasting of both
recurrent and non-recurrent events, knowledge of the solar wind conditions near-Earth is required.

The Sun’s magnetic field forms an Archimedean spiral due to the field lines remaining rooted at the Sun as it rotates; this shape is known as the “Parker Spiral” (Parker, 1958). The solar wind flows almost radially away from the Sun; however, fast and slow structures rotate with the Sun, which has a rotational period of 27-days with respect to Earth. Assuming a steady-state solar-wind structure in the rotating solar frame, this means that the same solar wind conditions will reoccur every 27-days at Earth. M. J. Owens et al. (2013) quantified the potential benefit of such 27-day “recurrence” (also called “27-day persistence”) forecasts. They can provide useful long-lead time forecasts and a benchmark for more sophisticated models. The same principle can be used with observations from spacecraft distant from Earth, but at the same heliographic latitude, for example, on the ecliptic plane. Applying a time shift to observations at one spacecraft allows them to be used as a forecast for another, further on in the Sun’s rotation. These are known as corotation forecasts and the reduction in forecast lead time limits (but does not eliminate) the assumption of a completely steady-state solar-wind structure. They have been shown to be a useful forecasting tool, often outperforming the 27-day recurrence model (Simunac et al., 2009; Kohutova et al., 2016; Thomas et al., 2018; Bailey et al., 2020). For observations at the same heliocentric distance, the required time shift \( \Delta t \) is given solely by corotation time \( t_C \), the time it takes the Sun to rotate by the angle \( \phi \) between the longitudes of the observation (referred to as the source) and the location to be forecast (referred to as the target). For \( \phi = 1^\circ \), \( t_C = 1.8 \) hours. However, spacecraft (and the Earth) orbiting the Sun typically have elliptical orbits, resulting in radial distance variations, as shown in panel 1 in Figure 1. This must also be accounted for in the calculation of \( \Delta t \).

Due for launch in 2027, the European Space Agency (ESA) propose to place a space weather monitor at the L5 Lagrangian point, a gravitational null located 60\(^\circ\) behind Earth (Davies, 2020). This point would provide a view of the Sun-Earth line, and so could give a side-on view of Earth directed CMEs (Akioka et al., 2005). It would also present the opportunity to use corotation forecasts from L5 to predict the solar wind conditions near-Earth with a lead time of approximately 4.5 days. The accuracy of corotation forecasts from L5 has been investigated using data from the Solar Terrestrial Relations Observatory [STEREO] (Kaiser et al., 2008) mission during specific phases of the operational lifetime (Simunac et al., 2009; Kohutova et al., 2016; Thomas et al., 2018; Bailey et al., 2020). The STEREO mission consisted of two spacecraft, STEREO-A ahead of Earth’s orbit and STEREO-B behind, moving away from Earth at a rate of \( \sim 22.5^\circ \) per year (Kaiser et al., 2008). Combining these observations with near-Earth data from the Advanced Composition Explorer [ACE] (Stone et al., 1998) or the OMNI data set (Vokhmyanin et al., 2019) provides a number of periods where there are two spacecraft 60\(^\circ\) apart in longitude. Simunac et al. (2009) demonstrated that the profiles of solar wind speed are similar when using STEREO-B as a forecast for STEREO-A at \( \phi \approx 60^\circ \) in July 2008. Further to this, Kohutova et al. (2016) found that using corotation from STEREO-B to ACE improved the forecast of the \( B_z \) component of the interplanetary magnetic field when compared to a 27-day recurrence forecast. Thomas et al. (2018) used different combinations of STEREO and ACE to show the effectiveness of an L5 monitor. It was found that a number of solar wind parameters, including speed, density and temperature, were well predicted using four combinations of spacecraft, with \( \phi \approx 60^\circ \), to produce corotation forecasts. The geomagnetic storm time index (Dst) has also been effectively forecasted through corotation from STEREO-B to OMNI, when \( \phi \approx 60^\circ \) (Bailey et al., 2020). In both cases, corotation provides an improvement from 27-day recurrence.

Although extensive research has been conducted on the effectiveness of corotation from L5, previous studies have been limited to short periods of time when the spacecraft are separated by 60\(^\circ\). The majority of previous analysis has been around periods of low
solar activity (solar minimum). The corotation forecasting method assumes a steady state solar wind; however, in reality the solar wind varies with time and the rate of evolution is linked to the 11-year solar cycle. At solar minimum, the steady state assumption is more valid as solar-wind structure slowly evolves with time. Conversely, at solar maximum the higher activity levels and rapid evolution of solar-wind structure lead to the steady Sun assumption breaking down more readily (M. J. Owens et al., 2013). This means that longer corotation times, and therefore longer forecast lead times, are generally expected to be more accurate at solar minimum than at solar maximum.

As the Sun progresses through the solar cycle, the latitudinal structure of the solar wind changes. At solar minimum, there is a slow solar-wind band centred on the heliographic equator, with faster winds emanating from coronal holes at higher latitudes (McComas et al., 2003). This latitudinal ordering breaks down at solar maximum, due to the weaker dipole component of the Sun’s magnetic field (Wang & Sheeley, N. R., 1991). The variation in latitudinal structure is important for corotation forecasts, as spacecraft in the ecliptic plane vary in heliographic latitude \( \theta \) owing to the 7.25° tilt between the ecliptic plane and the rotational plane of the Sun, as shown in panel 3 of Figure 1. This results in a ‘latitudinal offset’ \( \Delta \theta \) between the point of observation (the source) and the location where the forecast is required (the target). This can introduce a representation error into corotation forecasts that needs to be accounted for in solar-wind data assimilation (M. J. Owens et al., 2020).

As will be demonstrated below, the available observations from the STEREO mission make the effect of \( \Delta \theta \) on corotation forecast accuracy difficult to disentangle from solar activity and \( \Delta t \). In particular, the contribution of latitudinal offset errors to the total corotation forecast error is expected to be significantly higher at solar minimum than solar maximum. Conversely, the contribution from \( \Delta t \) will increase as the corona becomes more dynamic, which is at solar maximum. Finally, as all spacecraft are in the ecliptic plane, large latitudinal spacecraft separation can only occur when there is also large longitudinal separation (and hence large \( \Delta t \)). Thus all contributions to corotation forecast error are interdependent.

Previous study into the error introduced by \( \Delta \theta \) in corotation forecasts has been investigated using steady-state model output. M. J. Owens et al. (2019) and M. J. Owens et al. (2020) showed that \( \Delta \theta \) can have a significant effect on corotation forecast error, especially at solar minimum. It was found that during solar minimum, the solar wind could be considered broadly similar up to \( |\Delta \theta| = 3^\circ \), whereas at solar maximum, this increases to \( |\Delta \theta| = 10^\circ \) (M. J. Owens et al., 2020). Corotation forecast error from L5 to Earth was shown to be up to 80 km s\(^{-1}\) at solar minimum purely due to \( \Delta \theta \) (M. J. Owens et al., 2019), though the peak value occurs around the Winter and Summer solstices. Averaged over the year, this reduces to around 50 km s\(^{-1}\). Although models have shown that a strong effect of \( \Delta \theta \) on corotation forecast error is expected, Allen et al. (2020) found little effect when predicting repeat occurrences of SIRs/CIRs from L5, though this may be the result of compensating errors, as shown below.

The M. J. Owens et al. (2019) and M. J. Owens et al. (2020) work was motivated by improving solar-wind data assimilation (DA) capabilities (Lang et al., 2017). DA combines model output and observational data to find an optimal estimation of reality and is beginning to be used in solar-wind forecasting (Lang & Owens, 2019). Quantifying the error from \( \Delta \theta \) allows observations to be fully utilised through the specification of more accurate observation error covariances and the removal of any potential biases. DA is a step forward in the use of observations for solar wind forecasting as it allows for the observations to be mapped to all longitudes and radial distances, whereas corotation only gives a forecast for a single point. Current DA schemes developed for solar-wind forecasting make use of solar wind speed observations (Lang et al., 2017; Lang & Owens, 2019). Therefore, although corotation can be used for forecasting parameters such as plasma
density and magnetic polarity, only solar wind speed is used here due to its application to DA.

Due to the previous reliance on model output for analysis of the effect of $\Delta \theta$ on corotation forecast error, it is necessary to investigate whether this is present in observational solar wind data. Magnetohydrodynamic (MHD) models produce a solar wind that is ‘smoother’ than what is observed. This means that an error introduced from $\Delta \theta$ could be more easily detected as there are no transient events or any small-scale turbulence. Furthermore, analysis of the model output was steady-state, and so no time variation of the solar wind was captured. This study uses solar wind data from the STEREO mission and near-Earth to investigate the error introduced from $\Delta \theta$.

Sections 2 and 3 will detail the data and methods used to produce our analysis, followed by the results in Section 4. Finally, we will discuss and draw conclusions in Section 5.

2 Data

Corotation forecasts require spacecraft at approximately the same heliocentric distance [$R$] and heliographic latitude [$\theta$] as the intended forecast position (typically Earth), but separated in heliographic longitude [$\phi$]. Greater $\phi$ implies longer forecast lead-times, but also decreases the forecast reliability, as will be demonstrated.

The twin STEREO (Kaiser et al., 2008) spacecraft, in conjunction with near-Earth observations from the OMNI dataset (Vokhmyanin et al., 2019), provide a unique dataset to test corotation forecasting and to better understand the factors that contribute to errors. Here, we use 1-hour STEREO plasma data obtained from the PLASTIC instrument (Galvin et al., 2008) and downloaded from CDAWeb (cdaweb.gsfc.nasa.gov). One-hour OMNI data are obtained from OMNIWeb (omniweb.gsfc.nasa.gov). The heliographic locations of STEREO spacecraft and Earth were obtained from OMNIWeb (omniweb.gsfc.nasa.gov/coho/helios/heli.html). We additionally use daily sunspot number from SILSO (Sunspot Index and Long-term Solar Observations) as a proxy for solar activity, downloaded from sidc.be/silso.

The STEREO spacecraft separate from Earth at a rate of $\approx 22.5^\circ$ per year. Thus from launch in late 2006, they passed behind the Sun in 2014 leading to a data gap in the STEREO-A data from August 2014 to November 2015 and the loss of communication with STEREO-B from August 2014. While both spacecraft orbit the Sun at a distance close to 1 AU, $R$ varies by up to 0.11 AU and must be accounted for when computing corotation forecasts. For completeness, we also take account of Earth’s orbital eccentricity, though the associated change in $R$ is small ($\sim 0.01$ AU).

Here, OMNI data are used for near-Earth solar wind observations. Solar wind data from a succession of spacecraft (including WIND and ACE) located at the L1 Lagrange point is propagated to Earth, providing another source of data for use in corotation forecasts alongside the STEREO spacecraft (Vokhmyanin et al., 2019).

A single spacecraft can be used to provide a corotation forecast for one whole Carrington rotation (approximately 27 days) ahead. Such 27-day recurrence forecasts have already been considered in detail (M. J. Owens et al., 2013). The maximum latitude difference for a single in-ecliptic spacecraft over a 27-day period occurs at the equinoxes and reaches a magnitude of approximately $3.5^\circ$. As will be demonstrated later (see Figure 6), this is insufficient to quantify the latitudinal-offset contribution to corotation forecast error. Thus we focus on pairs of spacecraft. By combining the STEREO-A, B and OMNI spacecraft, there are 6 potential pairs of source (at the position where the solar wind observations are made) and target (at the position of the forecast) spacecraft. These can be seen in Table 1.
Table 1. The possible corotation forecast configurations using STEREO-A, STEREO-B and OMNI solar wind data, where the data from the source spacecraft is used as a forecast for the target spacecraft. A gap in the STEREO-A data exists between August 2014 and November 2015, affecting the STEREO-A to OMNI and OMNI to STEREO-A corotations.

Figure 1. Variation of radial distance, heliographic longitude, heliographic latitude and synodic angular speed of STEREO-A (red), STEREO-B (blue) and Earth (black).
3 Methods

Solar-wind speed corotation forecasts are calculated and tested from combinations of the STEREO and OMNI spacecraft observations of solar wind speed \( V \). (Simunac et al., 2009) and (Thomas et al., 2018) describe this process in terms of mapping between Carrington longitudes at pairs of spacecraft. We here use an equivalent description in terms of time, to make explicit a number of assumptions.

Each hourly \( V \) observation at the source spacecraft \( [V_S] \) is used to produce a forecast \( [V_F] \) at the target spacecraft location at a time \( \Delta t \) in the future:

\[
V_F(t + \Delta t) = V_S(t) \tag{1}
\]

where \( V_S(t) \) is the observed solar wind speed at the source spacecraft at time \( t \). \( \Delta t \) is the required time delay for the same solar wind observed at the source location to reach the target location. Consequently, it is also the forecast lead time. \( \Delta t \) consists of two elements: \( t_R \), the time for solar wind to propagate between the source and target radial distances \( [R_S \text{ and } R_T \text{ respectively}] \) and \( t_C \), the time for solar wind sources to rotate between the source and target longitudes, accounting for spacecraft motion in the inertial frame. This is shown schematically in Figure 2.

Figure 2a shows a time \( t = t_0 \), when the target spacecraft has a longitude of \( \phi_{T0} \) and a radial distance of \( R_T \). Similarly, the source spacecraft has a longitude of \( \phi_{S0} \) and a radial distance of \( R_S \). The first step is to ballistically map the source observations to a radial distance of \( R_T \):

\[
t_R = \frac{R_T - R_S}{V_S(t_0)} \tag{2}
\]

where \( t_R \) is the radial propagation time. As the propagation in radial distance is purely ballistic, it ignores any stream interaction effects or solar wind acceleration. Thus this approach is only valid for \( |R_T - R_S| << R_T \). Given the radial variations of the spacecraft are slow, we assume \( R_S \) and \( R_T \) are constant over the interval \( \Delta t \).

Figure 2b shows that during the interval \( t_R \), the target spacecraft continues to move ahead in longitude at an orbital angular speed in the inertial frame of \( \Omega_{I,T} \). Note that if \( R_S > R_T \), \( t_R \) will be negative and spacecraft will move to smaller \( \phi \) during radial propagation. STEREO-A, B and OMNI spacecraft have different average values of \( \Omega_{I} \), which allows the spacecraft to separate over time. For all three spacecraft these values also vary slowly over the year, owing to the slightly elliptical orbits. This is shown in panel 4 of Figure 1. We account for this effect by computing \( \Omega_{I} \) from the change in \( \phi \) over a 5-day window centred on time \( t_0 \). (This window is short enough to allow for the change in \( \Omega_{I,F} \) over the year, but large enough to remove numerical noise from taking the time gradient of \( \phi_V \).) Over the interval \( \Delta t \), which is typically a few days, it is reasonable to assume a constant value of \( \Omega_{I,S} \), which allows us to express the longitude of the target spacecraft as:

\[
\phi_T(t_0) = \Omega_{I,T} \cdot t_0 + \phi_{T0} \tag{3}
\]

After a time \( t_R \), the solar wind structure observed by the source spacecraft at \( t_0 = 0 \) will corotate with the solar wind, meaning its longitude varies as:

\[
\phi(t_0) = \Omega_{SID} \cdot [t_0 - t_R] + \phi_{S0} \tag{4}
\]

where \( \Omega_{SID} \) is the sidereal rotation speed of the Sun (i.e., \( 2.86 \times 10^{-6} \text{ rad s}^{-1} \)). Thus it will encounter the target spacecraft at a time \( \Delta t \), where:

\[
\Delta t = \frac{1}{\Omega_{SYN,T}} [\phi_{T0} - \phi_{S0} + \Omega_{SID} \cdot t_R] \tag{5}
\]

where \( \Omega_{SYN,T} \) is the synodic orbital angular speed of the target spacecraft, given by \( \Omega_{SYN,T} = \Omega_{SID} - \Omega_{I,T} \).
Figure 2. A schematic of the corotation forecast in the inertial frame. The grey circle tracks the position of a solar wind structure observed by the source spacecraft at time \( t = t_0 \). Top: (a) At time \( t = t_0 \), the target spacecraft (red dot) has a longitude of \( \phi_{T0} \) and radial distance of \( R_T \), while the source spacecraft (blue dot) is at \( \phi_{S0} \) and \( R_S \). (b) Radial propagation from \( R_S \) to \( R_T \) takes a time \( t_R \). (c) Corotation from \( \phi_{S0} \) to the target spacecraft takes time \( t_C \). Bottom: The same steps shown as a time series of \( \phi \). \( \Omega_{I,S} \) and \( \Omega_{I,T} \) denote the orbital angular speed of the source and target spacecraft, respectively, while \( \Omega_{SID} \) denotes the sidereal rotation speed of the Sun.
Figure 3. Time series at daily resolution for the STEREO-B to A corotation forecast, covering the duration of the STEREO-B lifetime. Here, STEREO-B is the source spacecraft and STEREO-A is the target spacecraft. (a) Sunspot number. (b) $|\Delta \theta|$, the absolute latitude difference between the source and target location. The grey horizontal line indicates $7^\circ$, the separation between high and low $|\Delta \theta|$ used in this study. (c) $\Delta t$, the forecast lead time. (d) 27-day rolling average of the daily mean absolute error (MAE) for the corotation forecast. In all panels, the vertical black line separates the definitions of solar minimum and solar maximum used in this study (see main text). The grey-shaded region highlights an interval during solar minimum used for further investigation.

For the STEREO-B corotation forecast of $V$ at STEREO-A’s position, $\Delta t$ is shown as the orange line in Figure 3c.

The observed radial solar wind speeds at the target and source spacecraft ($V_T$ and $V_S$, respectively) are taken from 1-hour resolution data. While the forecast speed, $V_F$, is computed from hourly $V_S$ data, the $t_R$ term means that the computed forecast speed, $V_F$, is no longer on a regular 1-hour time step. Thus, $V_F$ is linearly interpolated back to a standard hourly time base for direct comparison with the $V_T$.

Figure 4 shows a stack plot of $V$ at STEREO-A’s location. This uses a forecasted solar wind from STEREO-B, $V_F$ in blue, with observations by STEREO-A, $V_T$ in red. $V_F$ is produced from time shifting the STEREO-B observations and $V_T$ is used to verify the forecast. Data have been further averaged to 1-day resolution for clarity. It can be seen that the agreement is extremely good for 2007 and 2008, and becomes gradu-
Figure 4. Time series of solar wind speed at STEREO-A’s location. In red is the observed solar wind speed by STEREO-A. In blue is forecast solar wind speed, $V_F$, produced from time shifting the STEREO-B observations. Thus, STEREO-A is the target spacecraft providing the observations to verify the forecast, and STEREO-B is the source spacecraft used to produce $V_F$. Data have been averaged to 1-day resolution for clarity.

ally worse as time progresses. To quantify the degree of agreement we use the mean absolute error (MAE) between the observed and forecast $V$: 

$$MAE = \frac{1}{N} \sum_{n=1}^{N} |V_T(t_n) - V_F(t_n)|$$  

(6)

where $N$ is the total number of time steps considered. MAE is a point-by-point analysis and thus small timing errors in the forecast can be heavily penalised (M. J. Owens, 2018). In the case of a corotation forecast, where the solar wind structure is assumed to be merely time lagged between two positions, the general solar-wind structure should be well reproduced. Therefore MAE is an appropriate metric to use as timing errors indicate a time evolution of the solar wind, for which corotation forecasts should be penalised.

The green line in Figure 3d shows 27-day averages of MAE for STEREO-B observations used to forecast the solar wind conditions at STEREO-A. The increase in MAE in 2007 through 2009 is consistent with the divergence in the time series seen in Figure 4. In Section 4 we consider the different contributions to this MAE, with a focus on quantifying the role of latitudinal difference between the forecast and verification spacecraft. This is measured as:

$$\Delta \theta(t) = \theta_T(t) - \theta_S(t-\Delta t)$$  

(7)

where $\theta_T$ and $\theta_S$ are the heliographic latitudes of the target and source spacecraft/positions, respectively. The absolute value of $\Delta \theta(t)$ is shown in Figure 3b.
Figure 5. Forecast MAE as a function of forecast lead time, $\Delta t$, for solar minimum and maximum periods. Lines show the mean values, while error bars span one standard error on the mean. All STEREO/OMNI spacecraft pairings are used. Only periods with $|\Delta \theta| < 2^\circ$ are included.

Combining the data from the 6 corotation configurations listed in Table 1 allows for the most robust analysis of the variables affecting the forecast error. There are, however, a number of biases in the sampling of this dataset that make it complex to isolate individual factors in corotation forecast error. In particular, the motion of the STEREO spacecraft results in strong aliasing of the $|\Delta \theta|$ and $\Delta t$ with both each other and the solar cycle, and mean that confounding variables and compensating errors are an ever-present problem.

In order to coarsely isolate the influence of solar activity, the data are split into periods of solar minimum and maximum. Given only a single solar maximum is covered by the STEREO data set and the loss of communication with STEREO-B reducing it further, a simple sunspot number threshold is appropriate. We choose a value of 75 sunspots in the total daily sunspot number time series, as this selects the transition from solar minimum to solar maximum in February 2011, when there is a clear step-change in daily sunspot number. Using the same threshold puts the transition from solar maximum to minimum in March 2016.

We further split the data into periods of high and low $|\Delta \theta|$. Given the maximum $|\Delta \theta|$ available with the STEREO/OMNI dataset is approximately 14.5°, we use a cut off of 7°, though this will be further investigated in the remainder of the study.
Figure 6. Variation of mean absolute error (MAE) with $|\Delta \theta|$. Unless otherwise stated, all spacecraft pairings are included. Lines show the mean values, while error bars span one standard error on the mean. Left: The entire dataset (black), further split into solar maximum (red) and minimum (blue). While there appears to be a correlation between MAE and $|\Delta \theta|$ at solar minimum, this could be a result of aliasing of $|\Delta \theta|$ with $\Delta t$. Thus we also show (right) a combination of STEREO-A to B and STEREO-B to A corotations (magenta) and using all corotations (black) for a limited period from August 2009 to February 2011. Both panels show the equivalent modelled MAE at different $|\Delta \theta|$ for steady-state solar wind model solutions (grey). See body text for further description.

4 Results and discussion

We first consider the effect of forecast lead time, $\Delta t$, on forecast accuracy. To minimise the influence of $|\Delta \theta|$, we limit analysis to periods when $|\Delta \theta| < 2^\circ$. Figure 5 shows forecast MAE as a function of $\Delta t$, for all spacecraft pairings. In general, MAE at solar maximum is higher than at solar minimum for the same $\Delta t$, as expected. At solar minimum, there is a trend for increasing MAE with increasing $\Delta t$ out to around 7 days. However, past 20 days, MAE decreases. $\Delta t > 20$ days is confined exclusively to STEREO-A to STEREO-B forecasts very early in the mission, when the spacecraft were still near Earth. Thus the reduced MAE may actually be the result of particularly quiet solar activity levels at this time. Despite 2007-2010 being classified as solar minimum on the basis of a sunspot number threshold, Figure 4 shows a clear difference in the character of the solar wind speed structures between 2007 and 2009, with recurrent fast streams giving way to more persistent slow wind.

Next we consider the effect of $|\Delta \theta|$. Figure 6 shows the differing latitudinal dependencies between solar minimum and solar maximum. At solar maximum, the MAE remains relatively constant at $\sim 80$ km s$^{-1}$. At solar minimum, there is a clear correlation between $|\Delta \theta|$ and MAE. This is the expected behaviour from previous modelling studies (M. J. Owens et al., 2020). However, it is here likely the result of aliasing of $|\Delta \theta|$ with $\Delta t$ and/or sunspot number. This is shown by Figure 7. During the solar minimum interval, splitting the data into high and low $|\Delta \theta|$ does not give equal sampling of either sunspot number or forecast lead time. Thus while MAE is lower for low $|\Delta \theta|$, we cannot rule out the lower mean sunspot number or the existence of lower $\Delta t$ values as being the causal effect.
Figure 7. Probability density of (top) the MAE between the observed and forecast $V_\parallel$, (middle) sunspot number and (bottom) $\Delta t$. Data have been split into solar minimum (left) and solar maximum (right), and into high (black) and low (red) $|\Delta \theta|$ using a threshold of 7°. All STEREO/OMNI spacecraft pairings are included.
Figure 8. Probability density for STEREO-A to B (left) and STEREO-B to A (middle) corotation forecasts limited to the interval August 2009 to February 2011. The right column shows the combined dataset. Rows show (top) the MAE between the observed and forecast $V$, (middle) sunspot number and (bottom) $\Delta t$.

In order to better isolate the effect of $|\Delta \theta|$ it is necessary to further subdivide the dataset. However, a competing requirement is to retain enough data for meaningful statistical analysis. A compromise of these factors is shown as the grey-shaded region in Figure 3, which spans August 2009 to February 2011. This provides a period of time where $|\Delta \theta|$ rises to a large enough value (maximum of $14.9^\circ$) but it is still relatively close to solar minimum, when the latitudinal effect is expected. High and low $|\Delta \theta|$ periods are approximately evenly spaced through this period, meaning both contain similar levels of solar activity. Finally, by comparing the STEREO-A-to-B forecasts with STEREO-B-to-A forecasts, we can effectively eliminate $\Delta t$ as contributing factor, as the two combinations have opposing $\Delta t$ trends.

As can be seen in Figure 8, the interval from August 2009 to February 2011 provides approximately equal sunspot number distributions for high and low $|\Delta \theta|$ periods (see also Table 2). $\Delta t$ distributions are also in approximate agreement, particularly when STEREO-A to B and STEREO-B to A forecasts are combined. Furthermore, the difference in the MAE histograms is consistent when the source/target spacecraft, and hence bias in $\Delta t$, are switched. Thus we can reasonably conclude that the observed difference in MAE between high and low $|\Delta \theta|$ periods shown here is not the result of aliasing with other effects.

It is apparent from Table 2 that there is a distinct difference in the average corotation forecast MAE for high and low $|\Delta \theta|$ times. The average values for MAE are statistically distinct (i.e., differ by far more than one standard error on the mean). Low $|\Delta \theta|$
Table 2. Averages, with associated standard errors, of the corotation forecast MAE, sunspot number and forecast lead time for the STEREO-A to B and STEREO-B to A corotations, for both combined, and for all possible corotations combined (i.e., including OMNI), for the period August 2009 to February 2011.

<table>
<thead>
<tr>
<th></th>
<th>MAE (km s(^{-1}))</th>
<th>Sunspot number</th>
<th>(\Delta t) (hours)</th>
</tr>
</thead>
<tbody>
<tr>
<td>STEREO-A to B High</td>
<td>78.8 ± 3.5</td>
<td>20.1 ± 0.8</td>
<td>395.5 ± 1.8</td>
</tr>
<tr>
<td>Low</td>
<td>54.0 ± 3.2</td>
<td>19.7 ± 1.3</td>
<td>418.6 ± 2.4</td>
</tr>
<tr>
<td>STEREO-B to A High</td>
<td>76.7 ± 3.1</td>
<td>20.3 ± 0.8</td>
<td>259.7 ± 1.7</td>
</tr>
<tr>
<td>Low</td>
<td>52.6 ± 3.7</td>
<td>20.2 ± 1.3</td>
<td>235.2 ± 2.4</td>
</tr>
<tr>
<td>Both corotations High</td>
<td>77.7 ± 2.4</td>
<td>20.2 ± 0.6</td>
<td>327.8 ± 2.8</td>
</tr>
<tr>
<td>Low</td>
<td>53.3 ± 2.4</td>
<td>19.9 ± 0.9</td>
<td>327.1 ± 5.0</td>
</tr>
<tr>
<td>All corotations High</td>
<td>74.0 ± 1.6</td>
<td>21.8 ± 0.4</td>
<td>325.4 ± 3.9</td>
</tr>
<tr>
<td>Low</td>
<td>56.4 ± 1.1</td>
<td>18.7 ± 0.4</td>
<td>330.2 ± 4.5</td>
</tr>
</tbody>
</table>

Table 3. Percentage increase (calculated using Equation 8) from low to high \(|\Delta \theta|\) for average MAE, sunspot number and \(\Delta t\) from Table 2. This covers the period August 2009 to February 2011.

<table>
<thead>
<tr>
<th></th>
<th>MAE (%)</th>
<th>Sunspot number (%)</th>
<th>(\Delta t) (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>STEREO-A to B</td>
<td>46.0</td>
<td>2.0</td>
<td>-5.5</td>
</tr>
<tr>
<td>STEREO-B to A</td>
<td>45.9</td>
<td>0.3</td>
<td>10.4</td>
</tr>
<tr>
<td>Both corotations</td>
<td>45.9</td>
<td>1.2</td>
<td>0.2</td>
</tr>
<tr>
<td>All corotations</td>
<td>31.4</td>
<td>16.7</td>
<td>-1.5</td>
</tr>
</tbody>
</table>
Table 4. Linear correlation coefficients and corresponding p-values for MAE and $|\Delta \theta|$, split into $|\Delta \theta| < 6$ and $|\Delta \theta| \geq 6$. This uses all corotations and covers the period from August 2009 to February 2011.

| $|\Delta \theta|$ | Correlation coefficient | p-value |
|------------------|------------------------|---------|
| $< 6$            | 0.40                   | 0.44    |
| $\geq 6$         | 0.75                   | 0.02    |

Further to this, Table 3 shows the percentage increase in MAE, sunspot number and $\Delta t$ from low to high $|\Delta \theta|$ averages in Table 2. Percentage difference is calculated using Equation 8.

$$\text{% difference} = \frac{x_{\text{high}} - x_{\text{low}}}{x_{\text{low}}} \times 100$$

where $x_{\text{high}}$ and $x_{\text{low}}$ is the data at high and low $|\Delta \theta|$ respectively.

The percentage increase in MAE is consistent at around 46% for the two corotations and when both datasets are combined. It is slightly lower when including the OMNI data, as this skews the data set in favour of low $|\Delta \theta|$ occurrence. For sunspot number, we can see that there is very little increase from low to high $|\Delta \theta|$, with the percentage increases below 2% for the STEREO-A and B corotations. Although there is a positive and negative percentage increase between $\Delta t$ from low to high $|\Delta \theta|$, this seems to have little impact on the difference for MAE. As Figure 5 shows, for solar minimum, the effect of corotation time on MAE increases to $\Delta t = \sim 7$ days (168 hours), where it remains approximately constant thereafter. This could explain the minimal effect that differing $\Delta t$ has for high and low $|\Delta \theta|$, as both for both cases, $\Delta t > 8$ days.

Comparing these results with the right-hand panel of Figure 6, we can see that the MAE contribution from $|\Delta \theta| < 6$ remains approximately constant, before increasing. To assess this, correlation coefficients of MAE and $|\Delta \theta|$ were calculated for $|\Delta \theta| < 6$ and $|\Delta \theta| \geq 6$. These are shown in Table 4. We can see the transition between the two classes of $|\Delta \theta|$, as there is a marked increase in the correlation. The low p-value for $|\Delta \theta| \geq 6$ indicates that there is a strong and significant correlation, whereas below this, the relationship is not significant.

5 Summary and Discussion

Accurate prediction of near-Earth solar wind conditions over the coming hours to days is vital for space weather forecasting and mitigation. By assuming a steady state solar wind, longitudinally-separated observations in or near the ecliptic plane can be used as a forecast for further on in the Sun’s rotation. This implicitly assumes that the solar wind structures seen at both locations will be the same. The accuracy of this “corotation forecast” is affected by time evolution of the solar wind and latitudinal separation ($|\Delta \theta|$). The error due to time evolution is itself a function of how rapidly the solar wind structure is evolving and the lead time of the forecast, which is due to the longitudinal and radial separation of the source and target spacecraft. Increased time evolution is approximately a function of solar activity, and this leads to the steady state assumption breaking down more readily, and so longer corotation times being less valid,
at solar maximum. $|\Delta \theta|$ can introduce a forecast error through sampling a solar wind at the source spacecraft that is not representative of the target spacecraft. This is most important at solar minimum, where a narrow band of slow solar wind is located near the Sun’s equator.

Several studies have shown the effectiveness of corotation forecasts from L5 (Simunac et al., 2009; Kohutova et al., 2016; Thomas et al., 2018; Bailey et al., 2020). These studies used data from periods when combinations of the STEREO and ACE spacecraft were 60° apart in heliographic longitude ($\phi$), and showed that they outperformed the 27-day recurrence forecasts. Due to the limitation of periods where there was such a separation in $\phi$, previous analysis has mostly been restricted to solar minimum. Here, similar methods have been followed; however, the corotation forecasts have not been limited to separations of 60° and so a wider range of the solar cycle has been sampled in order to fully understand the effect of $|\Delta \theta|$.

We have produced corotation forecasts using solar wind speed data from the STEREO mission and OMNI. This produces 6 corotation configurations, mostly covering 2007 to 2014. However, a large amount of aliasing exists within this data set. As the STEREO spacecraft separate, the forecast lead time ($\Delta t$) increases, as does the maximum $|\Delta \theta|$ and sunspot number. Therefore, it is difficult to ascribe an increase in forecast error to a single factor. At solar minimum, the solar wind is highly structured in latitude, whereas at solar maximum this structure is far more dynamic (e.g. Figure 5 of M. Owens (2020)). Thus, the contribution of $|\Delta \theta|$ to corotation forecast error is expected to be a strong function of the solar cycle, with largest contributions at solar minimum and smallest at solar maximum. Conversely, solar-wind structure evolves much more slowly at solar minimum than solar maximum, so the contribution of $\Delta t$ to corotation forecast error is expected to be largest at solar maximum. Finally, as STEREO and OMNI spacecraft are all in the same orbital plane, the largest $|\Delta \theta|$ values are restricted to times of large longitudinal separation and hence large $\Delta t$.

The combined STEREO/OMNI data sets, however, do provide a wide range of $\Delta t$ values during both solar minimum and solar maximum even when restricted to $|\Delta \theta| < 2^\circ$. In general, for a given $|\Delta \theta|$ value, corotation forecast mean absolute error (MAE) is higher at solar maximum than solar minimum. If the elevated MAE at solar maximum was the result of increased time-variability of ambient solar-wind structures, we would expect a correlation of MAE with $\Delta t$. Instead, MAE is fairly constant across the range of $\Delta t$ available at solar maximum, suggesting the increased MAE is the result of increased frequency of transient solar-wind structures at this time (Gopalswamy et al., 2009). At solar minimum, MAE increases steadily with $\Delta t$ up to around 7 days.

To attempt to isolate the $|\Delta \theta|$ contribution, we focused analysis on a period of time where sunspot number and the $\Delta t$ were fairly constant so that $|\Delta \theta|$ could be isolated. This period covered August 2009 to February 2011. Combining STEREO-A-to-B and B-to-A corotation forecasts for this period, the MAE in the corotation forecasts was significantly smaller for low $|\Delta \theta|$ periods (taken to be ($< 7^\circ$) than for high $|\Delta \theta|$ periods ($\geq 7^\circ$). The mean sunspot number and $\Delta t$ values for low and high $|\Delta \theta|$ periods show no significant difference. Thus we can attribute the difference in MAE to latitudinal offset with reasonable confidence.

Looking in more detail at this 8/2009 to 2/2011 period, there is a strong correlation between $|\Delta \theta|$ and MAE for $|\Delta \theta| > 6^\circ$, but not for $|\Delta \theta| \geq 6^\circ$. At around this same latitudinal separation value, the observed forecast MAE becomes comparable to that expected from heliospheric modelling, where only the latitudinal effect is present (i.e. there is no time evolution and no solar wind transients M. J. Owens et al. (2020)). See the grey curve in Figure 6. Thus we suggest that for $|\Delta \theta| < 6^\circ$, the latitudinal offset error in corotation forecasts is present, but is not detectable due to other factors (such as time evolution and CMEs) dominating. For $|\Delta \theta| \geq 6^\circ$, however, the latitudinal offset is the
primary source of corotation forecast error and the magnitude is in good agreement with that expected from steady-state solar-wind modelling. This explains why a latitudinal effect is not detectable in analysis of 27-day recurrence forecasts. The maximum change in latitude for a single spacecraft in the ecliptic plane from one Carrington rotation to the next is $3.5^\circ$, hence the signal not being present. This also implies that for using observations in data assimilation (DA), if $|\Delta \theta| < 6$, observation errors could be assumed constant, where above this, the observational error would be dependent on $|\Delta \theta|$.

Typically, observations with $|\Delta \theta| < 6$ would be preferable for DA and corotation forecasting, as at this separation, the latitudinal effect is minimised in comparison with other sources of error. This finding has implications on the use of future L5 mission data. L5 reaches a maximum $|\Delta \theta|$ of around 5 degrees with Earth (at times close to the Summer and Winter solstices), meaning that the latitudinal variation can be largely disregarded. M. J. Owens et al. (2019) showed that there is a time-of-year variation in the modelled impact of $|\Delta \theta|$ on MAE. This is not investigated here due to data limitations.

The future space weather monitoring mission to the L5 Lagrange point offers a new opportunity for corotation forecasts for the solar wind. The investigation into the effect of $|\Delta \theta|$ on forecast error here has found that for $|\Delta \theta| < 6$, there is a minimal impact due to other sources of error. However, for $|\Delta \theta| \geq 6$, the error contribution increases and there is a clear relationship between $|\Delta \theta|$ and forecast MAE. Due to the maximum $|\Delta \theta|$ between L5 and Earth being 5 degrees, this result implies that the effect from $|\Delta \theta|$ on the forecast error would be minimal.

Moving forwards, this work can aid the effective use of observations in data assimilation for forecasting the solar wind. It will enable more accurate observation error covariances to be calculated when there is a $|\Delta \theta|$ between observations and Earth. Furthermore, this will allow observational errors that result from $|\Delta \theta|$ to be corrected, ensuring the DA methodologies perform optimally.

Acknowledgments

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