Improving the constraint on the Mw 7.1 2016 off-Fukushima shallow normal-faulting earthquake with the high azimuthal coverage tsunami data from the S-net wide and dense network: Implication for the stress regime in the Tohoku overriding plate

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Abstract

Tsunamis with maximum amplitudes of up to 40 cm, related to the Mw 7.1 normal-faulting earthquake off Fukushima, Japan, on November 21, 2016 (UTC), were clearly recorded by a new offshore wide and dense ocean bottom pressure gauge network, S-net, with high azimuthal coverage located closer to the focal area. We processed the S-net data and found that some stations included the tsunami-irrelevant drift and step signals. We then analyzed the S-net data to infer the tsunami source distribution. A subsidence region with a narrow spatial extent (~40 km) and a large peak (~200 cm) was obtained. The other near-coastal waveforms not used for the inversion analysis were also reproduced very well. Our fault model suggests that the stress drop of this earthquake is ~10 MPa, whereas the shear stress increase along the fault caused by the 2011 Tohoku earthquake was only ~2 MPa. Past studies have suggested that horizontal compressional stress around this region switched to horizontal extensional stress after the Tohoku earthquake due to the stress change. The present result, however, suggests that the horizontal extensional stress was locally predominant at the shallowest surface around this region even before the 2011 Tohoku earthquake. The present study demonstrates that the S-net high-azimuthal-coverage pressure data provides a significant constraint on the fault modeling, which enables us to discuss the stress regime within the overriding plate around the offshore region. Our analysis provides an implication for the crustal stress state, which is important for understanding the generation mechanisms of the intraplate earthquake.
Improving the constraint on the $M_w$ 7.1 2016 off-Fukushima shallow normal-faulting earthquake with the high azimuthal coverage tsunami data from the S-net wide and dense network: Implication for the stress regime in the Tohoku overriding plate

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Key Points:
- Tsunamis due to the 2016 off-Fukushima shallow normal-faulting earthquake were observed by the S-net wide and dense pressure gauge network
- Use of the near-field and the high-coverage array significantly improved the constraint of the fault modeling of the 2016 earthquake
- Our fault model suggested that the stress around the focal area should be in a normal-faulting regime even before the 2011 Tohoku earthquake
Abstract

Tsunamis with maximum amplitudes of up to 40 cm, related to the $M_w$ 7.1 normal-faulting earthquake off Fukushima, Japan, on November 21, 2016 (UTC), were clearly recorded by a new offshore wide and dense ocean bottom pressure gauge network, S-net, with high azimuthal coverage located closer to the focal area. We processed the S-net data and found that some stations included the tsunami-irrelevant drift and step signals. We then analyzed the S-net data to infer the tsunami source distribution. A subsidence region with a narrow spatial extent (~40 km) and a large peak (~200 cm) was obtained. The other near-coastal waveforms not used for the inversion analysis were also reproduced very well. Our fault model suggests that the stress drop of this earthquake is $\sim$10 MPa, whereas the shear stress increase along the fault caused by the 2011 Tohoku earthquake was only $\sim$2 MPa. Past studies have suggested that horizontal compressional stress around this region switched to horizontal extensional stress after the Tohoku earthquake due to the stress change. The present result, however, suggests that the horizontal extensional stress was locally predominant at the shallowest surface around this region even before the 2011 Tohoku earthquake. The present study demonstrates that the S-net high-azimuthal-coverage pressure data provides a significant constraint on the fault modeling, which enables us to discuss the stress regime within the overriding plate around the offshore region. Our analysis provides an implication for the crustal stress state, which is important for understanding the generation mechanisms of the intraplate earthquake.

Plain Language Summary

On November 21, 2016 (UTC), a large earthquake occurred within the continental plate off Fukushima, Japan, and a new seafloor tsunami network, S-net, recorded its tsunamis with much higher azimuthal coverage and with shorter epicentral distance than any of the previous networks. We analyzed the S-net data to reveal the rupture process of this earthquake. Our result explained all of the S-net data and the other tsunami network data very well. According to past studies, the continental plate in northeastern Japan was under horizontal compression before the 2011 Tohoku earthquake due to the pushing force by the subducting oceanic plate. However, our rupture modeling result suggested that the plate around the earthquake rupture area was horizontally stretched even before the Tohoku earthquake, so that the off-Fukushima earthquake occurred. Our study demonstrated that the S-net, which has high spatial coverage, makes it
possible to reveal the rupture model of offshore earthquakes, which was difficult in the past before S-net became available. The S-net will also enable us to discuss the impact of the Tohoku earthquake on the crustal stress, which is necessary for understanding the earthquake generation mechanics.
1 Introduction

In this decade, the coseismic rupture process of the 2011 Tohoku earthquake and its
preseismic and postseismic processes have been investigated in detail (e.g., Hino, 2015; Kodaira
et al., 2020; 2021; Lay, 2018; Uchida & Burgmann, 2021; Wang et al., 2018). In response to the
Tohoku earthquake, a new wide offshore deep-ocean observation network, Seafloor Observation
Network for Earthquakes and Tsunamis along the Japan Trench (S-net), has been constructed off
eastern Japan (Aoi et al., 2020; Kanazawa et al., 2016; Mochizuki et al., 2017; Uehira et al.,
2016, Figure 1a). Recent studies have started to utilize S-net ocean bottom seismometers to
investigate the seismotectonics and geodynamics in the Tohoku subduction zone (Hua et al.,
2020; Matsubara et al., 2019; Nishikawa et al., 2019; Sawazaki & Nakamura, 2020; Takagi et al.,
2019, 2021; Tanaka et al., 2019; Uchida et al., 2020; Yu & Zhao, 2020). The S-net also
incorporates ocean-bottom pressure gauges (OBPGs), which are expected to be utilized for
tsunami forecasts (e.g., Aoi et al., 2019; Inoue et al., 2019; Mulia & Satake, 2021; Tanioka,
2020; Tsushima & Yamamoto, 2020; Wang et al., 2021; Yamamoto Aoi et al., 2016; Yamamoto,
Hirata et al., 2016). The other potential contributions to the earth sciences of the S-net OBPG
have also been demonstrated, such as understanding the wave propagation process in the ocean
as well as the rupture process of subseafloor earthquakes (Kubota, Saito, & Suzuki, 2020;
Kubota et al., 2021; Saito & Kubota, 2020; Saito et al., 2021). The wide and dense network data
of S-net will significantly broaden our understanding of the Tohoku subduction zone after the
Tohoku earthquake.

On November 21, 2016, a major shallow normal-faulting earthquake occurred within
the overriding plate off Fukushima Prefecture (20:59 UTC, $M_w$ 6.9, 12 km, Global CMT
[GCMT], https://www.globalcmt.org, Figure 1, hereafter referred to as the off-Fukushima
earthquake). Compared with the GCMT centroid, its epicenter, as determined by Japan
Meteorological Agency (JMA), was located ~20 km east to northeast (white star in Figure 1).
Numerous aftershocks accompanied this earthquake (Figures 1b and 1c). It has been reported
that the tsunamis associated with the off-Fukushima earthquake were observed by onshore and
offshore tsunami networks (e.g., Gusman et al., 2017; Kawaguchi et al., 2017; Suppasri et al.,
2017). However, these stations were located only on the shore-side from the focal area, and the
source-station distances are large (Figure 1a). In contrast, the S-net OBPGs recorded tsunamis
with much higher azimuthal coverage and with a closer distance to the focal area (~30 km,
Because of the much better station coverage of the S-net, the constraint on the initial sea height (tsunami source) estimation and the finite fault modeling of the off-Fukushima earthquake will be significantly increased, as compared with the previous datasets. The normal-faulting mechanism of the off-Fukushima earthquake is similar to nearby shallow normal-faulting micro-seismicity within the overriding plate, with a tensile axis ($\sigma_3$) oriented in basically the east-west direction, which significantly increased after the Tohoku earthquake (Figures 1d–1f, e.g., Asano et al., 2011; Hardebeck & Okada, 2018; Hasegawa et al., 2012; Tanaka et al., 2014; Wang et al., 2019; Yoshida et al., 2012). This increase in the normal-faulting seismicity is considered to be related to the significant stress perturbation by the Tohoku earthquake, which switched the intraplate stress regime from horizontal compression to horizontal extension (e.g., Hasegawa et al. 2012). If we can obtain a detailed fault model of the off-Fukushima earthquake, then the quantitative relationship between the crustal stress released during the off-Fukushima earthquake and the stress increase due to the 2011 Tohoku earthquake can be discussed. This quantitative comparison will be useful to deepen our understanding of the temporal change of the crustal stress state associated with the Tohoku earthquake.

In the present study, we therefore estimate the detailed finite fault model of the off-Fukushima earthquake using the S-net OBPG data. From the finite fault model, we also attempt to examine the normal-faulting stress state within the crust around the off-Fukushima earthquake and its relationship with the Tohoku earthquake. The OBPG data process is described in Section 2, and Section 3 summarizes the feature in the S-net OBPG data. The spatial distribution of the initial sea surface height (tsunami source) and the finite fault model of the off-Fukushima earthquake are estimated in Sections 4 and 5, respectively. Section 6 examines the relationship between the Tohoku earthquake and the stress regime around the focal area. Section 7 concludes the present study.
Figure 1. (a) Location map of the present study. Locations of the tsunami stations are shown by colored symbols (black circle: S-net OBPG, blue inverted triangle: ERI OBPG, yellow inverted triangle: Tohoku University OBPG, orange square: NOWPHAS GPS buoy, pink triangle: NOWPHAS wave gauge). The epicenter (white star) and the CMT solution (red) of the off-Fukushima earthquake are taken from JMA and GCMT, respectively. (b) Enlarged view of the rectangular area drawn by gray lines in Figure 1a. Aftershocks during about one week as determined by JMA are shown (color denotes its depth). Orange contours show the depth of the subducting plate interface (Nakajima & Hasegawa, 2006). The locations of fresh seafloor cracks found by the JAMSTEC survey are shown by blue triangles. (c) Vertical cross section along line A-A’ in Figure 1b. (d–f) The F-net fault mechanisms (Fukuyama et al., 1998) at depths shallower
than 20 km, (d) before the Tohoku earthquake, (e) during the Tohoku earthquake and the off-Fukushima earthquake, and (f) after the off-Fukushima earthquake.

2 Tsunami dataset

The present study used the S-net OBPG data (black circles in Figure 1a), which was also used by Wang & Satake (2021). Although S-net now consists of 150 observatories (Aoi et al., 2020), 25 of these observatories, located at the outer-trench region, were not installed when the off-Fukushima earthquake occurred. Each observatory is equipped with absolute pressure sensors manufactured by Paroscientific, Inc. (e.g., Polster et al., 2009; Watts & Kontoyianiss, 1996). Two pressure sensors are equipped in each observatory for redundancy. The sensors are not directly exposed to the seawater, but rather are sealed in a metal housing filled with oil. The metal housing is further sealed in a metal cylindrical vessel filled with oil. The external pressure is transferred to the pressure sensor inside via a diaphragm made of hard rubber. See Aoi et al. (2020) for more details.

In addition to S-net, we use other OBPGs to evaluate the modeling resolution. We use the OBPGs off Iwate Prefecture installed by the Earthquake Research Institute (ERI) of the University of Tokyo (blue inverted triangles in Figure 1a, Gusman et al., 2017; Kanazawa & Hasegawa, 1997) and the OBPGs off eastern Japan installed by Tohoku University (yellow inverted triangles, Hino et al., 2014). We also use the offshore GPS buoys (orange squares) and wave gauges (pink triangles) of the Nationwide Ocean Wave information network for Ports and HArbourS [NOWPHAS] (Kawaguchi et al., 2017; Nagai et al., 1998).

3 Fundamental feature of the S-net OBPGs: Tsunami-irrelevant pressure signals

In order to investigate the fundamental feature of the S-net OBPG signals, we first process the OBPG data. We decimate the original 10 Hz data to 1 Hz (Figure 2). We then subtract the theoretical tide calculated by the model of Matsumoto et al. (2000) and apply a low-pass filter with a cutoff of 100 s to reduce the high-frequency seismic wave signals (Figure 3). Figure 2 shows the 1-Hz-sampling pressure waveforms. The high-frequency fluctuations related to the seismic waves and ocean-acoustic waves (e.g., Kubota, Saito, Chikasada et al., 2020) are observed. The gradual pressure increases related to the ocean tide are also observed, although some traces show different trends. The pressure changes recorded by the
two sensors equipped in the same observatory (black and gray lines) are very similar to each other. The difference between these two traces (red lines) is around zero, although some stations have offsets in the differences. At station S2N13, which is located just above the focal area of the off-Fukushima earthquake, no seismic or tsunamis signals were recorded.

Figure 2. The 1-Hz ocean-bottom pressure waveforms for stations (a) S2N02, (b) S2N03, (c) S2N06, (d) S2N13, (e) S2N12, (f) S2N11, (g) S2N14, (h) S2N15, and (i) S2N18. Black and gray traces denote the waveforms from each of the pressure sensors. Red traces denote the difference between the two sensors. Note that the vertical scale for the difference waveforms is different in each subfigure. The dominant signals are indicated by arrows and text. The epicentral distance $\Delta$ measured from the JMA epicenter, and the tilt change $\lambda$, rotation angle change $\theta$, and PGA values measured by the co-equipped accelerometer (Takagi et al., 2019) are also shown.
Figure 3. Ocean-bottom pressure waveforms after data processing for the stations. See Figure 2 for a detailed description.

Although the tsunamis are confirmed in the lowpass-filtered S-net OBPG waveforms (Figure 3), we also recognize some unfamiliar pressure signals irrelevant to the tsunamis, such as the large drift components (e.g., S2N06, S2N18). Since the observed drift rates are very large (e.g., ~50 hPa/hour at S2N06), these drifts are considered to be due to neither tsunamis nor postseismic seafloor deformations. It might be possible that the mechanical drifts of the pressure sensors are the cause of these drifts, because it was reported that the Paroscientific pressure sensors contain instrumental drift with rates of ~8.8 hPa/year (Inazu & Hino, 2011; Polster et al. 2009; Watts & Kontoyianiss, 1996). However, the previously-reported drift rates of the Paroscientific pressure sensors are much smaller than those confirmed in the S-net. In addition, it is incomprehensible that the drift rates are completely identical in the sensor pair, although the drift rates must be different in each sensor. Therefore, we do not consider the cause of these
drifts to be as previously reported. Although we cannot identify the reason for these drifts, we suspect the observation system of the S-net may be related to the cause of the drift.

In addition, abrupt steps at the origin time are observed at some OBPGs, particularly at S2N11, S2N12, S2N14, and S2N15. The step is also observed at S2N13, where no tsunami signals were recorded (Figure 3d). If we consider the pressure offset changes as a result of the seafloor vertical movement, these pressure changes correspond to a seafloor vertical displacement of ~30–60 cm (assuming a pressure change of 1 hPa is equal to a seawater column height change of 1 cm H$_2$O). Considering the source-station distances, these displacements seem too large compared with those expected from typical M~7 earthquakes. Furthermore, even if the OBPGs are located inside the focal area where the vertical displacement is large, the ocean-bottom pressure, or the seawater column height above the OBPG, cannot change so abruptly because both seafloor and sea-surface simultaneously move vertically during tsunami generation (e.g., Tsushima et al. 2012). Therefore, these steps are unlikely to be caused by the seafloor permanent displacement. Similar pressure steps were also recorded by the S-net and the other OBPG networks during the past earthquakes (Kubota, Suzuki et al., 2018; Kubota, Saito, Suzuki, 2020; Wallace et al. 2016), which are not considered to be related to the tsunami or the seafloor crustal deformation.

It has been reported that outputs of Paroscientific pressure sensors strongly depend on its orientation relative to the direction of gravity (Chadwick et al., 2006). Thus, the step signals might be caused by the rotation of the pressure sensor. According to Chadwick et al. (2006), the rotation angle change of the pressure sensor of $\theta \sim 10^\circ$ roughly corresponds to the apparent pressure offset change of up to ~10 hPa. Takagi et al. (2019) analyzed the co-equipped accelerometer during the off-Fukushima earthquake and found that some observatories near the epicenter rotated associated with large seafloor ground motion (Figures 2 and 3). However, comparing the rotation angles at some near-source stations (e.g., $\theta = 0.86^\circ$ at S2N12 and 9.95$^\circ$ at S2N14, Takagi et al., 2019), the observed pressure steps were extremely large ($> ~50$ hPa).

Furthermore, considering that the sensitivity to the rotation angle must be different in each sensor, it is quite strange that the amounts of the pressure step in two pressure sensors are almost identical. We also confirm that the pressure steps in the two pressure sensors are different at some stations where the large rotation was observed (e.g., S2N13, S2N15), leading to the steps around the focal time in the difference traces between the two sensor outputs (red lines in Figure...
3). Taking these points into account, we consider that the dominant cause of the pressure steps is not the response to the sensor rotation, as reported by Chadwick et al. (2006), but might be the observation system of the S-net, and the difference in the steps between the two sensors may be due to the difference in the response to the rotation angle. As a summary of this section, we emphasize that we must be careful to analyze the OBPG data to distinguish whether such signals are real or are artifacts related to the drift or offset, although the S-net OBPGs clearly recorded the tsunamis due to the 2016 off-Fukushima earthquake.

4 Tsunami source modeling

4.1 Modeling procedure

In this section, we analyze the S-net data to estimate the spatial distribution of initial sea-surface height (tsunami source) of the off-Fukushima earthquake and to investigate how the S-net OBPGs provide better constraint. In order to reduce the long-period tsunami-irrelevant drift signals as well as the short-period seismic wave components, we apply the bandpass filter with passbands of 100–3,600 s (Figure 4b). We here briefly describe the procedure for the tsunami source modeling. The full details are shown in Text S1.

We set the analytical area as 50 km × 50 km (rectangular area in Figure 4a) and distribute the unit source elements of the seafloor vertical displacement with horizontal spatial intervals of 2 km. Assuming that the seafloor displacement from the unit source elements is equivalent to the initial sea-surface height change, we simulate a tsunami by solving a linear dispersive tsunami equation (Saito, 2019; Saito et al., 2010). We use the JTOPO30 bathymetry data with a spatial resolution of 30 arcsec (http://www.mirc.jha.jp/en/), interpolating the spatial interval of \( \Delta x = \Delta y = 1 \) km. The displacement is assumed to occur instantaneously at time \( t = 0 \) s.

After calculation, the pressure offset change due to the seafloor displacement is subtracted from the sea-surface height change assuming that a sea height change of 1 cm \( H_2O \) is equal to a pressure change of 1 hPa (the method of Tsushima et al., 2012). We finally apply the same bandpass filter to the simulated waveform as that applied to the observation.

In the inversion analysis, we use the time-derivative waveforms for the inversion analysis (\( \partial p / \partial t \), the method of Kubota, Suzuki et al. (2018)), because the time-derivative can reduce the artificials due to the tsunami-irrelevant steps, which becomes the impulse and thus does not contain the offset change. The data time window used for the modeling is manually
determined, which includes the main part of the tsunami (indicated by the blue traces in Figure 4c). The goodness of the estimated source is evaluated using the variance reduction (VR):

$$VR = 1 - \frac{\sum (d_{i}^{\text{obs}} - d_{i}^{\text{cal}})^2}{\sum d_{i}^{\text{obs}2}} \times 100\%$$  \hspace{1cm} (1)

where $d_{i}^{\text{obs}}$ and $d_{i}^{\text{cal}}$ are the $i$-th data of the observed and calculated time-derivative pressure waveforms. We impose the smoothing constraint for the inversion, and its weight is determined based on the trade-off between the weight and the VR (Figure S1) to avoid both the overfitting and oversmoothing of data.

4.2 Results

Figure 4 shows the results of the inversion. A subsidence with a horizontal extent of ~40 km $\times$ ~20 km, having a sharp peak near the GCMT centroid, was obtained (Figure 4a). The direction of the northeast-southwest extents of the subsided region is consistent with the GCMT strike angle of 49°. The northwest edge of the subsidence region is consistent with the locations where the seafloor displacements of 1–2 m and fresh seafloor cracks were found by a seafloor bathymetry survey just after the off-Fukushima earthquake conducted by Japan Agency for Marine-Earth Science and Technology [JAMSTEC] (blue triangles in Figure 4a). The time derivatives of the S-net pressure waveforms were well reproduced (VR = 95.7%, Figure 4c). Except for the waveforms just after the focal time at some near-source OBPGs, the observed pressure is also well explained (Figure 4b). The waveforms recorded at the other tsunami stations (Figure 1a) are also reproduced surprisingly well (Figure 5), even though they were not used for the inversion. This suggests that the use of the S-net tsunami data provides good spatial resolution of the tsunami source, and thus it is expected that we can obtain a reliable fault model. Note that the later arrivals in some stations (e.g., ~100 min at TM1 and TM2) are not well reproduced, which are caused by the coastal-reflections (Gusman et al., 2017). This is probably because the spatial resolution of the coastal shape from the topography data in our simulation is
not sufficient ($\Delta x = \Delta y = 1$ km) to reproduce the reflected tsunami waves, and the high-resolution bathymetry data is important to reproduce the reflected tsunamis (Gusman et al., 2017; Kubota, Saito et al., 2018).

**Figure 4.** Results of the tsunami source inversion. (a) Spatial distribution of the tsunami source. Contour lines denote the subsided region with intervals of 20 cm. The white star is the JMA epicenter, and blue triangles denote the location of the seafloor survey, where fresh surface cracks were found. The yellow and gray circles show the S-net OBPG locations used or not used, respectively, for inversion analysis. Comparisons of (b) the pressure waveforms and (c) the time-derivative waveforms. The gray and red traces denote the observed waveforms and simulated waveforms from the tsunami source model. Traces marked by blue lines denote the time window used for the inversion analysis.
Figure 5. Waveform comparisons for the other tsunami stations, from the tsunami source model, for (a) NOWPHAS Near-coastal GPS buoys, (b) NOWPHAS wave gauges, (c) OBPGs installed by ERI, and (d) OBPGs installed by Tohoku University. At station 801, the waveforms during the data missing are not drawn. See Figure 1 for station locations.
In the inversion, we used the time-derivative waveforms of the pressure to reduce the artificials attributed to the tsunami-irrelevant pressure components (Kubota, Suzuki et al., 2018). In order to see how well this method reduced the artificials, we also conduct the additional inversion using the original pressure waveforms, instead of its time-derivative waveforms (Figure S2). The weight of the smoothing is also determined based on the VR between the observed and simulated pressure waveforms (Figure S1). As a result, the distribution of the tsunami source is fundamentally similar to the original distribution, although a significant artificial uplift of > 60 cm is estimated around S2N14 where the large step was recorded. In order to avoid this artificial due to the tsunami-irrelevant components, using the inversion method by time-derivative waveforms (Kubota, Suzuki et al., 2018) worked very well to reduce the artificial due to the apparent step signals irrelevant to the tsunami or the seafloor displacement.

We compare the tsunami source model estimated by the present study with the models obtained using the tsunami data, except for the S-net data, by Gusman et al. (2017) (Figure 6a), Adriano et al. (2018) (Figure 6b), and Nakata et al. (2019) (Figure 6c). The horizontal location and spatial extent of the subsided region of our tsunami source model roughly correspond to those obtained by the previous studies. However, the amount of the maximum subsidence was much larger than the previous models and the locations of the peak subsidence of tsunami source are slightly different from each other. Our tsunami source model had a maximum subsidence of ~238 cm, whereas the two models obtained from the far-field tsunami data (Gusman et al. 2017; Adriano et al., 2018) underestimated the subsidence (~180 cm and ~130 cm, respectively, Table 1). The subsidence peak of our model was located ~5–10 km southeast of the models by Gusman et al. (2017) and Nakata et al. (2019) and ~10 km east of the model by Adriano et al. (2018). One reason for these differences may be the assumption of the fault geometry, but the more significant reason should be the station coverage and the source-station distance. The coastal tide gauges or the offshore stations used in these previous studies were located far from the source region and the stations at the offshore side of the source region were not used in these studies, whereas the S-net has better station coverage and a smaller source-station distance. This could provide a better constraint on the horizontal location and peak displacement amount to reproduce surprisingly well the tsunami waveforms not used for the inversion. Thanks to this improvement in the constraint, we believe that we can obtain a finite fault model with a higher resolution, as shown in the next section.
Figure 6. Comparison of the tsunami source calculated from the finite fault models of the previous studies (black contours) and the tsunami source model (red). Models of (a) Gusman et al. (2017), (b) Adriano et al. (2018), and (c) Nakata et al. (2019) are shown. The contour intervals are 20 cm. The configuration of the fault is also shown by gray lines.

5 Fault modeling

5.1 Rectangular fault model with uniform slip

Here, we attempt to constrain the finite fault model of the off-Fukushima earthquake. The horizontal location and the peak subsidence of our tsunami source distribution are slightly different from the other previous models. Therefore, we first constrained the optimum fault location based on a grid-search approach (Kubota et al., 2015; 2019). In the grid-search, we assume one planar rectangular fault with a uniform slip. The strike angle of the fault is fixed to the GCMT value ($\text{strike} = 49^\circ$), considering the consistency with the direction of the northeast-southwest extent of the tsunami source. Since the dip and rake angles cannot be constrained only from the tsunami source, we assume these angles based on the GCMT solution ($\text{dip} = 35^\circ$ and $\text{rake} = -89^\circ$), as inferred from the analysis of the teleseismic data. To find the optimum model that best reproduces the S-net waveforms, we vary the other fault parameters and simulate tsunamis. The unknown parameters of the rectangular fault that we search are the fault center location (longitude, latitude, and depth) and its dimensions (length $L$ and width $W$). The slip amount on fault $D$ is adjusted to maximize the VR in Eq. (4). The search range for these parameters is summarized in Table S1, which is determined based on the tsunami source model obtained in the previous section. Using an assumed rectangular fault with a set of parameters (the
fault model candidate), we calculated the seafloor displacement (Okada, 1992) and simulated the tsunamis. The goodness of each of the fault model candidates is evaluated using the VR values. The horizontal location of the optimum fault is shown in Figure 7a. The detailed results of the grid-search analysis are shown in Figure S3. We obtain the optimum fault model as $L = 15\, \text{km}$, $W = 10\, \text{km}$, and $D = 467.7\, \text{cm}$ ($M_0 = 2.1 \times 10^{19}\, \text{Nm}$, $M_w = 6.8$, assuming a rigidity of $\mu = 30\, \text{GPa}$). The center of this model is located at a depth of 10 km, ~10 km east of the GCMT centroid (the detailed parameters are listed in Table 1). The GCMT centroid depth was 12 km and the aftershocks are mainly located at depths of ~ 20 km (Figures 1b and 1c), whereas the estimated fault is located at the very shallow part of the crust (Figure 1c and Table 1). This disagreement has also been pointed out by Gusman et al. (2017) from their numerical simulations. They suggested that the aftershocks determined from the inland network are systematically deeper than the actual depth. The horizontal extent of the tsunami source is relatively narrow and is located at the northeast, compared with that obtained by the inversion analysis (Figures 7a and S3a). The reproductivity of the S-net pressure waveforms is reasonable (Figures S3b and S3c), although the VR is lower than that for the tsunami source inversion ($\text{VR}_{\text{optimum}} = 59.3\%$). These mismatches are probably because of the simple assumption of the rectangular fault, which could not reproduce the southwest part of the tsunami source.
Figure 7. (a) Horizontal location of the optimum rectangular fault model. The red rectangle shows the location of the rectangular fault model. (b–i) Evaluation of the fault dimension. Comparisons of the stations near the epicenter between the observed (gray) waveform and the simulated waveforms from the varied fault dimensions are shown. The simulated waveforms with thick red and blue traces denote the optimum rectangular fault.
If we consider the empirical scaling relations from the magnitude, then the fault dimension is expected to be \( \sim 700 \text{ km}^2 \) (e.g., Wells & Coppersmith, 1994). On the other hand, the estimated fault dimension of 150 km\(^2\) is much smaller. In order to assess the dimensions of the rectangular fault, we simulate tsunamis, fixing the seismic moment \( M_0 \) and the fault center location to the optimum model and varying the fault dimensions. In Figures 7b to 7i, we compare the waveforms of representative S-net stations relatively close to the focal area. If we assume a larger fault with \( L > 20 \text{ km} \), then the arrival of the peak downheaval wave and its amplitude cannot be explained for the stations located northward (S2N01 and S2N02) or southward (S2N14 and S2N15) from the source. In addition, the sharp peak of the downheaval waves observed at the stations located eastward (S2N09, S2N10, S2N11, S2N12, and S2N15) from the source are not well reproduced by the fault width for the case in which \( W > 15 \text{ km} \). These results suggest that the fault dimensions should be \( L \leq \sim 20 \text{ km} \) and \( W \leq \sim 15 \text{ km} \). Considering this range, the estimated fault dimensions are obviously smaller than expected based on the scaling relation. These much smaller fault dimensions are consistent with the size of the asperity, defined as the region of the large slip on the fault (e.g., Somerville et al., 1999), expected from the empirical relation deduced from the inland crustal earthquakes (Somerville et al., 1999; Miyakoshi et al., 2020). This may suggest that this optimum rectangular fault corresponds to the asperity.

5.2 Slip distribution

We then conduct a finite fault inversion to estimate the slip distribution (finite fault model) in a similar manner to that reported by Kubota, Saito et al. (2018). We assume a rectangular planar fault with dimensions of 45 km \( \times \) 30 km, so that the fault passes through the optimum fault obtained by the grid search. The planar fault is divided into subfaults with size 3 km \( \times \) 3 km. We then simulate the Green’s function, i.e., the pressure change waveforms excited by each subfault, using a similar calculation procedure to that used in the grid-search analysis. The inversion scheme is almost the same as the tsunami source inversion analysis, but we imposed a nonnegativity constraint (Lawson & Hanson, 1974). The weighting of the smoothing constraint is determined by trial and error.

The slip distribution obtained by the inversion analysis and the tsunami source distribution calculated from this slip distribution are shown in Figure 8a. The tsunami source distribution is similar to that obtained by the tsunami source inversion (Figure 4).
The S-net and other tsunamis waveforms are well explained (VR = 72.4%, Figures S4b, S4c, and S5). We obtain a maximum slip of $D_{\text{max}} = 637.2$ cm, and the total seismic moment is $M_0 = 6.3 \times 10^{19}$ Nm ($M_w 7.1, \mu = 30$ GPa). The large slip is concentrated in the northeastern part of the fault plane, corresponding to the rectangular fault estimated by the grid-search analysis. More specifically, subfaults with slip amounts with $D > 0.5 \times D_{\text{max}}$ roughly correspond to the rectangular fault (subfaults marked by green lines in Figure 8a, 41% of the total $M_0, M_w 6.9$). In addition, a relatively small slip also extends to the southwestern part, which was not resolved in the grid-search analysis. The reason why this slip was not resolved in the grid search is probably the simple assumption of the uniform slip rectangular fault. If we take subfaults with slip amounts larger than $0.2 \times D_{\text{max}}$, then both large northeastern slip and relatively small southwestern slip are included (indicated by the thick black lines in Figure 8). Thus, we define these subfaults as the rupture area. The rupture area had dimensions of $\sim 30$ km $\times$ $\sim 20$ km, and 81% of the total moment was concentrated in the main rupture area. The horizontal location of the centroid, defined as the slip-weighted average of subfaults within the rupture area (pink star in Figure 8a, Table 1), is located $\sim 5$ km southeast from the GCMT centroid.

Figure 8. Result of the slip inversion. (a) Slip distribution (colored tiles) and tsunami source distribution (black contours, 20 cm interval). The pink and white stars indicate the slip-weighted averaged centroid and the JMA epicenter, respectively. Subfaults with slip amounts larger than $0.2 \times D_{\text{max}}$ and larger than $0.5 \times D_{\text{max}}$ are marked by thick black lines and green lines, respectively. (b) Shear stress change along the fault. Negative (blue) and positive (red) denote...
the shear stress decrease and increase, respectively. The dark red rectangle denotes the optimum rectangular fault obtained by the grid-search analysis.

In Figure 8b, we calculate the distribution of the shear stress change along the fault, using the equation of Okada (1992). The rectangular fault estimated by the grid-search analysis agrees well with the region where the shear stress is largely released (green rectangle in Figure 8b), indicating that the rectangular fault model corresponds to the asperity, as discussed above. Using the shear stress change distribution, we calculate the energy-based stress drop $\Delta \sigma_E$ (Noda et al., 2013) as:

$$\Delta \sigma_E = \frac{\sum_i D_i \Delta \sigma_i}{\sum_i D_i},$$

where $D_i$ is the slip amount at the $i$-th subfault, and $\Delta \sigma_i$ is the stress drop at the $i$-th fault, which is defined as the shear stress change (Figure 8b) multiplied by $-1$. Using the subfaults within the rupture area, we obtain $\Delta \sigma_E = 10.0$ MPa. This stress drop seems not so small as expected for the interplate earthquakes (an order of $\sim 10^0$ MPa, e.g., Kanamori & Anderson 1975), but rather is consistent with the intraplate earthquakes, which generally have stress drop values of $\sim 10^1$ MPa (e.g., Somerville et al., 1999; Miyakoshi et al., 2020).

6. Discussion: implication for the intraplate stress regime

After the 2011 Tohoku earthquake, it has been reported that the normal-faulting seismicity significantly increased in the upper plate, which is thought to be related to the stress perturbation by the Tohoku earthquake (Figures 1d–1f, Asano et al., 2011; Hasegawa et al., 2012; Yoshida et al., 2012). The 2016 off-Fukushima earthquake is also considered to be an event of the normal-faulting seismicity related to the stress perturbation by the Tohoku earthquake. This change in seismicity is interpreted as the result whereby the intraplate stress regime switched after the Tohoku earthquake from the horizontal compression to the horizontal extension (e.g., Hasegawa et al. 2012). As discussed previously, the use of the S-net tsunami data
improved the constraint on the tsunami source and the fault model of the off-Fukushima earthquake, which made it possible to obtain the detailed distribution of the shear stress reduction and the static stress drop. Using these results, we attempt to discuss the quantitative relationship between the crustal stress released during the off-Fukushima earthquake and the stress increase due to the 2011 Tohoku earthquake. This kind of discussion is typically difficult to conduct because it is rare that both the high-resolution fault model of the M~7 offshore earthquake and the significant stress perturbation due to the megathrust earthquake are available.

If the stress regime switched by the Tohoku earthquake in the vicinity of the off-Fukushima earthquake, the deviatoric stress, or the initial shear stress on the fault of the off-Fukushima earthquake, should be smaller than (or at least equivalent to) the static shear stress increase due to the Tohoku earthquake (Figure 9a). In other words, the stress drop of the off-Fukushima earthquake should be smaller than the shear stress increase due to the Tohoku earthquake. In Figure 10a, we calculate the shear stress change due to the Tohoku earthquake, using the fault model of Iinuma et al. (2012), along the fault geometry of the off-Fukushima earthquake. The shear stress change related to the Tohoku earthquake around the focal area of the off-Fukushima earthquake is only ~2 MPa, which is smaller than the stress drop of the off-Fukushima earthquake. The larger stress drop of the off-Fukushima earthquake than the stress increase after the Tohoku earthquake is inconsistent with the presumption that the intraplate stress regime switched by the static stress change of the Tohoku earthquake. There should be other causes for the normal-faulting stress regime around the focal area of the off-Fukushima earthquake.
Figure 9. Schematic illustration of the temporal change of the stress regime around the off-Fukushima earthquake. The stress regimes (a) assuming the switching of the stress regime after the Tohoku earthquake and (b) without assuming the stress switching.

Figure 10. Horizontal distribution of the shear stress change on the 2016 off-Fukushima earthquake fault at a depth of 10 km. Shear stress changes along the fault geometry of the off-Fukushima earthquake due to (a) the Tohoku earthquake (Iinuma et al. 2012), (b) postseismic slip during April 2011 and December 2011 (Iinuma et al., 2016), and (c) Postseismic slip during September 2012 and September 2016 (Tomita et al. 2020). The main rupture area of the 2016
One possible cause is the postseismic slip of the Tohoku earthquake (Iinuma et al., 2016; Tomita et al., 2020). After the Tohoku earthquake, the postseismic seafloor deformation was detected by the seafloor geodetic observation (Tomita et al., 2015; 2017), which was caused by the postseismic slip along the fault and the viscoelastic deformation (Sun et al., 2014; Iinuma et al., 2016; Tomita et al., 2020). Among the postseismic deformation, the afterslip along the plate interface is dominant in the south of the rupture area of the Tohoku earthquake, including the region off Fukushima, whereas the viscoelastic deformation dominates the northern part of the Tohoku earthquake rupture area (Iinuma et al., 2016; Tomita et al., 2020). Therefore, we calculate the shear stress change on the 2016 fault geometry using the postseismic slip models to evaluate the contribution by the postseismic slip around the focal area. We calculate the stress change using the postseismic slip model from 23 April 2011 to 10 December 2011 proposed by Iinuma et al. (2016) (Figure 10b). The calculated shear stress change is too small (on the order of $10^{-1}$ hPa) to complement the shortage of the stress change of the off-Fukushima earthquake. We also calculated the stress change using the postseismic slip model during 2012 and 2016 (Tomita et al., 2020) and found that its contribution was also minor (Figure 10c). We therefore concluded that the shear stress increase due to the postseismic slip could not resolve the apparent contradiction between the stress drop of the off-Fukushima earthquake and the shear stress increase after the Tohoku earthquake. This contradiction arose from the assumption of the switching of the stress regime, which was a reverse-faulting and a normal-faulting regime before and after the Tohoku earthquake, respectively.

It was thought that the horizontal compressive stress attributed to the plate coupling force was widely dominant in Japan before the Tohoku earthquake (e.g., Wang & Suyehiro, 1999; Terakawa & Matsu’ura, 2010). However, there are some recent reports that some normal-faulting microearthquakes occurred even before the Tohoku earthquake in the inland region of Fukushima prefecture (Imanishi et al., 2012; Yoshida et al., 2015a; 2015b). This normal-faulting seismicity was interpreted as a result of the normal-faulting stress regime being predominant in this location even before the Tohoku earthquake. One possible reason for this normal-faulting stress regime is the effect of bending of the overriding plate, in which the horizontal extensional
and compressional stresses develop at the shallower and the deeper portion of the plate, respectively (e.g., Turcotte & Schubert, 2002; Hashimoto & Matsu’ura, 2006; Fukahata & Matsu’ura, 2016). Yoshida et al. (2015a) showed that the normal-faulting stress regime is dominant at depths shallower than ~15 km in this region, while the reverse-faulting stress regime is dominant at depths greater than ~15 km, which is consistent with the hypothesis. We can also consider the topographic effects (Wang et al., 2019) for the formation of the horizontal extensional stress. Taking these past studies into account, it is reasonable to interpret this apparent contradiction, in which the stress perturbation by the Tohoku earthquake around the off-Fukushima earthquake is insufficient to switch the intraplate stress regime, that the horizontal extensional stress regime was already predominant around the 2016 off-Fukushima earthquake even before the Tohoku earthquake (Figure 9b).

Some major normal-faulting earthquakes were reported around the focal area of the off-Fukushima earthquake in 1938 (Abe, 1977; Murotani, 2018). Furthermore, according to the geologic cross-section around the off-Iwaki gas field, which is located near the 2016 off-Fukushima earthquake, the northeast-southwest-trending reverse faults were developed at a depth shallower than 6 km, which are considered to have formed during Oligocene and Miocene (Iwata et al., 2002). Along this fault trace, it was also reported that the normal-faulting-type surface offsets with vertical offset of 5–10 m were found, and it was suggested that the direction of the tectonic stress flipped to the normal-faulting regime during Quaternary and a normal-faulting earthquake similar to the 2016 off-Fukushima earthquake repeatedly occurred along this fault (S. Toda, https://irides.tohoku.ac.jp/media/files/earthquake/eq/2016_fukushima_eq/20161122_fukushima_eq_activefault_toda.pdf, in Japanese). These reports may support our hypothesis that the crustal stress regime was under the normal-faulting regime even before the Tohoku earthquake.

Note that the downdip limit of the main rupture area of our fault model the off-Fukushima earthquake is ~14 km, which is approximately consistent with the downdip limit depth of the normal-faulting regime in the inland Fukushima region estimated by Yoshida et al. (2015a). This suggests that the horizontal extensional stress regime before the Tohoku earthquake around the focal area of the off-Fukushima earthquake is predominant at depths shallower than 15 km and the stress neutral zone related to bending of the overriding plate lies at a depth of ~15 km. We also note that the normal-faulting seismicity extensively increased in the
overriding plate, even at a depth deeper than 15 km (e.g., Asano et al., 2011; Hasegawa et al., 2012). This might suggest that the stress-neutral depth was slightly deepened around this region after the Tohoku earthquake.

As a summary of this discussion, the temporal change of the intraplate crustal stress around the off-Fukushima earthquake can be interpreted as follows. The horizontal extensional stress was predominant before the Tohoku earthquake within the shallowest part of the continental plate, but may not exceed the crustal strength. After the Tohoku earthquake, its stress perturbation enhanced the extensional stress, provoking the normal-faulting seismicity.

Before the 2011 Tohoku earthquake, no major seismicity was detected around the focal area of the off-Fukushima earthquake (e.g., Asano et al., 2011; Hasegawa et al., 2012) and the onshore seismic network could not detect micro-seismicity around this offshore region. On the other hand, the use of the S-net OBPGs could well constrain the fault modeling of the 2016 off-Fukushima earthquake, which provides an important implication for the crustal stress regime prior to the Tohoku earthquake, even though the S-net was not installed at that time. Such information about the stress regime is important to understand the spatio-temporal change of the intraplate stress state and the generation mechanisms of the intraplate earthquake, especially after a large megathrust earthquake. Our analysis demonstrated that the analysis of the offshore S-net data provided implications for the crustal stress regime at the offshore region, which was difficult to discuss before the S-net was available. Although the S-net OBPG data contains the tsunami-irrelevant pressure change signals, careful analysis of this data significantly improves the constraint of the fault model and will deepen our understanding of the earthquake generation.

7 Conclusions

We examined the S-net tsunami data associated with the off-Fukushima earthquake on 21 November 2016 ($M_w$ 7.1). We first processed the S-net OBPG data and found some pressure signals irrelevant to tsunami were observed: (1) an extremely large drift component and (2) an abrupt pressure step around the origin time. We discussed the cause of these tsunami-irrelevant signals and concluded that these signals were not due to the pressure sensors themselves but probably due to the observation system. We then analyzed the S-net data in order to estimate the tsunami source model and the fault model. Careful analysis of the S-net OBPG data provided the tsunami source distribution, which had a large subsidence with strike angle consistent with the
GCMT solution. Our fault model suggested that the energy-based stress drop of the off-Fukushima earthquake is \( \Delta \sigma_E \approx 10 \text{ MPa} \). The quantitative comparison between the stress drop and the static stress changes caused by the 2011 Tohoku earthquake and its postseismic slip suggested that the additional source of the horizontal extensional stress is necessary to explain the stress drop. We interpreted the stress regime around the off-Fukushima earthquake to be the horizontal extensional even before the Tohoku earthquake, related to the bending of the overriding plate. The S-net pressure data is very useful to constrain the tsunami source model and the finite fault model, even if the model is perturbed by the tsunami-irrelevant signals, which provided an important implication for the tectonic stress regime within the overriding plate.

**Data Availability Statement**

The S-net OBPG data are available from the website of the National Research Institute for Earth Science and Disaster Resilience [NIED] (NIED, 2019, https://doi.org/10.17598/NIED.0007). The NOWPHAS tsunami data is provided upon request to the Port and Airport Research Institute (PARI). The data of the OBPGs installed by ERI was provided upon request to ERI, the University of Tokyo. The OBPG data of Tohoku University was provided upon request to Ryota Hino of Tohoku University. Station locations of the S-net OBPG are available at https://www.seafloor.bosai.go.jp/st_info/. The location of the OBPGs installed by ERI is available in Gusman et al. (2017). The locations of the NOWPHAS GPS buoys and wave gauges are available at https://nowphas.mlit.go.jp/pastdata/. The locations of the OBPGs installed by Tohoku University are listed in Table S2.

We purchased the JTOPO30v2 bathymetry data from the Marine Information Research Center (http://www.mirc.jha.jp/en/) of the Japan Hydrographic Association. The plate boundary model in Figure 1 (Nakajima & Hasegawa, 2006) is available from the website of Fuyuki Hirose (https://www.mri-jma.go.jp/Dep/sei/fhirose/plate/PlateData.html, in Japanese, accessed on 1 April, 2021). The rotation data of the S-net sensor (Takagi et al., 2019) was provided by Ryota Takagi. The slip models of the mainshock and postseismic slip of Inoue et al. (2012; 2016) and Tomita et al. (2020) were provided by Takeshi Inoue and Fumiaki Tomita. The slip distribution models of Gusman et al. (2017), Adriano et al. (2018), and Nakata et al. (2019) are available in each paper. The location of the seafloor bathymetry survey conducted by the Japan Agency for Marine-Earth Science and Technology [JAMSTEC] (blue triangles in
Figure 4a) was taken from http://www.jamstec.go.jp/ceat/j/topics/20161208.html, http://www.jamstec.go.jp/j/about/press_release/20170301/ (in Japanese).

Acknowledgments

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References


Kubota, T., Saito, T., Chikasada, N. Y., & Suzuki, W. (2020). Ultrabroadband seismic and tsunami wave observation of high-sampling ocean-bottom pressure gauge covering...


Table 1. Fault parameters for the rectangular fault models.

<table>
<thead>
<tr>
<th>Models</th>
<th>Fault center location</th>
<th></th>
<th></th>
<th>$M_0$ [Nm]</th>
<th>Maximum vertical displacement [cm]</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>Longitude [°E]</td>
<td>Latitude [°N]</td>
<td>Depth [km]$^a$</td>
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<td>Uplift</td>
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<td>GCMT solution</td>
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<td>37.31</td>
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<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
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</tr>
<tr>
<td>Grid-search$^{ab}$</td>
<td>141.5165</td>
<td>37.3105</td>
<td>6.0</td>
<td>2.10 $\times 10^{19}$</td>
<td>16.0</td>
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<tr>
<td>Slip distribution$^a$</td>
<td>141.4908$^c$</td>
<td>37.2630$^c$</td>
<td>7.7$^c$</td>
<td>6.30 $\times 10^{19}$</td>
<td>10.5</td>
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<td>Gusman et al. (2017)</td>
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<td>N/A</td>
<td>N/A</td>
<td>3.70 $\times 10^{19}$</td>
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<td>Adriano et al. (2018)</td>
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<td>N/A</td>
<td>N/A</td>
<td>3.35 $\times 10^{19}$</td>
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<td>Nakata et al. (2019)</td>
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<td>N/A</td>
<td>N/A</td>
<td>8.52 $\times 10^{19}$</td>
<td>29.7</td>
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</table>

$^a$Fault geometry is fixed to the GCMT value; strike = 49°, dip = 35°, rake = −89°.

$^b$Fault dimension is $L = 15$ km, $W = 10$ km, and slip amount is $D = 467.7$ cm. The depths of the fault top and bottom are 3.1 km and 8.9 km, respectively.

$^c$Slip-weighted average location is shown.
Supporting Information for

Improving the constraint on the $M_w$ 7.1 2016 off-Fukushima shallow normal-faulting earthquake with the high azimuthal coverage tsunami data from the S-net wide and dense network: Implication for the stress regime in the Tohoku overriding plate

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Contents of this file

Text S1
Figures S1 to S5
Tables S1 to S2

Introduction

Text S1 explains the procedure for the inversion analysis. Figure S1 shows the trade-off curve used to determine the weight of the smoothing constraint. Figure S2 is the result of the tsunami source inversion using the pressure waveforms. Figure S3 is the result of the grid-search analysis. The forward simulation of the tsunami waveforms based on the finite fault model is shown in Figures S4 and S5. Table S1 shows the unknown parameters searched in the grid-search analysis. The station locations of the OBPGs installed by Tohoku University are listed in Table S2.
Text S1

This text explains the procedure for the tsunami source modeling shown in Section 4. We first explain how to simulate the tsunami Green’s function, which are the pressure change waveforms due to the tsunami and seafloor displacement at each OBPG caused by the displacement of the small region of seafloor. We distribute the small elements of the seafloor uplift (unit source elements) around the focal area (rectangular area in Figure 4a). The unit source element of the seafloor vertical displacement is given by

\[
 u_{ij}(x, y) = u_0 \left[ \frac{1}{2} + \frac{1}{2} \cos \left( \frac{2\pi (x-x_i)}{L_x} \right) \right] \left[ \frac{1}{2} + \frac{1}{2} \cos \left( \frac{2\pi (y-y_j)}{L_y} \right) \right]
\]

for \( x_i - \frac{L_x}{2} \leq x \leq x_i + \frac{L_x}{2}, \ y_j - \frac{L_y}{2} \leq y \leq y_j + \frac{L_y}{2}, \) \hspace{1cm} (S1)

which takes the maximum value of \( u_0 = 1 \text{ cm} \) at \((x, y)\). Here, \( L_x \) and \( L_y \) are the spatial extent of the unit source element along the \( x \)- and \( y \)-directions, respectively. We assume that \( L_x = L_y = 4 \text{ km} \). Each of the unit sources overlaps with adjacent unit sources with a horizontal interval of \( \Delta L_x = L_x/2 \) and \( \Delta L_y = L_y/2 \). The numbers of unit sources along the \( x \)-direction and \( y \)-directions are \( N_x = 25 \) and \( N_y = 25 \), respectively, and the total number of unit sources is \( N = N_x \times N_y = 625 \). The size of the analytical area where the unit sources are distributed is \( 50 \text{ km} \times 50 \text{ km} \).

Using the seafloor vertical displacement from the unit sources, we calculate tsunamis using the following procedure. We assume the initial sea-surface height change assuming that the sea-surface displacement is equal to the seafloor displacement. We then solve the linear dispersive tsunami equation (Saito et al., 2010; Saito, 2019) in Cartesian coordinates with the staggered grid in order to simulate tsunamis:

\[
 \frac{\partial M}{\partial t} + g h \frac{\partial \eta}{\partial x} = \frac{1}{3} h^2 \left( \frac{\partial^2 M}{\partial x^2} + \frac{\partial^2 N}{\partial y^2} \right)
\]

\[
 \frac{\partial N}{\partial t} + g h \frac{\partial \eta}{\partial y} = \frac{1}{3} h^2 \left( \frac{\partial^2 M}{\partial y^2} + \frac{\partial^2 N}{\partial y^2} \right),
\]

\[
 \frac{\partial \eta}{\partial t} = - \frac{\partial M}{\partial x} - \frac{\partial N}{\partial y}
\]

where the variable \( \eta \) is the sea surface height anomaly (tsunami height), \( M \) and \( N \) are the velocity components integrated along the vertical direction over the seawater depth, \( h \) is the water depth, and \( g \) is the gravitational constant. For water depth \( h \), we use the JTOPO30 data with a spatial resolution of 30 arcsec, provided by the Marine Information Research Center of the Japan Hydrographic Association (http://www.mirc.jha.jp/en/), interpolating the spatial interval of \( \Delta x = \Delta y = 1 \text{ km} \). We assume that the displacement occurs instantaneously, at time \( t = 0 \text{ s} \). The temporal interval of the calculation is \( \Delta t = 1 \text{ s} \). After the calculation, we subtract the pressure offset change due to the seafloor displacement (Tsushima et al., 2012), assuming that a seawater column height change of \( 1 \text{ cm} \) \( \text{H}_2\text{O} \) is equal to a pressure change of \( 1 \text{ hPa} \). We finally apply the same bandpass filter to the simulated waveform as that applied to the observation.

In order to estimate the tsunami source, we use the time-derivative waveforms of the bandpass-filtered pressure waveforms for the inversion analysis \( (\partial p/\partial t, \text{Figure 4c}) \), because the time-derivative of the step signal becomes the impulse signal and thus does not contain the offset change, which can reduce the artificials due to the tsunami-irrelevant steps (Kubota, Suzuki et al., 2018). The data time window used for the modeling, which includes the main part of the tsunami (indicated by the blue traces in Figure 4c), is manually determined. We solve the following observation equation:
\[
\begin{pmatrix}
\mathbf{d} \\
\mathbf{0}
\end{pmatrix} = \begin{pmatrix}
\mathbf{H} \\
\alpha \mathbf{S}
\end{pmatrix} \mathbf{m}
\] (53)

The data vector \( \mathbf{d} \) consists of the time-derivative waveforms of the observed pressure \( \partial p / \partial t \), and the matrix \( \mathbf{H} \) consists of the time-derivative of the tsunami Green’s functions. The vector \( \mathbf{m} \) consists of the amounts of the displacement of the unit sources, which are the unknown parameters to be solved. The matrix \( \mathbf{S} \) indicates the constraint for the spatial smoothing (e.g., Baba et al., 2006) and the parameter \( \alpha \) is its weight. The goodness of the estimated source is evaluated using the variance reduction (VR):

\[
VR = \left(1 - \frac{\sum_i (d_i^{\text{obs}} - d_i^{\text{cal}})^2}{\sum_i d_i^{\text{obs}}^2}\right) \times 100 \% \quad (54)
\]

where \( d_i^{\text{obs}} \) and \( d_i^{\text{cal}} \) are the \( i \)-th data of the observed and calculated time-derivative pressure waveforms, respectively. The smoothing weight \( \alpha \) is determined based on the trade-off between the weight and the VR (Figure S1) in order to avoid both the overfitting and oversmoothing of data.
Figure S1. Trade-off curve between the smoothing weight $\alpha$ and VR. Red and blue solid lines are the trade-off curves for the inversions using the time-derivative waveform of the pressure (Figure 4) and the pressure waveform (Figure S2), respectively. Dashed lines denote the weight values used for the inversion analyses.
Figure S2. Results of the tsunami source inversion based on the conventional method. See Figure 4 for another explanation of this figure.
**Figure S3.** Results of the grid-search analysis. (a) Spatial distribution of the tsunami source. The green rectangle shows the location of the rectangular fault model. Comparisons of (b) the pressure waveforms and (c) the time-derivative waveforms. See Figure 4 for a detailed explanation of the figure.
Figure S4. Results of the slip inversion. (a) Spatial distribution of the tsunami source calculated from the slip distribution in Figure 8a. Comparisons of (b) the pressure waveforms and (c) the time-derivative waveforms. See Figure 4 for a detailed explanation of the figure.
Figure S5. Waveform comparisons for the other tsunami stations from the finite fault model for (a) NOWPHAS Near-coastal GPS buoys, (b) NOWPHAS wave gauges, (c) OBPGs installed by ERI, and (d) OBPGs installed by Tohoku University. See Figure 1 for station locations.
Table S1. Search range for the grid search analysis.

<table>
<thead>
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<th>Parameters</th>
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<th>Increment</th>
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<tr>
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</tr>
<tr>
<td>Latitude (^a)</td>
<td>37.31°N ± 20 km</td>
<td>5 km</td>
</tr>
<tr>
<td>Depth (^a)</td>
<td>12.0 km ± 10 km (^a)</td>
<td>2 km</td>
</tr>
<tr>
<td>Strike (^a)</td>
<td>49°</td>
<td>Fixed</td>
</tr>
<tr>
<td>Dip (^a)</td>
<td>35°</td>
<td>Fixed</td>
</tr>
<tr>
<td>Rake (^a)</td>
<td>−89°</td>
<td>Fixed</td>
</tr>
<tr>
<td>Length (^c)</td>
<td>5 km – 60 km</td>
<td>5 km</td>
</tr>
<tr>
<td>Width (^c)</td>
<td>5 km – 60 km</td>
<td>5 km</td>
</tr>
<tr>
<td>Slip amount</td>
<td>Adjusted so that the VR value takes the maximum</td>
<td></td>
</tr>
</tbody>
</table>

\(^a\)Reference values are taken from the GCMT solution.
\(^b\)Fault center location is shown.
\(^c\)When the depth of the updip end of the fault is shallower than a depth of 0.1 km, the calculation is skipped.

Table S2. Station list of the OBPGs installed by Tohoku University

<table>
<thead>
<tr>
<th>Station</th>
<th>Longitude (°E)</th>
<th>Latitude (°N)</th>
<th>Depth (m)</th>
<th>Observation duration (yyyy/mm/dd)</th>
<th>Logger type(^a)</th>
</tr>
</thead>
<tbody>
<tr>
<td>G01</td>
<td>144.9204</td>
<td>38.7030</td>
<td>5456</td>
<td>2016/05/22 – 2017/04/11</td>
<td>UME</td>
</tr>
<tr>
<td>G12</td>
<td>143.5317</td>
<td>38.0213</td>
<td>4366</td>
<td>2016/05/24 – 2017/04/10</td>
<td>UME</td>
</tr>
<tr>
<td>G16</td>
<td>143.0470</td>
<td>37.3324</td>
<td>4414</td>
<td>2016/05/27 – 2017/04/15</td>
<td>HAK</td>
</tr>
<tr>
<td>G17(^b)</td>
<td>142.7123</td>
<td>36.8979</td>
<td>4232</td>
<td>2016/05/28 – 2017/04/09</td>
<td>HAK</td>
</tr>
<tr>
<td>G19</td>
<td>142.6735</td>
<td>36.4931</td>
<td>5691</td>
<td>2016/05/28 – 2017/04/09</td>
<td>HAK</td>
</tr>
<tr>
<td>AoA60(^b)</td>
<td>142.7140</td>
<td>36.8993</td>
<td>4225</td>
<td>2016/09/22 – 2017/10/15</td>
<td>UME</td>
</tr>
<tr>
<td>AoA70</td>
<td>142.2868</td>
<td>36.6937</td>
<td>2544</td>
<td>2016/09/22 – 2017/10/15</td>
<td>HAK</td>
</tr>
<tr>
<td>FKOB1</td>
<td>142.5800</td>
<td>36.8055</td>
<td>4550</td>
<td>2016/09/28 – 2017/10/15</td>
<td>UME</td>
</tr>
<tr>
<td>FKOB2</td>
<td>142.8553</td>
<td>36.7225</td>
<td>5506</td>
<td>2016/09/28 – 2017/10/14</td>
<td>HAK</td>
</tr>
<tr>
<td>G15</td>
<td>143.5215</td>
<td>37.6773</td>
<td>5239</td>
<td>2016/10/02 – 2017/10/19</td>
<td>UME</td>
</tr>
</tbody>
</table>

\(^a\)UME: Paroscientific Series 8CB intelligent type pressure sensor + Umezawa-Musen Co. data logger, HAK: Paroscientific Series 8B pressure sensor + Hakusan Co. LS9150 data logger
\(^b\)Station G17 and AoA60 are installed at almost identical location.