Detecting Discontinuities from in-Situ Space Measurements: Method and FPGA Implementation

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Abstract

The analysis in real time of space data variability is essential for scientists and space mission controllers. Automated tools designed to extract key descriptors of variability are needed and solutions to adapt such algorithms for on-board computers are rare. This paper describes the design of an automated system for detecting directional discontinuities of a physical quantity and its implementation in Field-Programmable Gate Array (FPGA). The system is currently adapted for solar wind or terrestrial magnetosheath magnetic field directional discontinuities, i.e. sharp changes of the magnetic field directionality. Our detection algorithm uses analysis windows of adjustable width and averaging procedures in order to reduce the effects of random fluctuations. A sliding-window approach is designed for continuous monitoring and detection of magnetic directional discontinuities. A software implementation of the algorithm was tested using in-situ magnetic field measurements, and emphasised improvements of performance when using analysis windows of adjustable width. The FPGA implementation of the detection algorithm is built on DILIGENT Nexys 4 DDR featuring a commercial Xilinx Artix-7 device and is designed to be ported to space qualified infrastructure. The FPGA system was tested with synthetic and laboratory signals, and provides results in very good agreement with the software implementation. The FPGA system provides an efficient real-time monitoring solution using minimal computational and energy resources, and reducing the main on-board computer utilization.
Detecting Discontinuities from in-Situ Space Measurements:
Method and FPGA Implementation

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Key Points:

- We designed an algorithm to detect directional discontinuities from in-situ space measurements, suitable for automated application
- A Field-Programmable Gate Array (FPGA) implementation of the algorithm, designed to be adapted for on-board operations, is provided
- Tests with laboratory and space measurements of the FPGA and software implementations of the detection algorithm, give excellent results

Abstract

The analysis in real time of space data variability is essential for scientists and space mission controllers. Automated tools designed to extract key descriptors of variability are needed and solutions to adapt such algorithms for on-board computers are rare. This paper describes the design of an automated system for detecting directional discontinuities of a physical quantity and its implementation in Field-Programmable Gate Array (FPGA). The system is currently adapted for solar wind or terrestrial magnetosheath magnetic field directional discontinuities, i.e. sharp changes of the magnetic field directionality. Our detection algorithm uses analysis windows of adjustable width and averaging procedures in order to reduce the effects of random fluctuations. A sliding-window approach is designed for continuous monitoring and detection of magnetic directional discontinuities. A software implementation of the algorithm was tested using in-situ magnetic field measurements, and emphasised improvements of performance when using analysis windows of adjustable width. The FPGA implementation of the detection algorithm is built on DILIGENT Nexys 4 DDR featuring a comercial Xilinx Artix-7 device and is designed to be ported to space qualified infrastructure. The FPGA system was tested with synthetic and laboratory signals, and provides results in very good agreement with the software implementation. The FPGA system provides an efficient real-time monitoring solution using minimal computational and energy resources, and reducing the main on-board computer utilization.
1 Introduction

A clear understanding of data variability recorded in space is vital for scientists and space mission controllers. Consequently, automatic tools designed to extract relevant key-descriptors of variability are extremely useful. Nevertheless, solutions to adapt such algorithms for on-board computers are still rare. In this paper we describe an algorithm that detects directional discontinuities of in-situ measured variables, and its implementation on Field-Programmable Gate Array (FPGA) devices with an application on directional discontinuities of the interplanetary magnetic field (IMF).

The abrupt changes in the orientation of the IMF, referred to as directional discontinuities (DDs), are known to trigger geomagnetic storms and substorms, with significant impact on ground-based and spaceborne technologies. DDs are important when estimating the solar wind propagation time from an upstream solar wind monitor to a downstream target (e.g., Mailyan et al., 2008; Haaland et al., 2010; Munteanu et al., 2013). IMF discontinuities play a key role in understanding the micro-scale structure of the solar wind. With an average occurrence rate of one or two per hour, IMF discontinuities are abundant structures in the solar wind (e.g., Newman et al., 2020) and represent an omnipresent source of variability for the terrestrial plasma environment.

Two general classes of idealized Magnetohydrodynamic (MHD) discontinuities can be distinguished: stationary structures, i.e. discontinuities that do not propagate with respect to the ambient plasma (tangential discontinuities (TDs) and contact discontinuities), and propagating discontinuities (rotational discontinuities (RDs) and shocks). The most frequent small-scale discontinuities in the interplanetary space are the abrupt changes in the direction of the magnetic field, predominantly expected for TDs and RDs (e.g., Paschmann et al., 2013).

Two main classes of algorithms to detect solar wind discontinuities are proposed in the literature. The first class includes algorithms searching for changes in the magnetic field direction (Burlaga, 1969; Lepping and Behannon, 1986; Li, 2008; Borovsky, 2008, 2010; Miao et al., 2011; Perri et al., 2012; Zhdankin et al., 2012 a, b); the second class includes algorithms searching for changes in the amplitudes of the magnetic field components and/or magnitude (Tsurutani and Smith, 1979; Vasquez et al., 2007; Greco et al., 2008; Greco and Perri, 2014; Greco et al., 2016, 2018).

The term “directional discontinuity” was originally introduced by Burlaga (1969) to denote a variation of solar wind magnetic field direction larger than 30 degrees in less than 30 seconds. Since then, this definition was used in many variant algorithms. Li (2008) developed an algorithm to identifying discontinuities based on this definition. Borovsky (2010) studied the spectral effects of solar wind DDs detected using the definition above. Chian and Munoz (2011) used the Li (2008) detection method to study the relation between discontinuities, turbulence, and magnetic reconnections at the leading edge of an interplanetary coronal mass ejection. Miao et al. (2011) further developed the algorithm by Li (2008) and introduced a way of determining the discontinuity thickness.

Vasquez et al. (2007) developed an original detection algorithm which is independent of the directional changes, but relies on changes in the amplitude of the magnetic field components. They found that the daily occurrence rate of strong solar wind discontinuities obtained with their original detection algorithm is comparable with the daily occurrence rate obtained using an algorithm based on directional changes. Tsurutani and Smith (1979) also showed that the method
used by Burlaga (1969) provides similar results to their method based on changes of the amplitude of field components. Burkholder and Otto (2019) describe yet another original detection algorithm based on changes of the amplitude of field components.

Due to various computational difficulties encountered when implementing automated detection methods, even very recent studies still use visual inspection to identify discontinuities (Mailyan et al., 2008; Munteanu et al., 2013; Artemyev et al., 2018, 2019 a, b). Note that the automated detection algorithm of Burkholder and Otto (2019) still uses visual inspection to eliminate events that are not isolated from other structures in the time series. For datasets of only a few hundred events/discontinuities, the detection by visual inspection can be an acceptable option, but, for large-scale statistical studies, visual inspection-based methods are certainly not suitable.

In this study we designed and implemented an original algorithm based on the principles described by Li (2008) (see also Borovsky, 2008). We adopt a discontinuity detection algorithm based on directional changes because: (i) traditionally, angular changes were the preferred detection method (Burlaga, 1969), which renders our approach compatible with previous ones; (ii) many authors have recently started to use angular changes in order to improve results from algorithms based on amplitude changes of the field components (e.g., Greco et al., 2018), (iii) it is an efficient and less complex approach, thus computationally less intensive and hence less power consuming compared to most algorithms based on amplitude changes of the field components. Since we aim to provide a hardware implementation of our algorithm, the directional changes approach leads to a more reliable and robust FPGA implementation. (iv) In many cases, the two approaches are equivalent, especially for discontinuities with rotation angles larger than 30° (e.g., Greco et al., 2018).

State of the art space plasma instruments on-board recent terrestrial or interplanetary missions, e.g., MMS (Burch et al., 2016) and Parker Solar Probe (Fox et al., 2016), provide high time-resolution in-situ measurements, while being constrained by limited telemetry possibilities. Thus, the on-board implementation of computations is critical for taking advantage of the full set of collected data. The on-board discontinuity detector would allow for the computation of magnetic field rotation angles from high-resolution measurements without downloading the entire dataset. The on-board computed angular changes can also be used to identify interesting events and activate triggers for temporary on-board storage and subsequent download of high-resolution data (selective downlink).

Most of the algorithms discussed above are capable of automatically detecting IMF directional discontinuities, but they were designed only for on-ground data analysis. To our knowledge, no other algorithm was designed to be implemented in an FPGA device. This study is part of a broader effort devoted to building a complex semi-autonomous digital signal processing library, able to apply on-board various digital signal processing techniques. The current version of the library already includes modules devoted for the spectral and statistical analysis of fluctuations (Deak et al., 2018; Opincariu et al., 2019; Deak et al., 2021; Turicu et al., 2022). Here we discuss a new feature, allowing to detect directional discontinuities.

The paper is structured as follows. Section 2 provides a theoretical background and a conceptual description of the discontinuity detection algorithm. It also discusses reconfigurable FPGA devices in the context of on-board data processing. Section 3 gives an overview of the system and describes the FPGA implementation of the discontinuity detection algorithm. Section
4 presents the main tests and validation procedures of both the algorithm and its FPGA implementation; the section shows results obtained using synthetic datasets, laboratory magnetic field measurements, and also in-situ interplanetary magnetic field measurements. Section 5 provides a summary and perspective.

2 Theoretical background

2.1 Directional discontinuity detection algorithm for automatic use

Let us consider a set of in-situ measurements of a plasma or field variable. Take, for instance, the triaxial measurements of the interplanetary magnetic field, $B_x$, $B_y$, and $B_z$, in an arbitrary reference system. Magnetic directional discontinuities observed in interplanetary space and in the terrestrial magnetosheath are characterized by sharp changes in the direction of the magnetic field vector $\mathbf{B} = [B_x B_y B_z]$. Magnetic directional changes are computed as:

$$\varphi(t_k) = \left(\frac{180}{\pi}\right) \cos^{-1}\left(\frac{B_1 B_2}{|B_1||B_2|}\right)$$ (1)

where $\varphi$ (in degrees) is computed at time $t_k$, and $B_1$ and $B_2$ are defined as:

$$B_1 = \langle B \rangle_{\tau_1} = \left\langle \left[ \begin{array}{c} B_x \\ B_y \\ B_z \end{array} \right] \right\rangle_{\tau_1}$$

$$B_2 = \langle B \rangle_{\tau_2} = \left\langle \left[ \begin{array}{c} B_x \\ B_y \\ B_z \end{array} \right] \right\rangle_{\tau_2}$$ (2)

with the symbol $\langle \cdot \rangle_{\tau}$ denoting time averaging. A window $W$ centered at time $t_k$ is defined: $W = [t_{k-l/2}, t_{k+l/2}]$, with $l$ denoting the length of this window. Within this window, the two averaging intervals in (2) are defined as: $\tau_1 = [t_{k-l/2}, t_k]$ and $\tau_2 = [t_k, t_{k+l/2}]$. Clearly, $\tau_1$ and $\tau_2$ contain the same number of data samples ($\tau_1 = \tau_2 = l/2$), thus, for brevity, we will refer to either one of these two intervals as $TAU$. According to (1), $\varphi$ takes values between 0° (parallel orientation) and 180° (antiparallel orientation).

Other authors used similar definitions for $B_1$ and $B_2$ (e.g., Borovsky 2008, 2010). Li (2008) and Miao et al. (2011) used only the instantaneous vector measurements at the two edges of the window $W$. Mailyan et al. (2008) (see also Munteanu et al., 2013) used two time intervals: one for computing the averages, and an additional time interval for separating $B_1$ from $B_2$. For the purpose of this study, we will use $B_1$ and $B_2$ as defined by (2).

Figure 1a depicts a synthetic dataset with three components of 1000 data samples each. The $x$ and $y$ components include sharp discontinuities added onto a constant signal with superposed white Gaussian noise; the $z$-component is white noise. Figure 1b shows the result obtained with (1) for a window $W$ of 128 data samples centered on the discontinuity. Figure 1b also shows an illustration of the time intervals $\tau_1$ and $\tau_2$ from (2). The two sharp changes in the $x$ and $y$ components correspond, as expected from geometrical considerations, to an angular change of $\varphi \approx 90°$.

For the analysis of a real signal, continuously collected in-situ, we developed a sliding-window algorithm which computes the angular changes for windows $W$ centered at each time instance $t_k$. An illustrative example is shown in Fig. 1c. The algorithm starts with the analysis of the first 128 samples of the signal and computes the value $\varphi(t_64)$ corresponding to the center of this first instance of the analysis window. In the next step the window is moved by one sample,
and the procedure is repeated to compute the value $\varphi(t_{36})$. The algorithm continues until the last value $\varphi(t_{36})$ is computed. Figure 1c shows that $\varphi$ takes values close to 0° up to sample number 436, then it starts to increase as the window position approaches the discontinuity, reaching a maximum value of $\varphi \approx 90°$ at the discontinuity center (at sample 500); then it starts to decrease back towards $\varphi \approx 0°$ (at sample 564). This increasing (decreasing) trend of angular changes is due to the relative position of the sliding window with respect to the actual position of the discontinuity, resulting in amplitude changes as the window moves closer to (away from) the discontinuity. Figure 1 was generated using the software analysis tool Integrated Nonlinear Analysis (INA) (Munteanu, 2017; see also http://www.storm-fp7.eu/index.php/data-analysis-tools).

**Figure 1.** a) Synthetic dataset with three components of 1000 data samples each. b) Zoom-in on the 128-sample interval highlighted in the top panel; $\tau_1$ and $\tau_2$ are marked in dark-blue and light-blue, respectively. c) Local discontinuity analysis of the synthetic dataset depicted in panel (a), using a sliding-window of 128 data samples: $\varphi(t_k)$ (from (1); blue line labeled “phi”), local discontinuity measure $\text{LDM}^{(\text{deg})}$ (from (3); red line) and $\varphi_c = 30°$ (green line labeled “thr”). This figure, and also Figs. 3, 4 and 5, were generated using the Integrated Nonlinear Analysis (INA) library (Munteanu, 2017; see also http://www.storm-fp7.eu/index.php/data-analysis-tools).

The discontinuity detection algorithm we propose here is based on a critical value of the angular change. This value, denoted in the following as $\varphi_c$, is set to 30°. We define a local discontinuity measure (LDM) which is equal to the value of the rotation angle $\varphi$, if this is larger than $\varphi_c$, and zero otherwise:
\[ LDM^{(deg)}(t_k) = \begin{cases} \phi(t_k), & \text{if } \phi(t_k) \geq \phi_c \\ 0, & \text{otherwise} \end{cases} \]  

(3)

\( LDM^{(deg)} \) is used as a quantitative measure for the presence of directional discontinuities. Figure 1c shows the \( LDM^{(deg)} \) values computed using (3) for the synthetic signal. As expected, \( LDM^{(deg)} \) is different from zero (and exactly equal to \( \phi \)) only when \( \phi \geq 30^\circ \).

For an on-board FPGA implementation of the sliding-window algorithm described above, there is no need to apply the \( \cos^{-1} \) function and multiply by \( \frac{180}{\pi} \), as in (1). If needed, these operations can be later performed on ground, using calibrated results. Thus, a simplified version of the method can be implemented in the FPGA device, based solely on the normalized dot product (\( ndp \)):

\[ ndp(t_k) = \frac{B_1 \cdot B_2}{|B_1||B_2|} \]  

(4)

with \( B_1 \) and \( B_2 \) defined by (2). From (1) and (4), it follows that angular changes of 180° and 0° correspond to normalized dot product values of −1 and +1, respectively. Similarly, the value of \( ndp = 0 \) will correspond to an angular change of \( \phi = 90^\circ \). For future reference, the threshold value \( \phi_c = 30^\circ \), corresponds to \( ndp_c \approx 0.87 \).

Based on the \( ndp \) parameter given in (4), a new localized discontinuity measure can be defined:

\[ LDM^{(ndp)}(t_k) = \begin{cases} ndp(t_k), & \text{if } ndp(t_k) \leq ndp_c \\ 0, & \text{otherwise} \end{cases} \]  

(5)

\( LDM^{(ndp)} \) will be further used in the FPGA implementation of the detection algorithm.

2.2 Reconfigurable FPGA devices for on-board processing

Modern architectures designed for on-board analysis of data make use of reconfigurable FPGA technology (Pingree, 2010; Kuwahara, 2009; French et al., 2018; Huber et al., 2007; Hanafi et al., 2017). In space, the electronic systems are prone to failures caused by radiations generated by high-energy particles. The FPGA devices are even more vulnerable since radiations can affect their configuration logic and applications data. To mitigate the effect of radiations, specific software and hardware techniques are used for space-qualified FPGA designs. The radiation tolerant FPGA devices from Xilinx (Virtex, 2014; Virtex, 2018; Kintex, 2020) or Microsemi (Microsemi, 2015) mitigate the effect of space radiations and eliminate the requirement of using dedicated mitigation techniques, like TMR (triple modular redundancy). Our current design/prototype relies on commercial FPGAs and can be ported to radiation hardened architectures.

The development flow for FPGA devices is based on a Register Transfer Level (RTL) description of the circuits using a hardware description language. The High-Level Synthesis (HLS) technology simplifies the digital signal processing algorithms implementation in FPGA devices allowing the description of the algorithm’s functionality using a classical programming language and the generation of the RTL description.

We used HLS to generate an RTL description for the discontinuity detector and an RTL description for the rest of the system components.
3 System overview and implementation

The spacecraft’s main on-board computers execute multiple critical tasks. Our prototype demonstrates that some tasks can be retargeted to be executed on FPGA devices even at instrument level, thus reducing the main on-board computers’ utilization and saving energy resources.

The functionality of the system was validated with synthetic signals, and also with real measurements received from a magnetic sensor, as discussed below. The laboratory tests were performed by continuously monitoring the measurements received from the magnetic sensor and calculating the local discontinuity measures. The output of the system can be used to notify the on-board computer to perform additional analyses or to confirm a status quo in the evolution of the field parameters.

3.1 System implementation

The directional discontinuity detector based on a local discontinuity measure defined by (4) is implemented on a Digilent Nexys 4 DDR development board featuring a commercial Xilinx Artix-7 FPGA device. The architecture of the system, shown in Fig. 2a, includes a Digilent CMPS2 module attached to the development board to measure the magnetic field. The laboratory prototype includes its own data provider which is a Memsic MMC34160PJ magnetic sensor (www.memsic.com/magnetometer-4) able to perform measurements of the magnetic field on 3 axes within the full-scale range of ±16 Gauss. The sensor can perform measurements every 10 ms when the resolution of the analog-to-digital convertor is set to 16 bits. The magnetic sensor provides an I2C communication channel for configuration, control and to read the measurements.

The discontinuity detector that implements our proposed detection algorithm is implemented in the Xilinx Artix-7 FPGA device. When directional discontinuities are detected, the Discontinuity Detected output notifies the main on-board computer or other instruments; this notification can be used to perform, for instance, additional analyses. The Serial Connection with the host computer is used only for the validation of the results produced by the system. In a production setup for the system to be deployed on the satellite’s on-board FPGA device, the Serial Connection will be removed or replaced with other communication protocols to receive the measurements from the on-board magnetic instrument and the computed discontinuity measures.

3.2 FPGA system design

The design implemented in the FPGA device provides the following functionalities: an I2C communication unit to interface with the attached data provider (magnetic sensor), the Directional Discontinuity Detector component that analyses the measurements received from the sensor and calculates the discontinuity measures, an Output component that notifies the main on-board computer when discontinuities are detected, a Data Buffer that aggregates the magnetic sensor measurements and the computed discontinuity measures, and a Serial Unit to interface with the host computer for the validation of the system. The architecture of the FPGA design is shown in Fig. 2b.
3.2.1 Magnetic sensor interface

The Magnetic Sensor Interface implements the communication protocol with the Memscic magnetic sensor. The implementation is based on an I2C controller which provides a generic implementation of the protocol, and on additional custom circuits to configure and control the magnetic sensor.

Figure 2c shows the architecture of the Magnetic Sensor Interface. The Commands State Machine and Compass State Machine components implement the operations specific to the Memscic magnetic sensor according to the sensor datasheet (www.memsic.com/magnetometer-4), e.g. take one measurement, activate continuous measurement mode, and calibration specific
commands. The interface also includes the Synthetic Signals Generator that generates synthetic signals for the validation of the discontinuity detector.

The communication with the magnetic sensor is initiated by the assertion of the Start input signal. A sequence of commands is sent to configure and control the sensor: 1) execute the self-check test, 2) measure and save the calibration offsets, and 3) activate continuous measure mode. After the initial self-check test, the sensor performs two measurements to determine the calibration offsets. Once the calibration phase is finished, the continuous measurements mode is activated and the sensor performs measurements of the three axes every 12 ms. The measurements for each axis are returned on the X, Y, and Z outputs.

3.2.2 Directional discontinuity detector

The Directional Discontinuity Detector was implemented in C++ and its corresponding RTL description was generated using the high-level synthesis tool from Xilinx. Since the current design assumes a sampling rate of the magnetic sensor of 100 Hz, which is reasonable for on-board triaxial fluxgate magnetometers and is also very low compared to the 100 MHz clock signal driving the FPGA device, the goal set for the high-level synthesis process is to reduce the amount of programmable logic resources required for the design. Note however that the sampling rate is an adjustable parameter of the system.

The raw measurements received from the magnetic sensor are first converted to Gauss and then passed to the Directional Discontinuity Detector. The pseudocode for the C++ implementation of the detector is depicted in Algorithm 1. The WX, WY and WZ parameters store the last measurements received from the magnetic sensor. These parameters are implemented as buffers in which each new measurement is saved and the oldest measurement is discarded. The first loop, lines 2-5, computes the sum of the TAU measurements defined by (2) up to the point for which the discontinuity measure (1) is computed. Lines 6-8 calculate the components of the B1 vector as the mean of all these measurements. The second loop, lines 10-13, computes the sum of the TAU measurements received after the point for which the discontinuity measure is computed, and similarly lines 14-16 calculate the components of the B2 vector as the mean of these measurements (see definitions (2)). Line 17 computes the scalar product between the vectors B1 and B2, while lines 18 and 19 compute the norm for each vector. Finally, line 20 computes the discontinuity measure ndp defined by (4).

3.2.3 Trigger component and serial unit

The Trigger component of the FPGA system generates the output of the discontinuity detection system for the main on-board computer or other instruments. The discontinuity measures ndp computed by the discontinuity detector are compared against a predefined threshold value. If the value exceeds the threshold defined by (5), the output is asserted to notify the main on-board computer or other devices. Based on the requirements of the on-board computer, the Trigger component can be further customized. While this component generates the main output of the system, the Serial Unit sends the measurements received from the magnetic sensor and the computed discontinuity measures to a host computer for the validation of the system and visualization of the results.
Algorithm 1. Pseudocode for the C++ implementation of the discontinuity detector.

```plaintext
function Discontinuity_Detector(WX, WY, WZ, TAU):
    sum_X ← 0, sum_Y ← 0, sum_Z ← 0
    for i = 1 to TAU do
        sum_X ← sum_X + WX[i]
        sum_Y ← sum_Y + WY[i]
        sum_Z ← sum_Z + WZ[i]
    end
    B1_X ← sum_X / TAU
    B1_Y ← sum_Y / TAU
    B1_Z ← sum_Z / TAU
    sum_X ← 0, sum_Y ← 0, sum_Z ← 0
    for i = TAU to 2*TAU do
        sum_X ← sum_X + WX[i]
        sum_Y ← sum_Y + WY[i]
        sum_Z ← sum_Z + WZ[i]
    end
    B2_X ← sum_X / TAU
    B2_Y ← sum_Y / TAU
    B2_Z ← sum_Z / TAU
    norm_B1 ← SQRT(B1_X*B1_X + B1_Y*B1_Y + B1_Z*B1_Z)
    NDP ← product / (norm_B1 * norm_B2)
return NDP
```

4 Experimental results

4.1 Computer validation of the discontinuity detection algorithm

4.1.1 Testing the effects of discontinuity strength, signal-to-noise ratio, discontinuity thickness and analysis window width

We define the “strength” of a directional discontinuity as the amplitude of the angular change across the discontinuity (see (1)). Figure 3a shows the results of the LDM algorithm applied on a synthetic three-component vector dataset comprised of 3600 data samples per component. Abrupt amplitude changes in the x and y components are included such that they correspond to angular changes of $\varphi = 180^\circ$ (at sample number 900), $\varphi = 90^\circ$ (at sample 1800) and $\varphi = 45^\circ$ (at sample 2700). The LDM algorithm uses a window $W$ of width $l = 128$ data samples, in this case.

Figure 3a demonstrates that the three predefined angular changes are accurately detected by our proposed discontinuity detection algorithm. Fig. 3a shows how the temporal profile of angular changes depends on discontinuity strength. For an angular change of $\varphi = 45^\circ$, one can observe a rather slow increase (decrease) of $\varphi(t_k)$ as we approach (move away from) the center of the discontinuity. For $\varphi = 90^\circ$, the increasing and decreasing trends are faster compared to the $\varphi = 45^\circ$ case. At $\varphi = 180^\circ$ these increasing and decreasing trends almost break down, and
we see rather abrupt jumps from $\varphi \cong 0^\circ$ to $\varphi \cong 180^\circ$. These results were obtained for a signal with a small-amplitude white noise whose standard deviation is equal to 0.1.

Figure 3b shows the results of our LDM algorithm when the noise level is increased by adding a white Gaussian noise with a standard deviation equal to 20. Note that the signal amplitude jumps are of 20 units (for $\varphi = 180^\circ$) and 10 units (for $\varphi = 90^\circ$ and $\varphi = 45^\circ$). Fig. 3b demonstrates that a high noise level, with standard deviation of the order of the signal amplitude jumps, can easily generate spurious discontinuities above the threshold level of $\varphi_c = 30^\circ$.

Figure 3c illustrates the performance of the LDM algorithm applied on a signal including discontinuities with larger width. This figure demonstrates that when a small analysis window is applied on signals containing thick discontinuities, the algorithm fails to accurately detect discontinuities.

![Figure 3](image)

**Figure 3.** a) Effect of discontinuity strength. b) Effect of poor signal-to-noise ratio. c) Effect of discontinuity width. d) Effect of window length. In each panel, top plots depict synthetic datasets with three components of 3600 samples each, and bottom plots depict the local discontinuity analysis using the setup in Fig. 1c. Amplitude changes are introduced in all synthetic datasets so as to correspond to angular changes of $180^\circ$ (at sample number 900), $90^\circ$ (at 1800) and $45^\circ$ (at 2700). Panel a) depicts the results for a low noise-level and abrupt (1 sample) amplitude changes, in panel b) the noise level is increased, and in panel c) the amplitude changes are widened to span 256 samples each. Local discontinuity analysis is performed using windows of 128 samples (panels a, b and c) and 1024 samples (panel d).

Figure 3d depicts the effect of enlarging the length of the analysis window. In this case the resulting temporal profiles of $\varphi(t_k)$ are much wider around each discontinuity, compared to those in Fig. 3a. When the length of the analysis window is comparable to the distance between
two adjacent discontinuities, as is the case here, the detection profiles corresponding to each
individual discontinuity start to merge and become indistinguishable from each other. By
enlarging the analysis window even more, the algorithm will eventually detect only one broad
discontinuity. Figure 3d shows results for an analysis window spanning 1024 samples, which is
slightly larger than the separation distance of 900 samples between adjacent discontinuities. One
can observe that the discontinuities characterized by angular changes of 90° and 45° are almost
fully merged, and undistinguishable by the LDM algorithm.

4.1.2 Improving detection accuracy of the LDM algorithm

Figures 3b, 3c and 3d identified cases when the discontinuity detection algorithm failed
to work properly for one of the following reasons: (i) due to poor signal-to-noise ratio (Fig. 3b),
(ii) due to discontinuities being thicker than the analysis window (Fig. 3c), and (iii) due to the
analysis window being larger than the time interval between adjacent discontinuities (Fig. 3d). In
this section we discuss how to address these issues and improve the detection accuracy of the
algorithm.

When the signal-to-noise ratio is decreased, the accuracy of the LDM algorithm can be
maintained by computing the angular changes (1) using a larger number of samples. This can be
explained using the standard error of the mean (SEM), a commonly used statistical measure for
the differences between the mean value of a sample dataset and the mean value of the population
from which the sample was drawn. By definition SEM is directly proportional to the standard
deviation of the sample dataset and inversely proportional to the square root of the sample
length. Thus, using a smaller dataset length increases SEM, and this increases the statistical
uncertainty of the average values used in computing the angular changes. This is even more
important in case of poor signal-to-noise ratio, where the larger standard deviation of the dataset
increases the statistical uncertainty (decreases the statistical significance) of the averages even
more. Increasing the width of the analysis window adds more data samples to the analysis and,
assuming that no other strong discontinuities are added within this enlarged analysis window,
leads to an increased accuracy.

When the width of the analysis window is smaller than the discontinuity thickness, our
algorithm computes angular changes using samples only from inside the discontinuity. Thus,
assuming that the discontinuity has a simple ramp-like structure (as in Fig. 3c), the angular
changes computed using small windows will always be smaller than the angular changes
computed using windows covering the full width of the discontinuity. As in the previous case,
increasing the width of the analysis window will increase the accuracy, assuming again that no
other discontinuities are included in the enlarged analysis window.

When more than one discontinuity is present inside the analysis window, we are in a case
similar to that depicted in Fig. 3d, where the discontinuity detection algorithm fails because the
analysis window is wider than the time interval between adjacent discontinuities. In this case,
accuracy can be increased by decreasing the width of the analysis window.

Figure 4 illustrates an example on how to improve the algorithm’s accuracy by using a
larger analysis window. The signal includes three wide discontinuities identical to those in Fig.
3c, with the addition of a white Gaussian noise with standard deviation equal to 20, as in Fig. 3b.
It is shown that increasing the width of the window allows the detection of discontinuities that
are missed by shorter windows.
To conclude, a compromise has to be made between enlarging the analysis window in order to increase detection accuracy for wider discontinuities and for those buried in noise, and keeping the analysis window small enough so as to be capable of distinguishing between two adjacent discontinuities separated by a small time-interval.

![Synthetic signal](image1)

![Local Discontinuity Analysis](image2)

**Figure 4.** Example on how to mitigate the effects of increased noise-level and discontinuity thickness, by using larger windows. Top plot: synthetic data containing three 256-samples-wide discontinuities superposed onto white Gaussian noise with standard deviation equal to 20 units. Bottom plot: local discontinuity analysis with windows of 512 samples, depicted using the setup in Fig. 1c.

4.1.3 Computer validation of the LDM algorithm using interplanetary magnetic field measurements

In the study by Munteanu et al. (2013) we compiled a database consisting of 365 solar wind discontinuities, identified as clear magnetic field rotations by visually examining interplanetary magnetic field measurements. We select a sample from that database, consisting of magnetic field measurements from the Advanced Composition Explorer (ACE) spacecraft in January 06, 2003. Figure 5 illustrates the results of the discontinuity detection algorithm applied on these real-life, in-situ measurements.

Several specific features are observed in Fig. 5. Let us examine the discontinuity around sample 3250. As we increase the window width, the LDM profile corresponding to this discontinuity becomes wider, as expected. In this case, the peak value of $\phi(t_k)$ computed by our algorithm remains almost unchanged as we increase the width of the analysis window: the discontinuity amplitude is slightly above 100° for the first two windows, and slightly below 100° for the last two windows. The situation is very different for the discontinuity centered around sample 4000. In this latter case, $\phi(t_k)$ decreases systematically, from a value around 120° for the window whose length is set to 32 samples, to a value of 60° for the window whose length is equal to 256 samples.
Figure 5. Computer validation of the directional discontinuity detector using interplanetary magnetic field (IMF) measurements from the Advanced Composition Explorer (ACE) spacecraft in January 06, 2003. a) IMF components as function of sample number. b-e) Local discontinuity analysis: $\varphi(t_k)$ (from (1); blue line labeled “phi”), $\text{LDM}^{(\text{deg})}$ (from (3); red line) and $\varphi_c = 30^\circ$ (green line labeled “thr”). The panels depict results using windows of 32 samples (panel b), 64 (panel c), 128 (panel d) and 256 samples (panel e), respectively.
Other features can also be observed in Fig. 5. The first part of the series, up to sample number 2000, shows very different scaling properties in terms of the number of discontinuities, compared to the second part of the series. The smallest window detects the largest number of discontinuities, and, as we increase the width of the analysis window, more and more discontinuities that are close to each other start to merge. See for example the part of the signal centered around sample 1500. Three distinct discontinuities are detected by the 32-samples analysis window. Using a 64-samples window, the weakest discontinuity starts to merge with the middle amplitude one. Using 128-samples, only two discontinuities are detected, and both are much weaker compared to the strongest one detected using the 32-samples window. The 256-samples window detects only one weak discontinuity around sample number 1500.

The results described above, are similar to the results discussed by Greco et al. (2016). They also observed complex “break ups” and “ramifications” going from singular large-scale discontinuities to multiple small-scale ones, giving rise to a tangled network of primary and secondary structures. We retrieve same types of structures in our LDM results obtained for the group of discontinuities observed around sample 1500 of the signal depicted in Fig. 5.

4.2 Implementing the discontinuity detector in FPGA

The initial prototype of the directional discontinuity detection algorithm was implemented in INA (Munteanu, 2017), a MATLAB-based software analysis tool. The algorithm was tested with series of signals that highlight different kinds of discontinuities, as described in Section 4.1.

For the FPGA implementation of the detection system, we used high-level synthesis to generate the RTL implementation of the discontinuity detection algorithm as described by (2)-(5). Since the Xilinx Vivado HLS 2019.1 (Vivado, 2019 a) does not support MATLAB as programming language for the description of the algorithms, the discontinuity detection algorithm was first rewritten in C++.

To validate the C++ implementation of the algorithm, we designed and implemented a testbench in Vivado HLS which generates the series of synthetic signals and the series of measurements captured by the magnetic sensor as inputs for the discontinuity detector, and then compares the results with the ones generated by the MATLAB prototype for the same inputs.

4.2.1 Data types analysis

The Xilinx Vivado HLS provides support for all the standard C++ datatypes and also supports additional data types which can generate more efficient hardware implementations for the algorithms. Several data types were analyzed for the implementation of the discontinuity detector. The algorithm uses advanced mathematical functions which are supported by the Vivado HLS math library.

Table 1 shows the analyzed data types and the computed errors between the results generated by the MATLAB implementation and the results of the C++ implementation for the series of synthetic signals described in Fig. 6a, and the measurements captured by the magnetic sensor described in Fig. 6b. The Max Error column describes the maximum absolute difference between the discontinuity measures computed by the MATLAB and the C++ implementations.
for the same series of inputs. The Errors Count column reports the number of absolute differences which are higher than 0.001, an arbitrarily selected threshold. Based on these results, we selected the float data type (single-precision) for the implementation of the discontinuity detector as it provides a good trade-off between precision and efficiency of the hardware implementation.

Table 1. Analyzed data types and resulting errors.

<table>
<thead>
<tr>
<th>Test Signal</th>
<th>Data Type</th>
<th>Max Error</th>
<th>Errors Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>Synthetic</td>
<td>Float</td>
<td>0.000000</td>
<td>0</td>
</tr>
<tr>
<td>Capture</td>
<td>Float</td>
<td>0.000000</td>
<td>0</td>
</tr>
<tr>
<td>Synthetic</td>
<td>Half</td>
<td>0.756262</td>
<td>90</td>
</tr>
<tr>
<td>Capture</td>
<td>Half</td>
<td>0.302604</td>
<td>3976</td>
</tr>
<tr>
<td>Synthetic</td>
<td>FXP&lt;32,16&gt;</td>
<td>1.984288</td>
<td>7402</td>
</tr>
<tr>
<td>Capture</td>
<td>FXP&lt;32,16&gt;</td>
<td>1.818750</td>
<td>4259</td>
</tr>
<tr>
<td>Synthetic</td>
<td>FXP&lt;32,14&gt;</td>
<td>1.999315</td>
<td>593</td>
</tr>
<tr>
<td>Capture</td>
<td>FXP&lt;32,14&gt;</td>
<td>1.967990</td>
<td>4235</td>
</tr>
<tr>
<td>Synthetic</td>
<td>FXP&lt;32,20&gt;</td>
<td>0.017650</td>
<td>4</td>
</tr>
<tr>
<td>Capture</td>
<td>FXP&lt;32,20&gt;</td>
<td>0.998943</td>
<td>5588</td>
</tr>
<tr>
<td>Synthetic</td>
<td>FXP&lt;32,22&gt;</td>
<td>0.170812</td>
<td>10</td>
</tr>
<tr>
<td>Capture</td>
<td>FXP&lt;32,22&gt;</td>
<td>1.435630</td>
<td>5910</td>
</tr>
</tbody>
</table>

4.2.2 Discontinuity detector analyses

The Xilinx Vivado HLS allows a direct inference of the RTL component from the C++ source code, thus ensuring a high-quality implementation in the FPGA device. In order to improve the quality of the generated RTL implementation, several code optimizations were analyzed and evaluated after circuit synthesis, based on the timing and resource utilization estimates provided by the Xilinx Vivado HLS tool.

These optimizations were not automatically generated but had to be developed by the research team. In the final version of the discontinuity detection algorithm we replaced the regular C++ arrays which store the last received measurements with shift registers. The sums of the measurements in buffers are maintained in variables which are adjusted for every new measurement received by adding the value of the new measurement and subtracting the value of the measurement leaving the buffer. This way, we eliminate the algorithm loops (see Algorithm 1) which compute the sums of the measurements in buffers.

Table 2 describes the timing estimates for the implementation of the discontinuity detector with different values for the TAU parameter. The implementation targets a clock period of 10 ns, due to the 100 MHz oscillator present on the development board which clocks the FPGA device. This timing constraint is met for all tested values of the TAU parameter.

The Initiation Interval defines the minimum and maximum number of clock cycles before new measurements can be accepted, while the Latency specifies the minimum and maximum number of clock cycles required to compute the discontinuity measure \( ndp \) (see (5)). Considering that we configured the magnetic sensor to take a new measure every 12 ms, these
requirements are also satisfied. Also, the results show that with the shift registers optimization the timing parameters are not influenced by the size of the TAU parameter.

Table 2 also describes the estimated programmable logic resources required for the implementation of the discontinuity detector in the FPGA device with different values for the TAU parameter. The results show that the TAU parameter influences the required number of Block-RAM resources of the FPGA device, while the amount of the other programmable logic resources remains constant.

The discontinuity detectors for two arbitrarily selected values of the TAU parameter, 50 and 100, were generated and exported from Vivado HLS to be integrated with the rest of the system components (see Section 3.2) for validation.

<table>
<thead>
<tr>
<th>TAU samples</th>
<th>Timing Estimates</th>
<th>Utilization Estimates</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Target estimated clock cycles</td>
<td>Initiation Interval</td>
</tr>
<tr>
<td>50</td>
<td>9.384 ns</td>
<td>74 ns</td>
</tr>
<tr>
<td>100</td>
<td>9.384 ns</td>
<td>74 ns</td>
</tr>
<tr>
<td>500</td>
<td>9.384 ns</td>
<td>74 ns</td>
</tr>
<tr>
<td>1000</td>
<td>9.384 ns</td>
<td>74 ns</td>
</tr>
<tr>
<td>5000</td>
<td>9.384 ns</td>
<td>74 ns</td>
</tr>
</tbody>
</table>

4.3 Validation of the discontinuity detector in FPGA

The RTL description of the discontinuity detector generated by the Xilinx Vivado HLS was integrated with the rest of the system as described in Section 3. The system implemented in the Artix-7 FPGA device using the Xilinx Vivado 2019.1 (Vivado, 2019 b) suite was tested with synthetic signals and real measurements of the magnetic field received from the magnetic sensor.

The measurements and the computed discontinuity measures \( ndp \) are sent to the host machine for visualization and the results were compared with the ones obtained with the MATLAB implementation (adapted according to (4)). The maximum absolute error between the two implementations is 0.

Figure 6a shows the local discontinuity measures computed using FPGA for three synthetic signals with 10,000 samples each. Note that the threshold value between weak and strong discontinuities used in the MATLAB-based results from Section 4.1, i.e. \( \varphi_c = 30^\circ \), corresponds to a normalized dot product value of \( ndp_c \cong 0.87 \) (see Section 2.1). Also note the thresholding of \( \varphi \) stated that all angular changes larger 30\(^\circ\) corresponded to strong discontinuities. In the case of the \( ndp \) parameter (defined in (4)) the situation is somewhat different: all normalized dot product values in the interval \([0.87, 1]\) are “below” the threshold value, and are considered weak discontinuities, while \( ndp \) values in the interval \([-1, 0.87]\), are “above” the threshold, and correspond to strong discontinuities.

Figure 6a demonstrates that the \( ndp \) measure is capable of accurately detecting all directional discontinuities included in the synthetic dataset. In particular, three strong
discontinuities dominate the results: the first one around sample 3500, with \( ndp = -1 \), i.e. \( \varphi = 180^\circ \) (see (1) and (4)); the second one around sample 5000, with \( ndp = 0 \), i.e. \( \varphi = 90^\circ \); and the third one around sample 6000, with \( ndp \approx 0.71 \), i.e. \( \varphi = 45^\circ \). These strong discontinuities are all accurately detected “above” the threshold value (see the previous paragraph).

The synthetic dataset of Fig. 6a also includes a few additional weak discontinuities: a set of two around sample 2500 and another set around sample 7500. One can observe that the \( ndp \) measure is able to detect even these weak discontinuities, but, since they are “below” the threshold value, they will not activate the **Trigger Component** of the FPGA system (see Section 3.2.3).

Another noteworthy result in Fig. 6a is the fact that all directional discontinuities detected by the FPGA device, even the weakest ones, show a persistency of the value of the \( ndp \) measure as we increase the analysis window from TAU = 50 to TAU = 100 samples. This is consistent with the results illustrated in Figs. 3a and 3d (see also Fig. 5), and is due to the fact that all discontinuities in Fig. 6a are isolated structures, i.e., the time intervals between adjacent discontinuities are larger than the width of the analyzing window. This is not the case for the signal in Fig. 6b, as we describe next.

**Figure 6.** Validation of the discontinuity detector in FPGA using: a) synthetic signals, and b) measurements received from the magnetic sensor. In both panels, top plot shows the analysed dataset; middle plot depicts \( ndp \) (from (4); red line) for TAU=50 samples; the \( ndp \) threshold (green line) is at \( ndp_c \approx 0.87 \); bottom plot, same as middle plot, but for TAU=100 samples.
Figure 6b shows the results obtained for measurements received from the magnetic sensor. To artificially modify the magnetic field measured by the sensor, a magnet was used to produce the sharp variations observed in the measured magnetic field. Figure 6b demonstrates that the *ndp* measure computed by the FPGA device is capable of accurately detecting directional discontinuities even for these highly fluctuating measurements received from the magnetic sensor. One can observe that multiple weak discontinuities are detected using the small analysis window (TAU = 50 samples), but some of them are not detected as distinct events when the larger analysis window (TAU = 100 samples) is used. This is because the weaker discontinuities have merged into a single profile (similar to the case around sample 1500 in Fig. 5). A clear example can be seen around sample 2500: for TAU = 50 samples, two relatively weak discontinuities with *ndp* values slightly above the threshold limit are observed; for TAU = 100, only one of these two discontinuities is detected, with a corresponding value for the *ndp* measure equal to the threshold limit.

Other interesting features evidenced by Fig. 6b are the large changes of the peak *ndp* values as we change the width of the analysis window. This is due to the fact that adjacent discontinuities are separated mostly by time intervals which are smaller than the width of the analysis window. See, e.g., the two strongest discontinuities around sample 4500: for TAU = 50 samples, they have *ndp* values slightly below -1, i.e. \( \varphi \approx 180^\circ \); while for TAU = 100, their *ndp* values are only slightly "above" -0.5, i.e. \( \varphi \approx 120^\circ \).

### 4.4 Energy efficiency and device utilization

Table 3 describes the amount of programmable logic resources used by the implementation of the whole system in an Artix XC7A100T-CSG324 FPGA device for the selected values of the *TAU* parameter, 50 and 100 samples. These results, generated after implementation, show that the system uses just a small part of the FPGA device resources, allowing for other functionalities to be implemented in the same device.

We also computed power estimates for the whole system implemented in the FPGA device. Our device power analysis showed that, from a total On-Chip Power of 0.261 W (100%), the Device Static Power was 0.098 W (37%) and the Dynamic Power was 0.163 W (63%). The power analysis for the design was performed using the default environmental settings in Xilinx Vivado 2019.1 environment.

<table>
<thead>
<tr>
<th>Resource</th>
<th>Utilization</th>
<th>Available</th>
<th>Utilization %</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td><em>TAU</em> 50</td>
<td><em>TAU</em> 100</td>
<td><em>TAU</em> 50</td>
</tr>
<tr>
<td>LUT</td>
<td>7110</td>
<td>7491</td>
<td>63400</td>
</tr>
<tr>
<td>LUTRAM</td>
<td>522</td>
<td>809</td>
<td>19000</td>
</tr>
<tr>
<td>FF</td>
<td>6165</td>
<td>6165</td>
<td>126800</td>
</tr>
<tr>
<td>BRAM</td>
<td>3</td>
<td>3</td>
<td>135</td>
</tr>
<tr>
<td>DSP</td>
<td>24</td>
<td>24</td>
<td>240</td>
</tr>
</tbody>
</table>
5 Summary and conclusions

We designed an algorithm to continuously compute changes in the direction of a three-component vector quantity. The algorithm was first implemented in the MATLAB-based software tool Integrated Nonlinear Analysis - INA (Munteanu, 2017; see also http://www.storm-fp7.eu/index.php/data-analysis-tools). This software implementation was used for the validation and testing of the algorithm for various synthetic datasets and in-situ magnetic field measurements. The algorithm’s functionality is demonstrated for magnetic discontinuities in space, but, due to its adjustable parameters, the detection method can be used to analyze any vector quantity for which rapid direction changes are important.

In space physics, the term “directional discontinuity” was originally used to denote a change in interplanetary magnetic field (IMF) direction of more than 30 degrees in less than 30 seconds. The exact threshold between weak and strong discontinuities and also their duration can vary significantly depending on the specific datasets being used and/or specific science questions being addressed. Random fluctuations in the direction of the IMF are ubiquitous, due to either natural variability and/or instrumental noise, making it almost impossible to use such fixed threshold values (e.g. 30 sec. for duration, or 30° for strength). Our algorithm uses adjustable thresholds, adjustable widths for the analysis windows and also averaging procedures in order to reduce the adverse effects of the background variability on the detection accuracy. A sliding-window algorithm is also designed in order to perform real-time monitoring and continuous discontinuity detection.

The directional discontinuity detection algorithm is adapted for and implemented on a Field-Programmable Gate Array (FPGA) device. In order to optimize the FPGA implementation, the complex calculations of angular changes used by the software implementation, which required the use of trigonometric functions, were replaced by much simpler calculations based solely on dot products, which require only basic arithmetic operations.

The FPGA design was extensively validated and tested using multiple synthetic datasets and real-life laboratory magnetometer measurements. Detailed experimental results regarding energy efficiency, power consumption, and resource utilization demonstrate the usefulness of the design and the feasibility of an FPGA-based discontinuity detector for a real-time monitoring of observables on-board spacecraft.

We also report the optimizations applied on the FPGA design in order to minimize the computational resources and ensure an efficient utilization of the limited computational and energy resources available on-board. The simplicity of the design flow, the flexibility and the short time to market of the FPGA devices, compared to ASIC, can constitute a pathway for future data analysis strategies.

The discontinuity detection algorithm described in this paper is part of a broader effort meant to build an integrated library for autonomous on-board digital signal processing. This library already includes modules designed for spectral and statistical analysis of on-board data and is able to produce a set of key data descriptors when the entire data stream cannot be sent to the ground for further analysis.
Acknowledgments

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Data Availability Statement

In Section 4.1.3 we tested the directional discontinuity detector using magnetic field data from the MAG instrument (Smith et al., 1998) on-board the Advanced Composition Explorer (ACE) spacecraft. We used a 24-hour time interval, at 16 sec time resolution, covering the whole day of January 06, 2003. The data are publicly available from the Coordinated Data Analysis Web (CDAWeb; https://cdaweb.gsfc.nasa.gov) maintained by the the National Aeronautics and Space Administration (NASA).

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