Discriminating underground nuclear explosions leading to late-time radionuclide gas seeps

Dylan Robert Harp\textsuperscript{1}, Suzanne Michelle Bourret\textsuperscript{2}, Philip H. Stauffer\textsuperscript{1}, and Ed Michael Kwicklis\textsuperscript{1}

\textsuperscript{1}Los Alamos National Laboratory (DOE)
\textsuperscript{2}Los Alamos National Laboratory

November 23, 2022

Abstract

Utilizing historical data from the U.S. nuclear test program and freely available barometric pressure data, we performed an analytical barometric-pumping efficiency analysis to determine factors resulting in late-time radionuclide gas seeps from underground nuclear explosions. We considered sixteen underground nuclear explosions with similar geology and test setup, of which five resulted in the measurement of late-time radionuclide gas concentrations at the ground surface. The factors we considered include barometric frequency and amplitude, depth of burial, air-filled porosity, intact-rock permeability, fracture aperture, and fracture spacing. The analysis indicates that the best discriminators of late-time radionuclide gas seeps for these explosions are barometric frequency and amplitude and air-filled porosity. While geologic information on fracture aperture and spacing is not available for these explosions, the sensitivity of barometric-pumping efficiency to fracture aperture indicates that fracture aperture would likely also be a good discriminator.
Discriminating underground nuclear explosions leading to late-time radionuclide gas seeps

Dylan R. Harp, S. Michelle Bourret, Philip H. Stauffer, and Edward M. Kwicklis

Computational Earth Science, Los Alamos National Laboratory, Los Alamos, NM, 87545

Key Points:
- Barometric-pumping efficiency facilitates discrimination of underground nuclear explosions leading to late-time seeps.
- Longer high-efficiency barometric periods and higher high-efficiency amplitudes indicate a greater chance of late-time seeps.
- Low air-filled porosity indicates a greater chance of late-time seeps.

Corresponding author: Dylan Harp, dharp@lanl.gov
Abstract
Utilizing historical data from the U.S. nuclear test program and freely available barometric pressure data, we performed an analytical barometric-pumping efficiency analysis to determine factors resulting in late-time radionuclide gas seeps from underground nuclear explosions. We considered sixteen underground nuclear explosions with similar geology and test setup, of which five resulted in the measurement of late-time radionuclide gas concentrations at the ground surface. The factors we considered include barometric frequency and amplitude, depth of burial, air-filled porosity, intact-rock permeability, fracture aperture, and fracture spacing. The analysis indicates that the best discriminators of late-time radionuclide gas seeps for these explosions are barometric frequency and amplitude and air-filled porosity. While geologic information on fracture aperture and spacing is not available for these explosions, the sensitivity of barometric-pumping efficiency to fracture aperture indicates that fracture aperture would likely also be a good discriminator.

Plain Language Summary
Variations in air pressures (barometric variations) can drive gases created during underground nuclear explosions to the ground surface. The changes in air pressure above the ground push and pull the air in connected spaces between rocks (fractures) allowing these pressure changes to access 100s of meters into the subsurface. Some barometric variations and geologies are more conducive to driving gases to the ground surface than others. Using a model that combines the effect of the barometric variations and geology, we are able to identify scenarios that are more likely to lead to gases arriving at the ground surface after an underground nuclear explosion. Identifying underground nuclear explosions that will likely result in gases arriving at the ground surface and entering the atmosphere provides information for investigators trying to verify nuclear test ban treaties.

1 Introduction
Verifying adherence of signatory countries to nuclear test ban treaties, such as the Comprehensive Nuclear Test Ban Treaty (CTBT), requires the ability to detect clandestine nuclear tests. In order to take advantage of the containment and obscurity provided by the subsurface, clandestine nuclear tests will likely be in the form of an underground nuclear explosion (UNE). Detecting radionuclide gases seeping at the ground surface of a suspected UNE site will provide “smoking gun” evidence of a clandestine UNE (Kalinowski et al., 2010; Sun & Carrigan, 2014). Identifying the factors that will increase the chance of late-time seeps after a clandestine UNE will help determine if radionuclide gases should be expected to be detected at the ground surface near the UNE site or in the atmosphere.

While prompt releases of radionuclide gas due to a severe containment failure could occur within minutes to a few hours after a UNE, late-time releases at the ground surface to the atmosphere due to barometrically driven gas transport (referred to as late-time seeps (United States Congress, 1989)) could occur from days to months afterwards. The occurrence of a late-time seep will depend on the complex process of barometrically driven subsurface gas transport, commonly referred to as barometric pumping, whereby increasing barometric pressure drives atmospheric air into the subsurface through fractures and decreasing barometric pressure draws subsurface air towards the ground surface (Nilson et al., 1991; Auer et al., 1996; Neeper, 2003; Neeper & Stauffer, 2012). Storage in the intact rock pore space (air and water filled) result in a ratcheting of gases towards the surface in between barometric cycles resulting in significantly faster transport than would occur due to diffusive transport alone (Nilson et al., 1991; Harp et al., 2019). The process of barometric pumping involves advective flow through fractures, diffusive transport in intact rock, dissolution/exolution from pore-water (Harp et al., 2018), iso-
topic fractionation, and transport due to explosion-induced pressure and temperature
gradients (Sun & Carrigan, 2016). Factors controlling the rate of gas transport can in-
clude subsurface properties, such as air-filled porosity, saturation, fracture aperture (i.e.,
permeability), and intact rock diffusivity (Jordan et al., 2014), and the characteristics
of the barometric pressure signal before and after the UNE, such as amplitude and fre-
quency (Harp et al., 2019). Factors associated with UNE design will also affect the like-
lihood of late-time seeps, such as depth of burial, yield, fissile material, etc.

In this study, we analyze the importance of barometric frequency and amplitude,
air-filled porosity, rock-matrix permeability, and depth of burial as discriminating fac-
tors in determining the potential for late-time seeps from UNEs. We evaluate these fac-
tors using an analytical barometric-pumping efficiency analysis approach presented in
Harp et al. (2019) and briefly summarized in Section 2. We performed the analysis on
barometric and site data associated with 16 historic U.S. UNEs collected and evaluated
in Bourret, Kwicklis, Harp, et al. (2019) and briefly described in Section 3. In Section 4,
we present a thorough analysis of the factors, including a comparison of barometric-pumping
efficiencies between UNEs with and without late-time seeps and an analysis of the sen-
sitivity of the barometric-pumping efficiency to the factors. In Section 5, we discuss the
implications of the results for discriminating late-time seeps from UNEs. In Section 6,
we provide a list of conclusions from the research.

2 Methods

We use an analytical approach to quantify barometric-pumping efficiency based on
analytical solutions derived by Nilson et al. (1991) described in detail in Harp et al. (2019).
The analytical approach is briefly described here.

Barometric-pumping efficiency quantifies the ability of a barometric component (i.e.,
a single frequency/amplitude pair, where a barometric signal is composed of many baro-
metric components) to extract gas from the subsurface to the atmosphere. It is comprised
of three factors: (1) the ability of the barometric component to push a packet of atmo-
spheric air to the depth of the gas in the subsurface and extract the packet of air back
to the atmosphere; (2) if the timing of the barometric component is such that gas-contaminated
air has time to exchange with the atmospheric packet of air; and (3) how often the baro-
metric component occurs (i.e., its frequency).

The first factor is captured in the breathing efficiency \( \eta_B \), which quantifies the vol-
ume of air that a barometric cycle is able to extract relative to the maximum volume
that could be removed if the subsurface were in perfect equilibrium with the atmosphere
(i.e., if the subsurface had infinite pneumatic diffusivity). The second factor is captured
in the diffusive exchange efficiency \( \eta_D \), which quantifies the fraction of the mass of tracer
that is removed versus the maximum that would be removed if the concentration of the
packet of air could achieve and maintain the concentration of gas at depth during its re-
turn to the ground surface. The third factor is the barometric component frequency, \( \omega \),
which accounts for the fact that given two barometric components with otherwise sim-
ilar efficiencies (i.e., breathing and diffusive exchange efficiencies), the one that occurs
more often will be able to extract more tracer gas over time.

These three factors can be combined into the overall barometric-pumping efficiency
\( \eta_P \) (referred to as production efficiency in Harp et al. (2019)), as

\[
\eta_P = \eta_B \eta_D \omega. \tag{1}
\]

In this study, we utilize equation 1 to discriminate factors associated with UNEs result-
ing in late-time seeps. Note that all the geologic factors considered here (depth of burial,
air-filled porosity, matrix permeability) are included in the calculation of barometric-pumping
efficiency.
Table 1. Site-specific UNE data.

<table>
<thead>
<tr>
<th>UNE</th>
<th>Date</th>
<th>Radionuclides</th>
<th>Days till seep</th>
<th>Depth of burial [m]</th>
<th>Air-filled porosity [-]</th>
<th>Matrix permeability [m²]</th>
</tr>
</thead>
<tbody>
<tr>
<td>KAPPELI</td>
<td>7/25/84</td>
<td>¹³¹mKr, ⁶⁵Kr</td>
<td>61</td>
<td>640</td>
<td>0.119</td>
<td>1.77 x 10⁻¹⁴</td>
</tr>
<tr>
<td>TIERRA</td>
<td>12/15/84</td>
<td>¹³¹mKr, ⁶⁵Kr</td>
<td>11</td>
<td>640</td>
<td>0.129</td>
<td>8.07 x 10⁻¹⁵</td>
</tr>
<tr>
<td>LABQUARK</td>
<td>9/30/86</td>
<td>¹³¹mKr, ⁶⁵Kr</td>
<td>25</td>
<td>616</td>
<td>0.154</td>
<td>7.13 x 10⁻¹⁵</td>
</tr>
<tr>
<td>BODIE</td>
<td>12/13/86</td>
<td>¹³¹mKr, ⁶⁵Kr</td>
<td>2</td>
<td>635</td>
<td>0.085</td>
<td>1.68 x 10⁻¹⁴</td>
</tr>
<tr>
<td>BARNWELL</td>
<td>12/13/86</td>
<td>¹³¹mKr, ⁶⁵Kr</td>
<td>9</td>
<td>600</td>
<td>0.056</td>
<td>8.17 x 10⁻¹⁵</td>
</tr>
<tr>
<td>EGMONT</td>
<td>12/13/86</td>
<td>¹³¹mKr, ⁶⁵Kr</td>
<td>–</td>
<td>546</td>
<td>0.155</td>
<td>1.50 x 10⁻¹⁵</td>
</tr>
<tr>
<td>TOWANDA</td>
<td>5/2/85</td>
<td>–</td>
<td>–</td>
<td>665</td>
<td>*0.13</td>
<td>5.40 x 10⁻¹⁵</td>
</tr>
<tr>
<td>SALUT</td>
<td>6/12/85</td>
<td>–</td>
<td>–</td>
<td>608</td>
<td>0.191</td>
<td>1.58 x 10⁻¹⁴</td>
</tr>
<tr>
<td>SERENA</td>
<td>7/25/85</td>
<td>–</td>
<td>–</td>
<td>597</td>
<td>0.103</td>
<td>2.26 x 10⁻¹⁴</td>
</tr>
<tr>
<td>GOLDSMTE</td>
<td>12/28/85</td>
<td>–</td>
<td>–</td>
<td>549</td>
<td>0.144</td>
<td>1.52 x 10⁻¹⁴</td>
</tr>
<tr>
<td>JEFFERSON</td>
<td>4/22/86</td>
<td>–</td>
<td>–</td>
<td>609</td>
<td>0.148</td>
<td>1.42 x 10⁻¹⁴</td>
</tr>
<tr>
<td>DARWIN</td>
<td>6/25/86</td>
<td>–</td>
<td>–</td>
<td>549</td>
<td>0.120</td>
<td>1.47 x 10⁻¹⁴</td>
</tr>
<tr>
<td>CYBAR</td>
<td>7/17/86</td>
<td>–</td>
<td>–</td>
<td>628</td>
<td>*0.13</td>
<td>9.27 x 10⁻¹⁵</td>
</tr>
<tr>
<td>BELMONT</td>
<td>10/16/86</td>
<td>–</td>
<td>–</td>
<td>605</td>
<td>0.137</td>
<td>7.96 x 10⁻¹⁵</td>
</tr>
<tr>
<td>DELMAR</td>
<td>4/18/87</td>
<td>–</td>
<td>–</td>
<td>544</td>
<td>0.157</td>
<td>1.23 x 10⁻¹⁴</td>
</tr>
<tr>
<td>HARDIN</td>
<td>4/30/87</td>
<td>–</td>
<td>–</td>
<td>625</td>
<td>0.104</td>
<td>1.45 x 10⁻¹⁴</td>
</tr>
</tbody>
</table>

*Value not available; average of values from other UNEs used.

3 Data

The data utilized here include geologic data and barometric pressure records for the 16 UNEs compiled by Bourret, Kwicklis, Harp, et al. (2019). We used the geologic data to assign air-filled porosity, intact-rock (matrix) permeability, and depth of burial for each UNE presented in Table 1 along with the date of the UNE, radionuclides detected, and the number of days until radionuclide gas detection after each UNE. The five UNEs where late-time seeps were observed are listed at the top of Table 1 followed by those where seeps were not observed. The air-filled porosity and matrix permeability are depth averaged properties using measured properties for the geologic layers overlying each UNE. Note that KAPPELI was the only UNE with an observed late-time seep in which an isotope of xenon was not detected (only ⁸⁵Kr was detected). KAPPELI also had significantly later radionuclide detection at the ground surface at 61 days after the UNE.

Bourret, Kwicklis, Harp, et al. (2019) collected the barometric records from the Weather Underground website (https://www.wunderground.com/history) for Mercury, NV, located just outside the southwestern entrance to the National Nuclear Security Site (NNSS). Since our analysis uses the frequencies and amplitudes of the barometric signals, and not the absolute magnitude, the barometric records were not elevation-corrected to the ground-surface elevations of the UNEs prior to analysis. In order to capture the characteristic of the barometer before and after each UNE, we included 30 days prior and 60 days after each UNE.

4 Results

Initially, we decomposed the barometric records for each UNE into frequency/amplitude pairs using a Fast Fourier Transform (Cooley & Tukey, 1965) algorithm. The top plot in Figure 1 presents the period/amplitude pairs, where period=2π/frequency. The components associated with UNEs with late-time seeps are in red and those without are in blue.

We used the historical data collected by Bourret, Kwicklis, Harp, et al. (2019) to assign air-filled porosity, matrix permeability, and depth of burial for each UNE. Lacking specific details on fracture aperture and spacing for each UNE, we applied a fracture aperture of 1 mm and fracture spacing of 10 m for all UNE’s. Using these decomposed period/amplitude pairs and properties, we then calculated the barometric-pumping efficiency using equation 1. We present these efficiencies in the bottom plot of Figure 1, where the barometric components associated with UNEs with late-time seeps are in red...
and those without are in blue. By inspecting the locations of red vs blue points, it is apparent that, although there is significant overlap, the efficiencies for UNEs with late-time seeps are generally higher than for those without.

Next, we calculated the average period and amplitude associated with the highest barometric-pumping efficiency components for each UNE. We accomplished this by sorting the period/amplitude pairs in order of decreasing barometric-pumping efficiency, smoothing the mean periods and amplitudes in this order, and then identifying the maximum period and amplitude of these smoothed curves. In Figure S1 of supplemental information, we present the raw and smoothed mean periods and amplitudes produced during this analysis. This process provides a good estimate of an average period and amplitude associated with high-efficiency barometric components.

The average high-efficiency periods and amplitudes for each UNE are plotted in the top and 2nd plot, respectively, of Figure 2. Subsequent plots in the figure contain depth of burial, air-filled porosity, matrix permeability, and the average maximum barometric-pumping efficiency (i.e., average of 30 highest efficiencies for each UNE) for reference. In general, all UNEs with late-time seeps had longer high-efficiency periods and larger high-efficiency amplitudes than those that did not. In Figure 3, we plot the average high-efficiency periods vs average high-efficiency amplitudes to illustrate the clustering of UNEs with late-time seeps at longer average periods and higher average amplitudes. The exception was KAPPELI, which had different late-time seep characteristics as described in Section 3 and discussed in Section 5.

In general, the UNEs with late-time seeps were deeper, although this is assumed to be coincidental as we are not aware of a physical reason this would increase the chances of late-time seeps. Two of the UNEs with late-time seeps (BODIE and BARNWELL)
had much lower air-filled porosities, which would be expected to increase the chance of late-time seeps, while the other three had air-filled porosities similar to UNEs without late-time seeps. The permeabilities of all UNEs varied within an order of magnitude, with similar ranges between UNEs with late-time seeps and those without. BODIE and BARNWELL also had high barometric-pumping efficiencies, while KAPPELI, TIERRA, and LABQUARK had efficiencies similar to UNEs without late-time seeps.

As mentioned above, the fracture aperture and spacing are not known for all the individual UNEs; therefore, the same values were used for all UNEs. The inability to include UNE-specific values for these factors may explain why barometric-pumping efficiencies were not higher for KAPPELI, TIERRA, and LABQUARK. To investigate this hypothesis, we analyzed the sensitivity of the barometric-pumping efficiency to UNE properties, including properties that were measured or estimated from historic data (depth of burial, air-filled porosity, and matrix permeability). We present these sensitivities in Figure 4, where for depth of burial, air-filled porosity, and matrix permeability, the vertical gray band indicates the range of values present in the data, while for the fracture aperture and spacing, a gray line indicates the value that was used in the analysis in lieu of actual data. Barometric-pumping efficiency is not sensitive to depth of burial within the range in the data, nor well beyond this range. Barometric-pumping efficiency is highly sensitive to air-filled porosity within the range of the data, and beyond this data range. Barometric-pumping efficiency becomes sensitive to matrix permeability at values less than around $10^{-15.5} \text{ m}^2$, however the range of matrix permeabilities in the data is higher than this and thus is in an insensitive region. The fracture aperture is relatively sensitive even at the sub-millimeter scale, while the fracture spacing is relatively insensitive from around 3 to 15 m, but does begin to show increased sensitivity for values less than around 3 m.

5 Discussion

The results of this analysis, based on 16 UNEs from the NNSS, indicate that barometric-pumping efficiency can facilitate the discrimination of UNEs that will result in late-time seeps. Barometric-pumping efficiency is able to account for the character of the barometric signal (frequency and amplitude), depth of burial, air-filled porosity, matrix permeability, fracture aperture, and fracture spacing. The differences in the period/amplitude pairs from the UNEs with late-time seeps versus those without presented in the top plot of Figure 1, along with the geologic data included in the analysis, result in generally higher barometric-pumping efficiency for barometric components associated with UNEs with late-time seeps (bottom plot of Figure 1). While there is overlap between the efficiencies of UNEs with and without late-time seeps, the highest barometric-pumping efficiencies for any given period are generally associated with a UNE with late-time seeps, and the lowest are associated with a UNE without.

The barometric-pumping efficiency analysis is able to discriminate UNEs with late-time seeps based on several factors, particularly air-filled porosity, fracture aperture, and, for values less than around $10^{-15.5} \text{ m}^2$, matrix permeability. If values for these factors can be well-constrained, and the characteristic of the barometric record can be obtained/forecasted at the location shortly before and after the suspected UNE, the approach can be used to forecast whether or not the UNE will result in late-time seeps. Barometric records from a fairly dense network of weather stations are available globally to obtain recent barometric pressures, fairly accurate barometric pressure forecasts out to around 10 days, and historical records to allow extraction of barometric characteristics typical at a site. Such information would be useful in determining the level of effort and expense that should be expended to detect radionuclide gases at the ground surface of the site or in the atmosphere based on the likelihood of late-time seeps.
Figure 2. Average period (top plot) and amplitude (2nd plot) associated with high-efficiency barometric components, depth of burial (3rd plot), air-filled porosity (4th plot), matrix permeability (5th plot), and average max barometric-pumping efficiency (i.e., average of 30 highest efficiencies for each UNE) for 16 UNEs indicated on the x-axis. Red dots correspond to 5 UNEs where late-time seeps were observed. Blue dots correspond to 11 UNEs where gas seeps were not observed. Dashed lines indicate the mean value for each factor associated with UNEs with late-time seeps (red) and without (blue).
Figure 3. Average period versus average amplitude of high-efficiency barometric components. Red dots correspond to 5 UNEs where late-time seeps were observed. Blue dots correspond to 11 UNEs where gas seeps were not observed. The number of days till radionuclide detection after the UNE and radionuclides detected are noted.
Figure 4. Barometric-pumping efficiency as a function of depth of burial (top plot), air-filled porosity (2nd plot), matrix permeability (3rd plot), fracture aperture (4th plot), and fracture spacing (5th plot). The range in the data from the 16 UNEs are indicated by a gray shaded region for depth of burial, air-filled porosity, and matrix permeability. The value used in the barometric-pumping efficiency analysis for fracture aperture and fracture spacing are indicated by gray lines.
The UNEs with late-time seeps have generally longer average high-efficiency periods and higher average high-efficiency amplitudes than the UNEs without (Figure 3). The magnitudes of the average high-efficiency periods and amplitudes of UNEs without late-time seeps decrease in general and become less distinguishable from the UNEs without late-time seeps as the number of days until radionuclide detection increases (refer to days until radionuclide detection noted in Figure 3). This suggests that the barometric-pumping efficiency analysis is able to easily discriminate UNEs that are the most likely to have late-time seeps (e.g., BODIE and BARNWELL), UNEs that may or may not have late-time seeps (e.g., TIERRA (observed late-time seeps) and EGMONT (no observed late-time seeps)), and UNEs that are likely to remain contained. Note that KAPPELI was unique in the set of UNEs with late-time seeps in that it took much longer to seep (more than twice as long as any other UNE) and no xenon isotopes were detected, only $^{85}$Kr. The UNEs without observed late-time seeps which had higher high-efficiency amplitudes and longer high-efficiency periods labeled in Figure 3 (EGMONT, TOWANDA, and BELMONT) do not have distinguishable geologic properties in common compared to the other UNEs without observed late-time seeps or that can distinguish them from UNEs with late-time seeps with similar high-efficiency periods and amplitudes (TIERRA and LABQUARK) (refer to Figure 2).

If knowledge was available regarding the fracture aperture, and to a lesser extent, the fracture spacing, further separation between the efficiencies of UNEs with late-time seeps vs those without may occur. For example, we demonstrate in Figure 5 that by simply increasing the fracture aperture associated with KAPPELI, TIERRA, and LABQUARK by half a millimeter (from 1 mm to 1.5 mm), their efficiencies become comparable to BODIE and BARNWELL and distinct from the UNEs without observed late-time seeps. Of course, there is no basis for this modification, but it does indicate that a small change in fracture properties can have a large effect on barometric-pumping efficiency and that the availability of this information can greatly constrain the analysis.

Barometric-pumping efficiency does not consider the UNE yield. The unclassified yield of the 16 UNEs considered here is 20-150 kt; therefore, differences in yield between these bounds may also explain why some had late-time seeps and others did not. Barometric-pumping efficiency also does not consider the pressurization and thermal effects on gas transport that would be associated with a UNE, which will be a function of yield. While these effects may help discriminate UNEs with late-time seeps, Bourret, Kwicklis, Miller, and Stauffer (2019) found that considering barometrically-induced gas seepage alone al-
ollowed numerical simulations of BARNWELL to produce consistent results with late-time seep measurements.

6 Conclusions

• UNEs with late-time seeps generally have higher barometric-pumping efficiencies than those without.
• UNEs with late-time seeps generally have higher high-efficiency amplitudes and longer high-efficiency periods than those without.
• The most sensitive geologic factors to aid in discriminating UNEs that are likely to have late-time seeps are air-filled porosity, fracture aperture, and matrix permeability ($< 5 \times 10^{-15} \text{ m}^2$)
• For the 5 UNEs with late-time seeps evaluated here, the time to detect a late-time seep decreases as the high-efficiency amplitudes and period lengths increase.
• UNEs with the shortest time to radionuclide gas detection had the highest high-efficiency amplitudes and longest high-efficiency periods, indicating that they are likely easier to discriminate.

Acknowledgments

This research is supported by National Nuclear Security Administration Office of Defense Nuclear Nonproliferation Research and Development and the Defense Threat Reduction Agency. Los Alamos National Laboratory completed this work under the auspices of the U.S. Department of Energy under contract DE-AC52-06NA24596 and 89233218CNA000001. The authors acknowledge the use of barometric pressure data from Weather Underground (www.wunderground.com).

References


Supporting Information for “Discriminating underground nuclear explosions leading to late-time radionuclide gas leakage”
Dylan R. Harp, S. Michelle Bourret, Philip H. Stauffer, and Edward M. Kwicklis

Computational Earth Science, Los Alamos National Laboratory, Los Alamos, NM, 87545

Analysis of average high-efficiency periods and amplitudes

Identifying representative periods and amplitudes of barometric components with high barometric-pumping efficiency aids in discriminating underground nuclear explosions (UNEs) that lead to late-time leakage. The first step in this process is to sort the barometric components (periods and amplitudes) associated with an UNE in order of decreasing barometric-pumping efficiency. Next, the cumulative mean is calculated for periods and amplitudes, starting at the highest barometric-pumping efficiency, in order to identify a representative average period and amplitude of high-efficiency barometric components. These efficiency-sorted, cumulative mean periods and amplitudes are shown in the first and third plot in Figure S1. Identifying characteristic high-efficiency average periods and amplitudes from these curves is difficult due to the erratic nature of the curves. Therefore, the curves are smoothed using a moving average approach using a 30 data point window.
shown for the cumulative mean periods and amplitudes in the second and fourth plot in Figure S1. Using these smoothed curves, characteristic, high-efficiency mean periods and amplitudes are easily identified as the maximum value along the curves. These values are used as the average high-efficiency periods and amplitudes. Although there is overlap, the leaked UNEs generally have longer high-efficiency periods and higher high-efficiency amplitudes than contained UNEs.
Figure S1. Cumulative mean period calculated in order of decreasing barometric pumping efficiency for raw (non-smoothed) period (top plot) and amplitude (3rd plot) and for smoothed period (2nd plot) and amplitude (bottom plot).